

Using Mixture Density Networks to infer the interior structure of exoplanets

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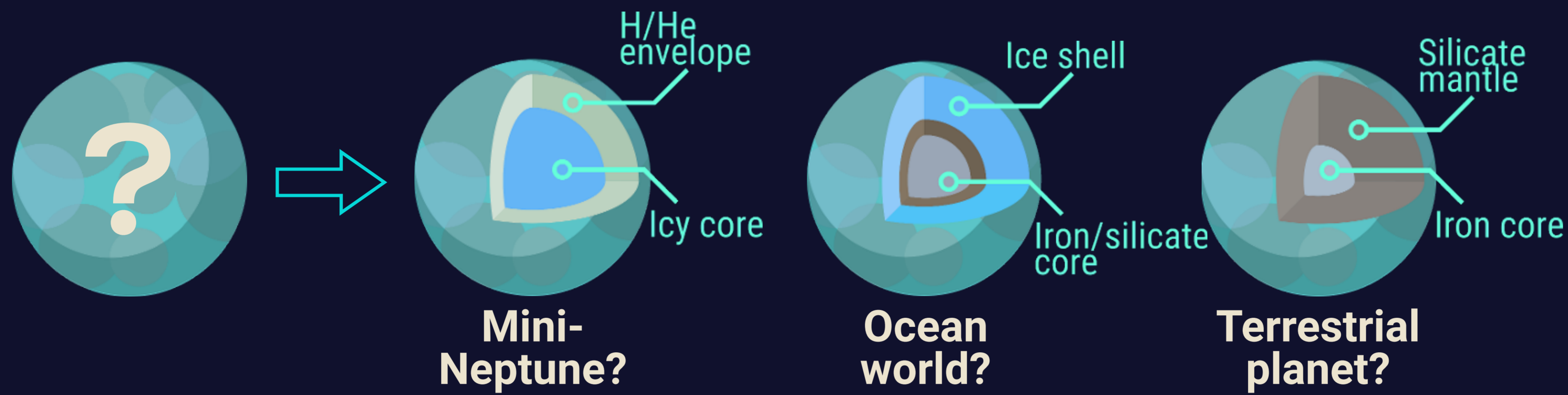
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Exoplanet observations

For most exoplanets, only **mass** and **radius** can be measured. To understand these planets better, we need to know their interior structure.

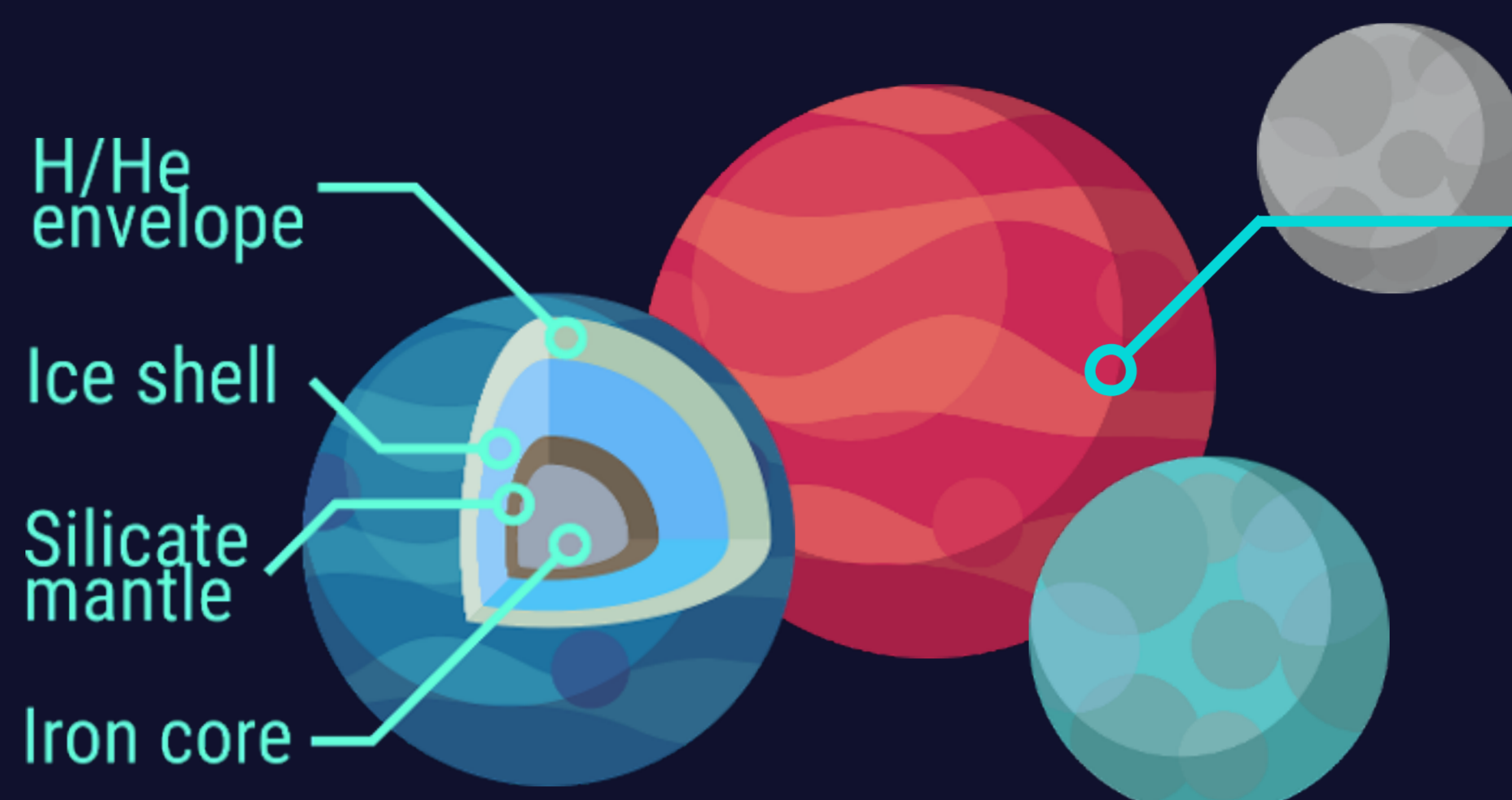


Interior structures

With only **mass** and **radius**, many solutions for the interior are possible^[1]. To find all interior structures, we need to run thousands of interior models for a given planet. This can be computationally expensive and time consuming.

Our approach

1. Compute set of planets with different interior structures covering a wide **mass** and **radius** range
2. Train a neural network to predict the interior structure based on **mass** and **radius**
3. Use network predictions instead of time-consuming forward models
4. Test with Solar System planets, where we have the most accurate data



Training data

- 900 000 synthetic planets with random interior structures
- Each planet has:
 - Iron-rich **core**
 - Silicate **mantle**
 - High-pressure **ice shell**
 - H/He **gas envelope** (solar-like)
- Planet **mass**: 0.01 - 25 M_{Earth}
- 70% used for training
- 30% used for validation

Mixture Density Networks

A **Mixture Density Network** is similar to a conventional Neural Network, but instead of single target values it predicts continuous parameters in form of a **mixture of normal distributions**.

MDNs work well with inverse problems, where each input has multiple output values.

Network architecture

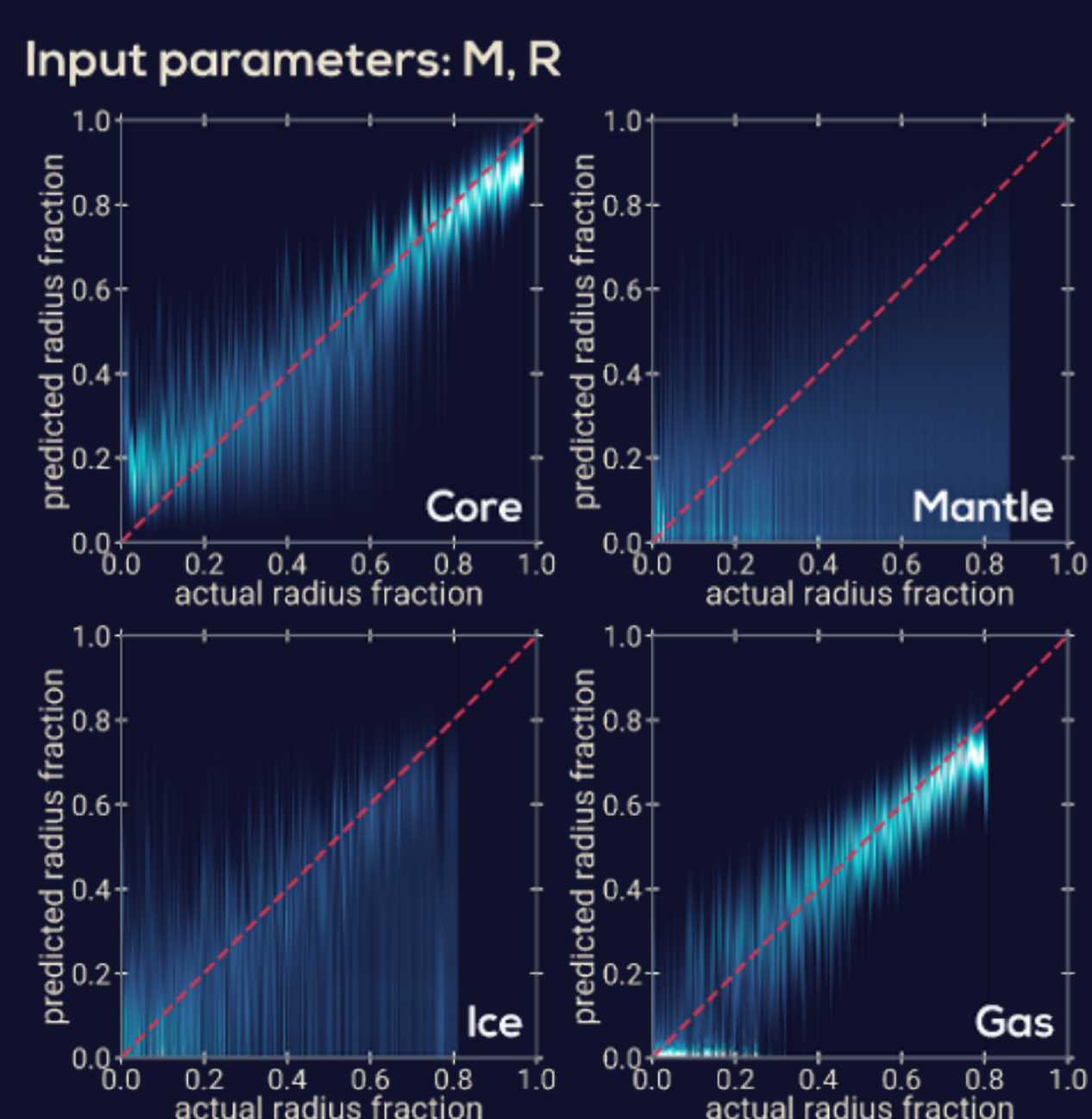
- 3 hidden layers with 512 neurons each
- Dropout layers before each hidden layer to improve robustness of model
- Outputs: Mixture density parameters

Results

- Predicted distributions align very well with distributions obtained by Monte-Carlo sampling the same prior distribution
- Predicted **Earth**:
 - Predominantly **metal-rich/silicate** planet
 - Thick **ice shell** possible
 - Small **gas envelope** possible
- Predicted **Neptune**:
 - Predominantly **gaseous** with small **iron core**
 - **Ice** and **mantle** not well constrained

Fluid Love number k_2

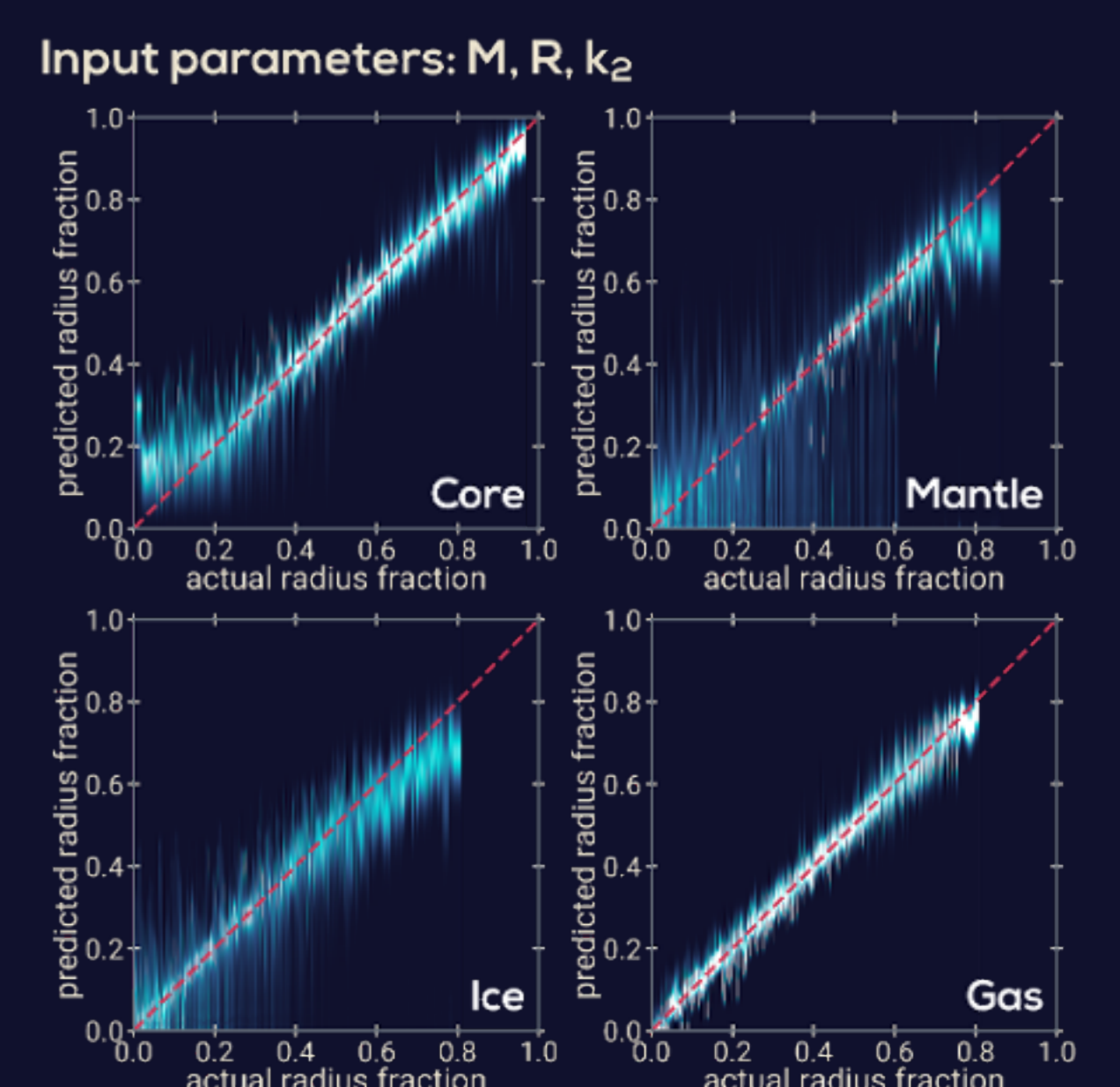
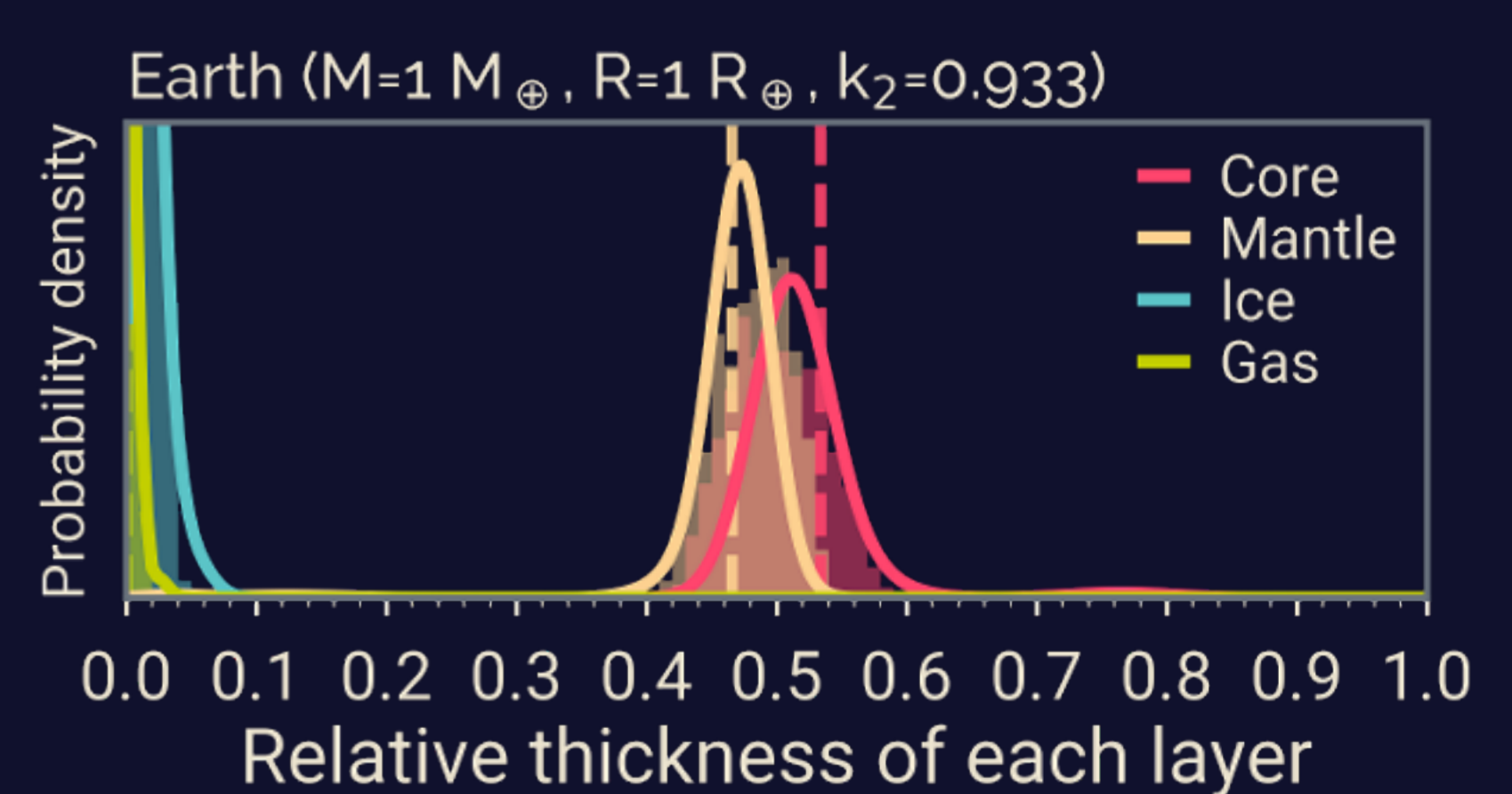
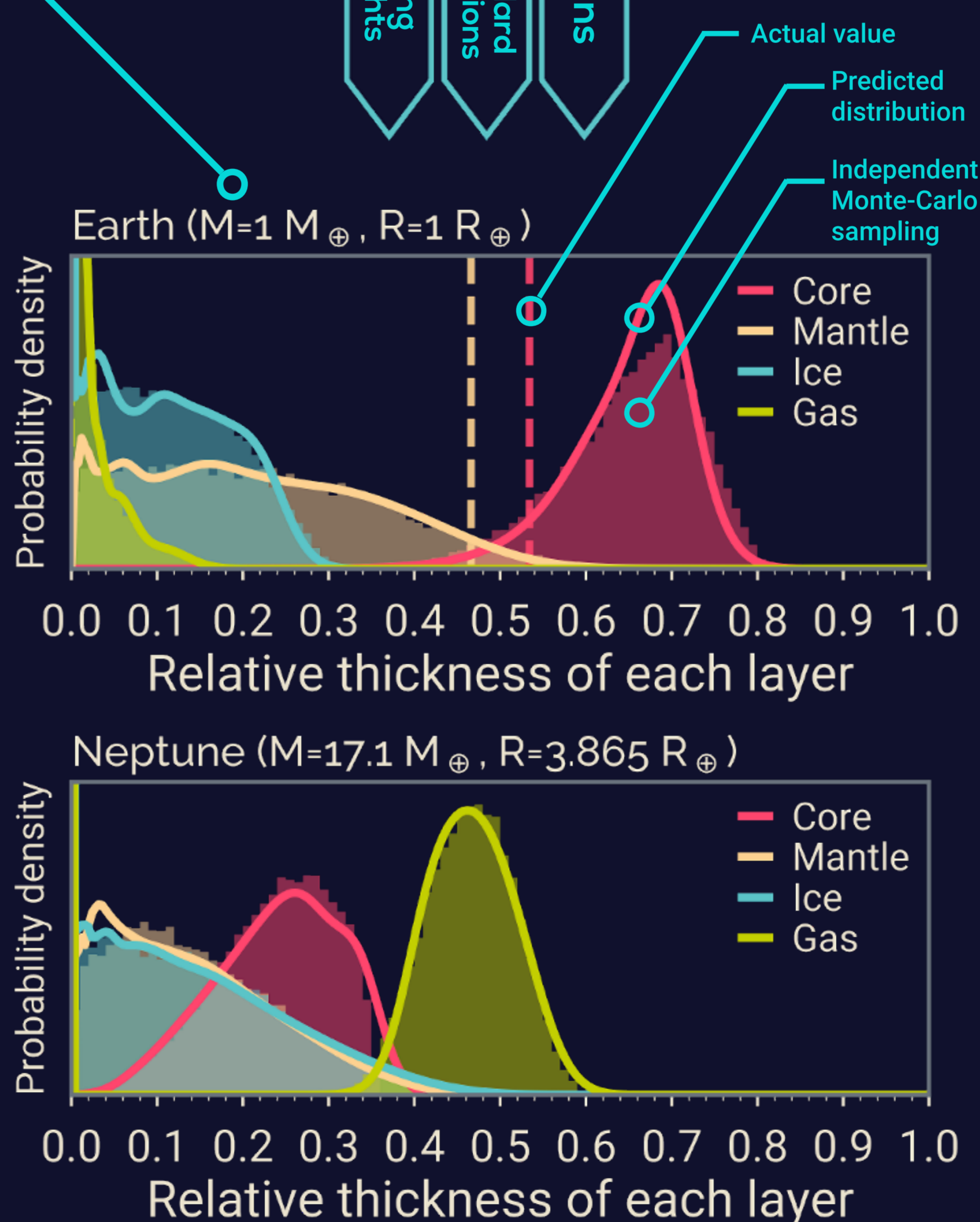
- k_2 is a measure of the mass concentration in the planet^[3]
- Measurable from shape and dynamics of the planet^[4]
- Using k_2 as additional input:
 - Interior structures constrained significantly better for all layers
 - Earth's interior predicted to within a few percent of the actual values



Accuracy

Each subplot shows the predicted layer thickness over the actual value from the validation data. Predictions on the **red** line are well constrained

- **Core** and **gas** layers are fairly well constrained
- **Mantle** and **ice** layers can not be constrained well



Acknowledgements

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References

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