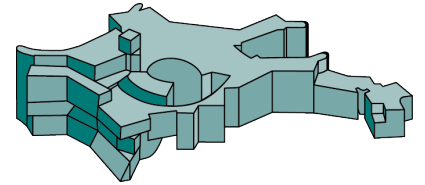


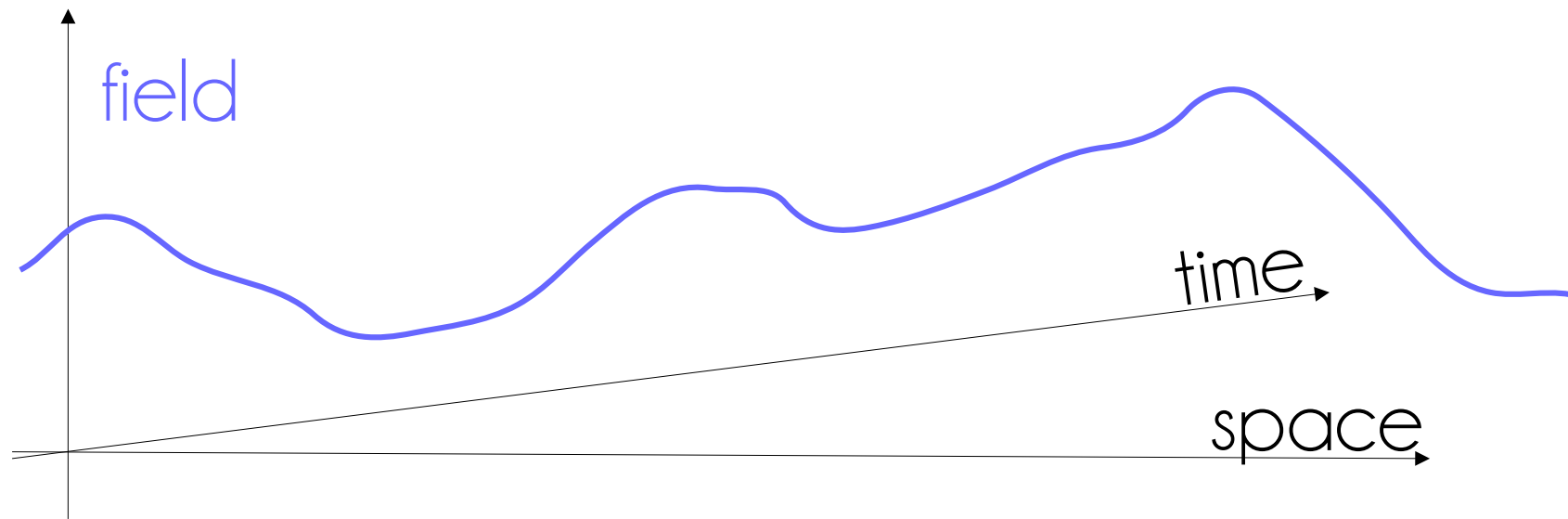
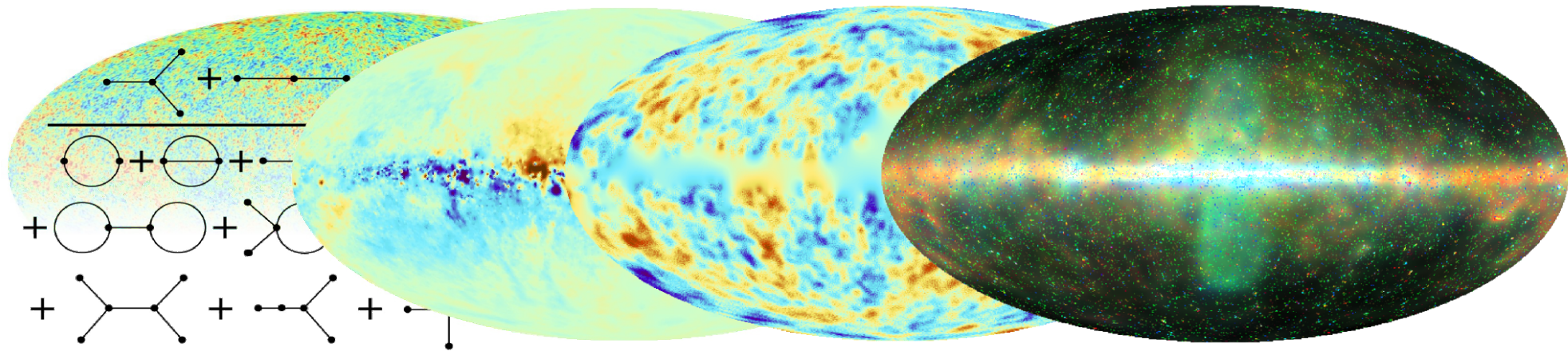
# Information field theory

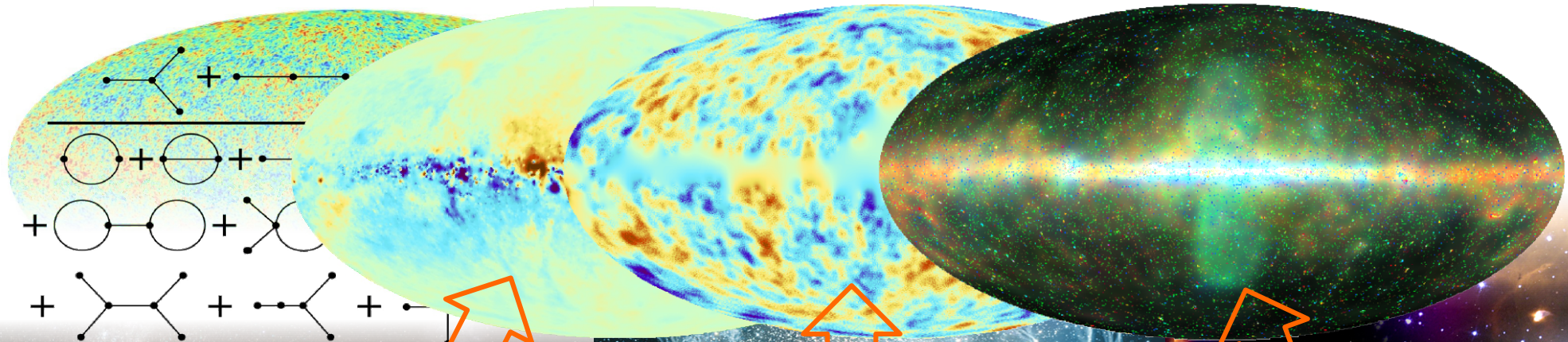


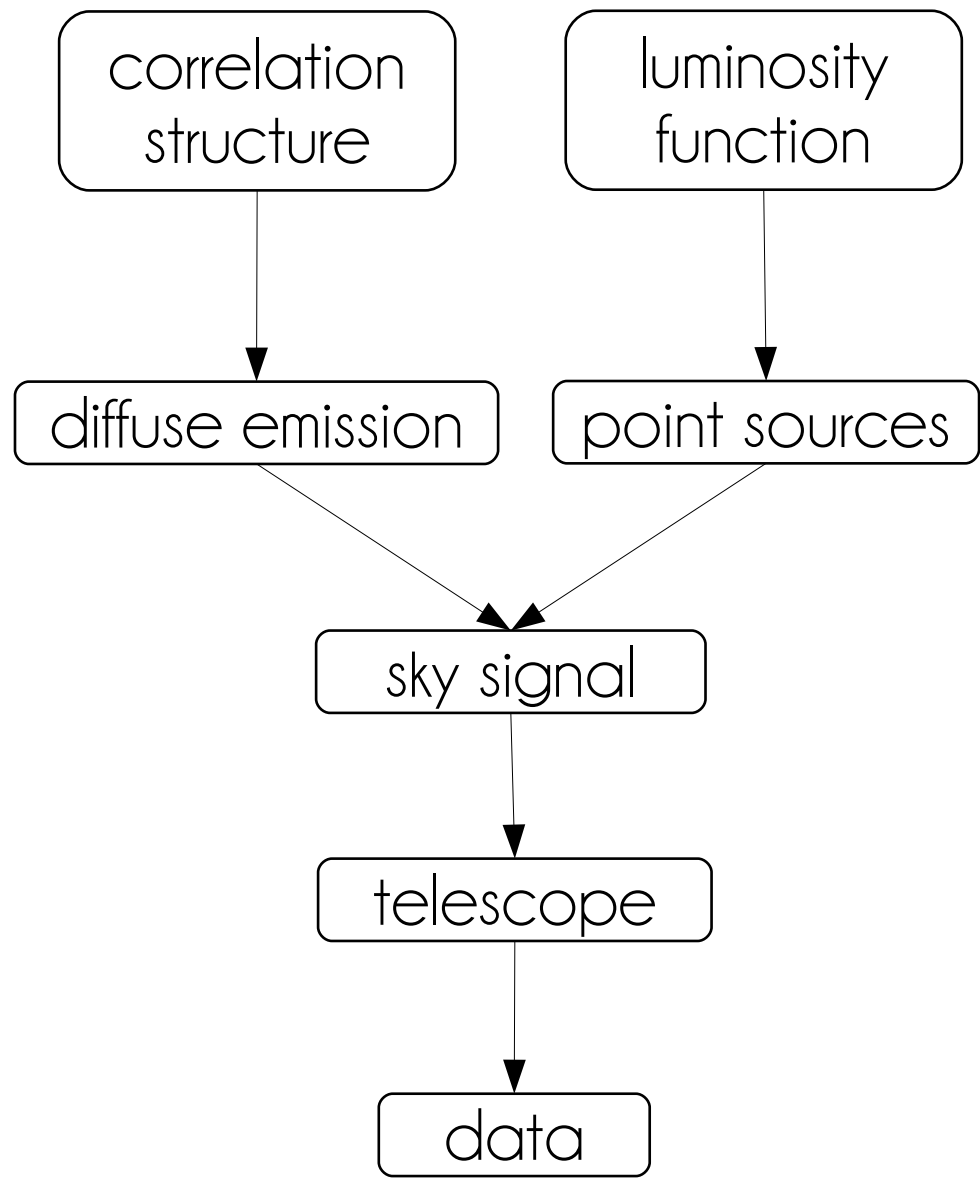
**Torsten Enßlin**  
MPI for Astrophysics  
Ludwig Maximilian University Munich

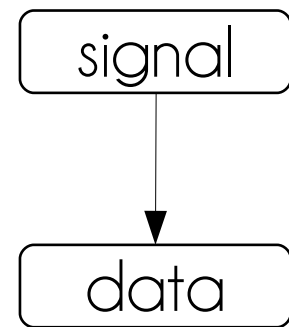
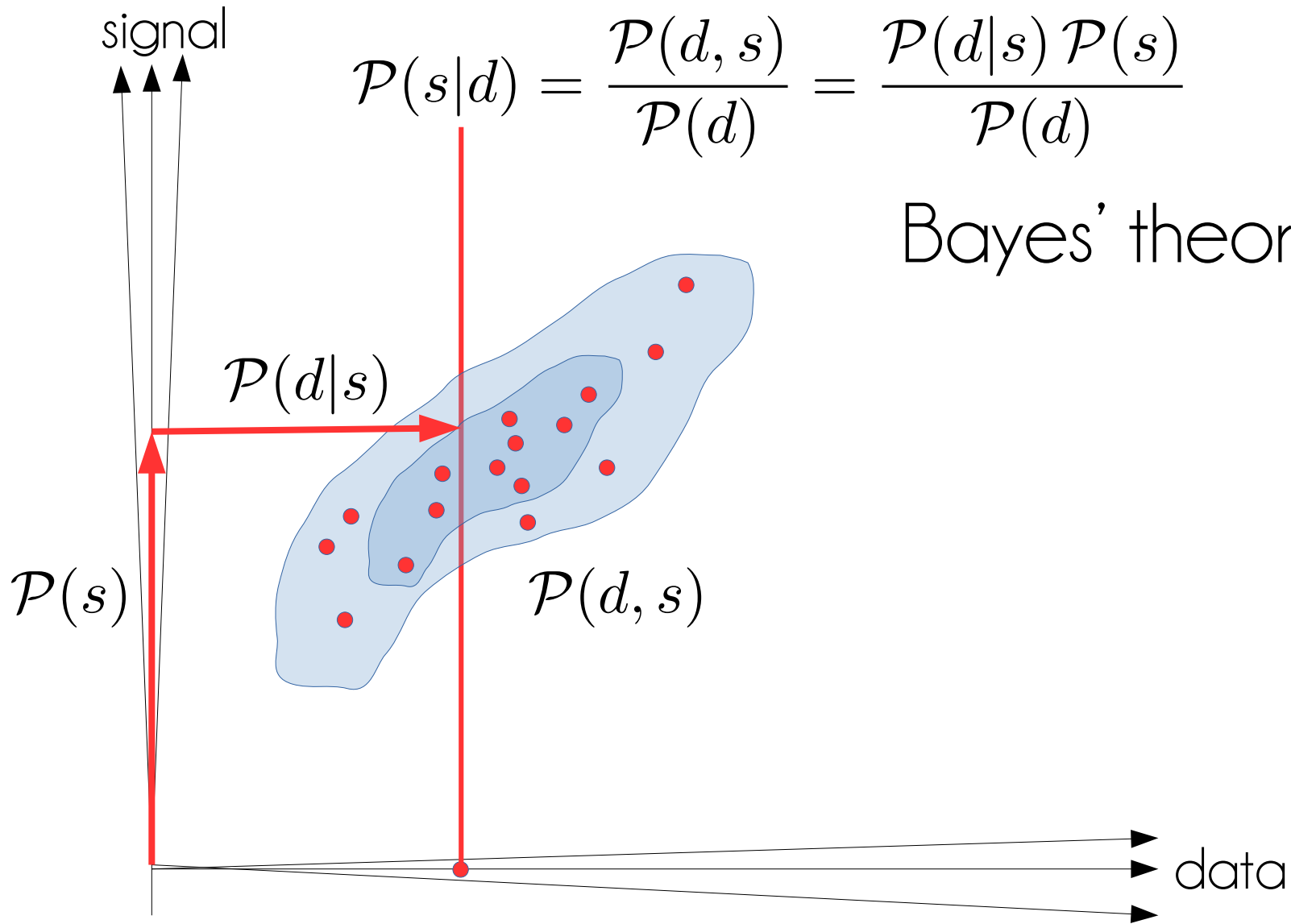


**IFT Team:** Philipp Arras, Michael Bell, Vanessa Böhm, Sebastian Dorn, Martin Dupont, Mona Frommert, Philipp Frank, Mahsa Ghaempanah, Maksim Greiner, Philipp Haim, Sebastian Hutschenreuter, Henrik Junklewitz, Francisco-Shu Kitaura, Jakob Knollmüller, Christoph Lienhard, Reimar Leike, Ancla Müller, Johannes Oberpriller, Niels Oppermann, Natalia Porquerese, Daniel Pumpe, Tiago Ramalho, Martin Reinecke, Julia Stadler, Marco Selig, Theo Steininger, Valentina Vacca, Cornelius Weig, Margret Westerkamp, & many more









# Information theory

$$\mathcal{P}(s|d) = \frac{\mathcal{P}(d, s)}{\mathcal{P}(d)} = \frac{e^{-\mathcal{H}(d, s)}}{\mathcal{Z}(d)}$$

$$\mathcal{H}(d, s) = -\log \mathcal{P}(d, s)$$

Information

$$\mathcal{Z}(d) = \mathcal{P}(d)$$

$$= \int \mathcal{D}s \mathcal{P}(d, s)$$

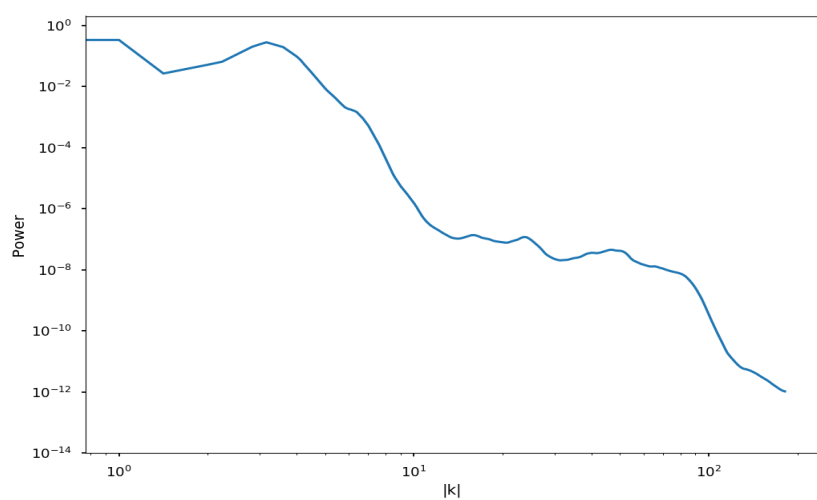
$$\mathcal{P}(d, s) = \mathcal{P}(d|s) \mathcal{P}(s)$$

$$\mathcal{H}(d, s) = \mathcal{H}(d|s) + \mathcal{H}(s)$$

is additive

**metric**

**regularization**



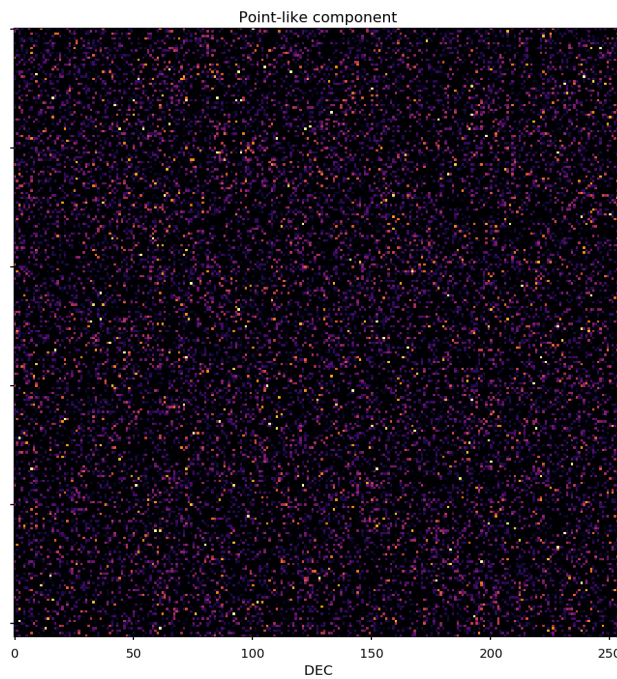
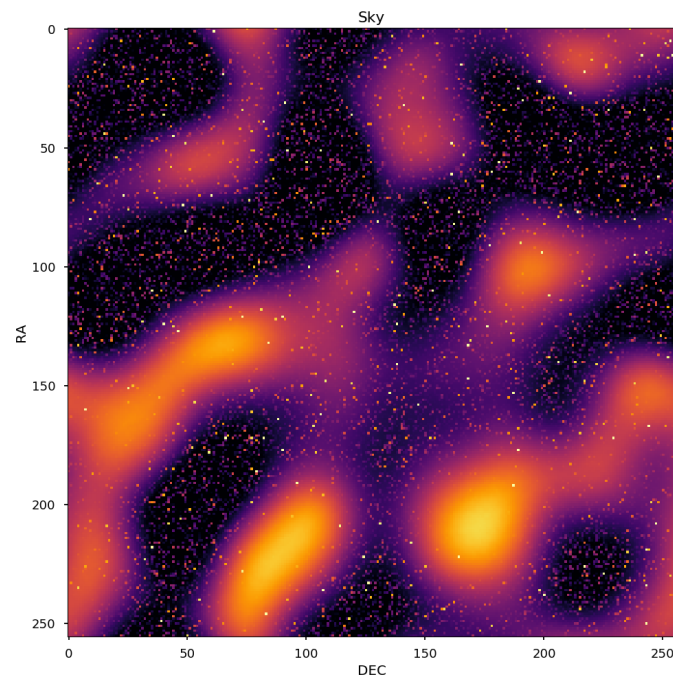
$$\mathcal{P}(s)$$

correlation  
structure

luminosity  
function

diffuse emission

point sources



sky signal

telescope

data

$$\mathcal{P}(d|s)$$

# Photon counting instrument: Log-normal Poisson model

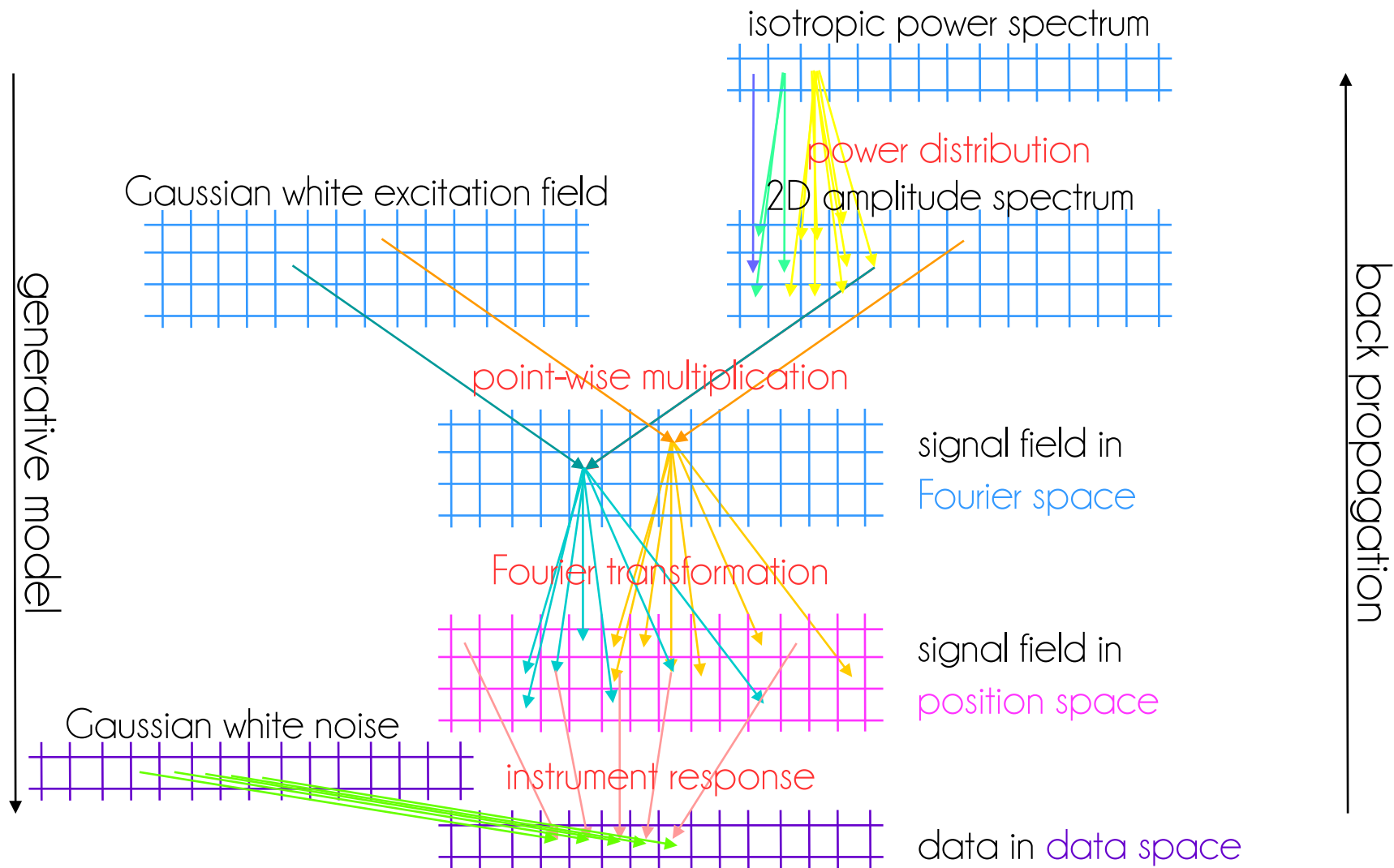




# Information

$$\begin{aligned}\mathcal{H}(\mathbf{d}, \mathbf{s}, \boldsymbol{\tau}) &= -\log \mathcal{P}(\mathbf{d}, \mathbf{s}, \boldsymbol{\tau}) \\ &= \mathbf{1}^\dagger [\log(d!) + \mathbf{R} (e^{\mathbf{s}} + e^{\mathbf{u}})] - \mathbf{d}^\dagger \log [\mathbf{R} (e^{\mathbf{s}} + e^{\mathbf{u}})] \\ &\quad + \frac{1}{2} \mathbf{s}^\dagger \mathbf{S}^{-1} \mathbf{s} + \frac{1}{2} \log (\det [\mathbf{S}]) \\ &\quad + (\boldsymbol{\alpha} - \mathbf{1})^\dagger \boldsymbol{\tau} + \mathbf{q}^\dagger e^{-\boldsymbol{\tau}} + \frac{1}{2} \boldsymbol{\tau}^\dagger \mathbf{T} \boldsymbol{\tau} \\ &\quad + (\boldsymbol{\beta} - \mathbf{1})^\dagger \mathbf{u} + \boldsymbol{\eta}^\dagger e^{-\mathbf{u}} \\ \mathbf{S} &= \sum_k e^{\tau_k} \mathbf{S}_k\end{aligned}$$

# IFT as neural network





## NIFTy – Numerical Information Field Theory

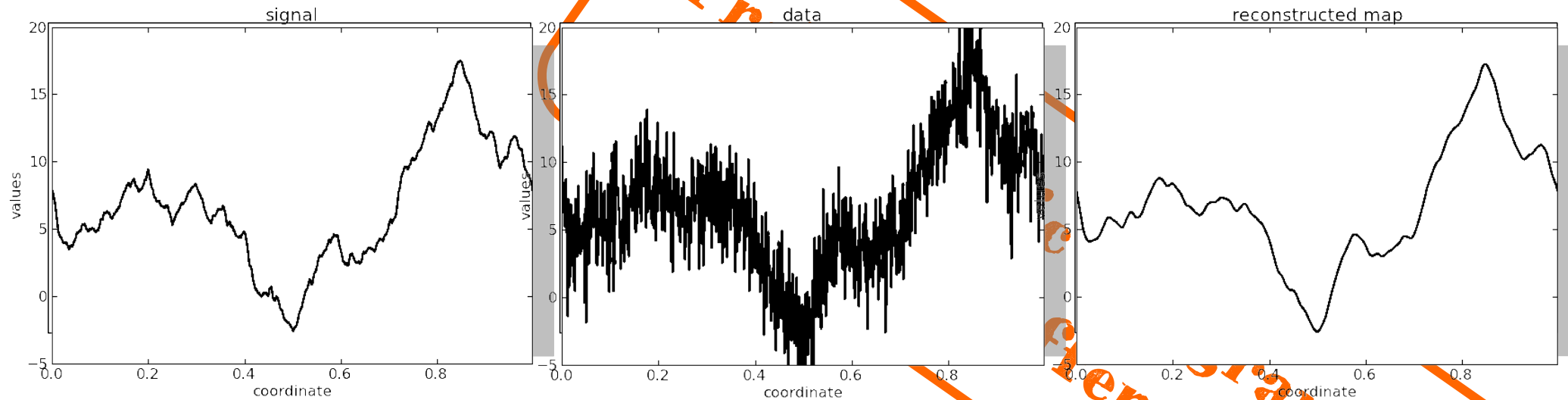
NIFTy <sup>[1]</sup>, <sup>[2]</sup>, "Numerical Information Field Theory" is a versatile library designed to enable the development of signal inference algorithms that are independent of the underlying grids (spatial, spectral, temporal, ...) and their resolutions. Its object-oriented framework is written in Python.

**Probabilistic programming  
with auto-differentiation**



## NIFTy – Numerical Information Field Theory

NIFTy [1], [2], "Numerical Information Field Theory" is a versatile library designed to enable the development of signal inference algorithms that are independent of the underlying grids (spatial, spectral, temporal, ...) and their resolutions. Its object-oriented framework is written in Python.

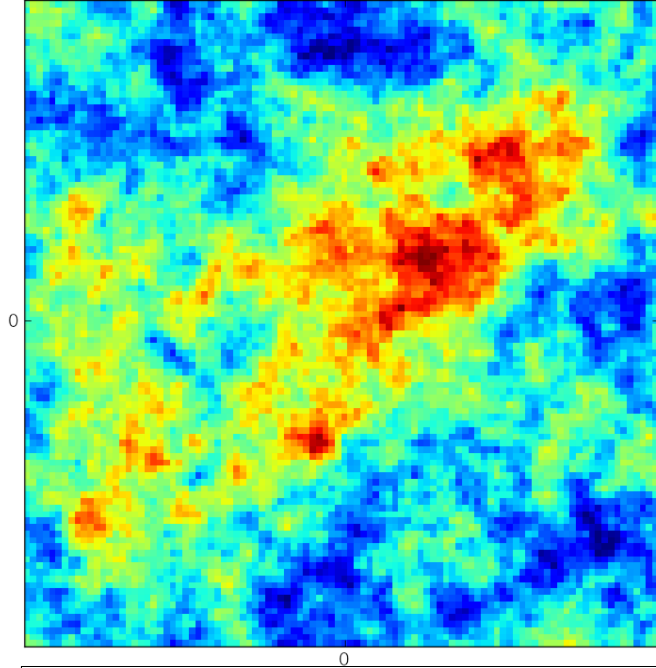


```
import nifty5 as ift
s_space = ift.RGSpace([N])
```

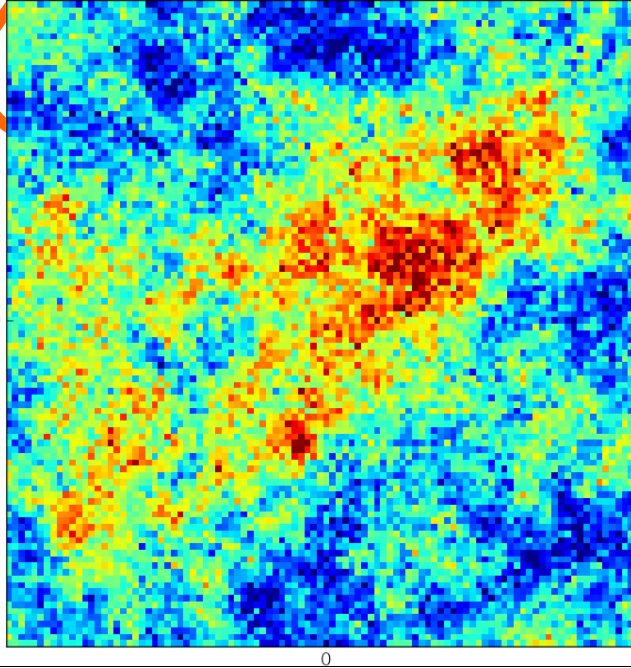
## NIFTy – Numerical Information Field Theory

NIFTy [1], [2], "Numerical Information Field Theory" is a versatile library designed to enable the development of signal inference algorithms that are independent of the underlying grids (spatial, spectral, temporal, ...) and their resolutions. Its object-oriented framework is written in Python.

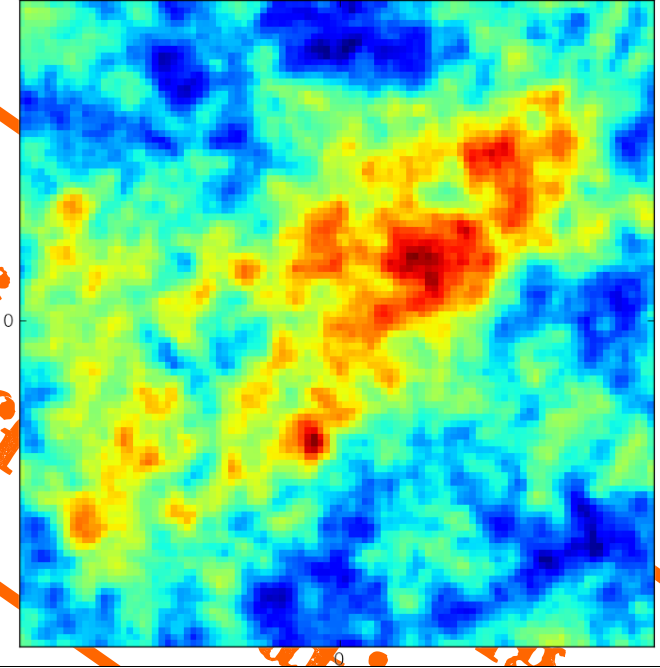
signal



data



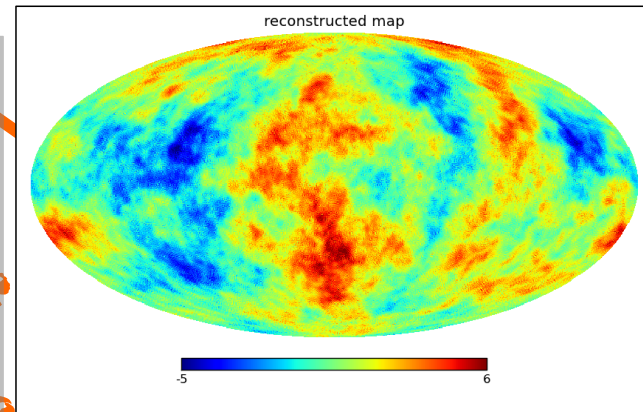
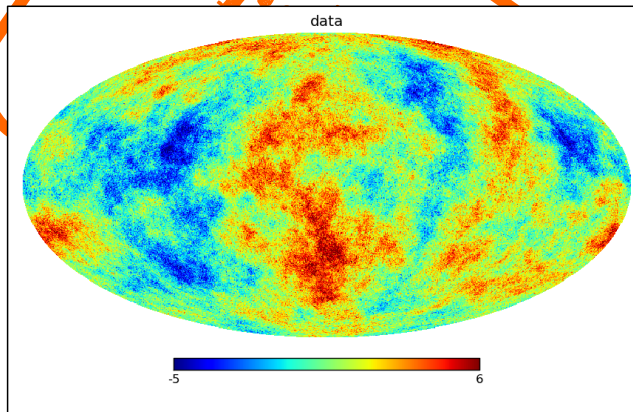
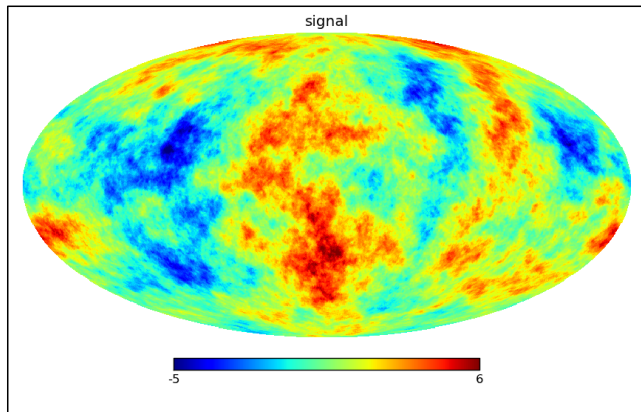
reconstructed map



```
import nifty5 as ift
s_space = ift.RGSpace([N,N])
```

## NIFTy – Numerical Information Field Theory

NIFTy [1], [2], "Numerical Information Field Theory" is a versatile library designed to enable the development of signal inference algorithms that are independent of the underlying grids (spatial, spectral, temporal, ...) and their resolutions. Its object-oriented framework is written in Python.



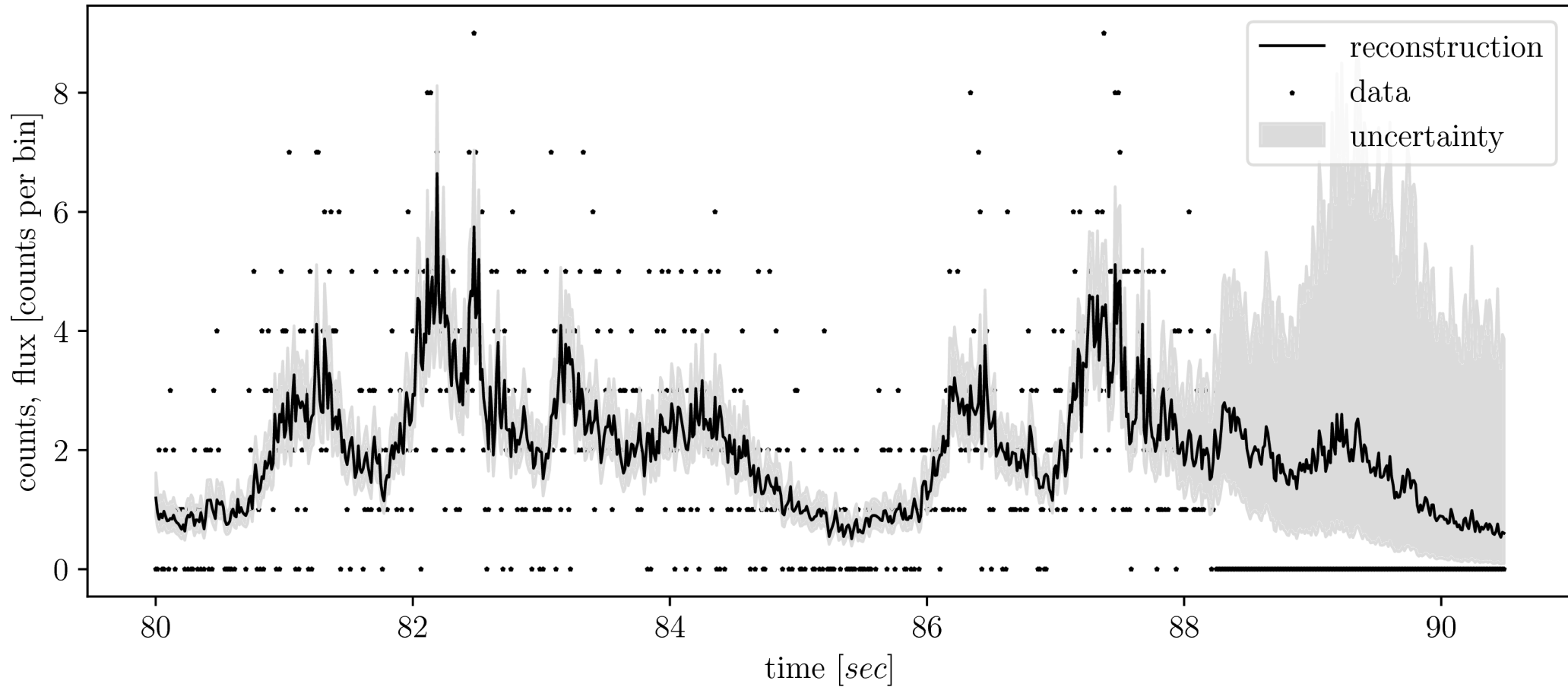
```
import nifty5 as ift  
s_space = ift.HPSpace(NSide)
```

# Information

$$\begin{aligned}\mathcal{H}(\mathbf{d}, \mathbf{s}, \boldsymbol{\tau}) &= -\log \mathcal{P}(\mathbf{d}, \mathbf{s}, \boldsymbol{\tau}) \\ &= \mathbf{1}^\dagger [\log(d!) + \mathbf{R} (e^{\mathbf{s}} + e^{\mathbf{u}})] - \mathbf{d}^\dagger \log [\mathbf{R} (e^{\mathbf{s}} + e^{\mathbf{u}})] \\ &\quad + \frac{1}{2} \mathbf{s}^\dagger \mathbf{S}^{-1} \mathbf{s} + \frac{1}{2} \log (\det [\mathbf{S}]) \\ &\quad + (\boldsymbol{\alpha} - \mathbf{1})^\dagger \boldsymbol{\tau} + \mathbf{q}^\dagger e^{-\boldsymbol{\tau}} + \frac{1}{2} \boldsymbol{\tau}^\dagger \mathbf{T} \boldsymbol{\tau} \\ &\quad + (\boldsymbol{\beta} - \mathbf{1})^\dagger \mathbf{u} + \boldsymbol{\eta}^\dagger e^{-\mathbf{u}} \\ \mathbf{S} &= \sum_k e^{\tau_k} \mathbf{S}_k\end{aligned}$$

# Magnetar flare SGR 1900+14

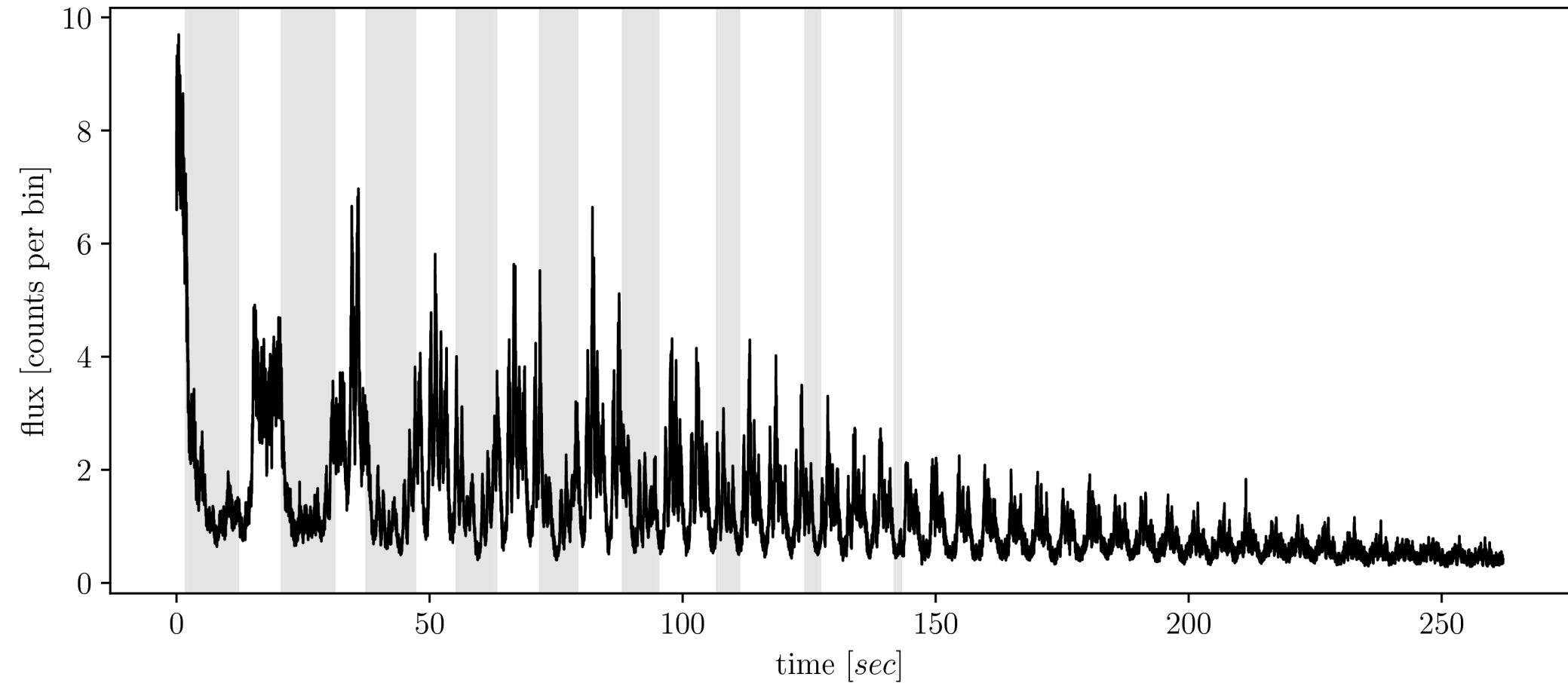
Pumpe et al. (2018)





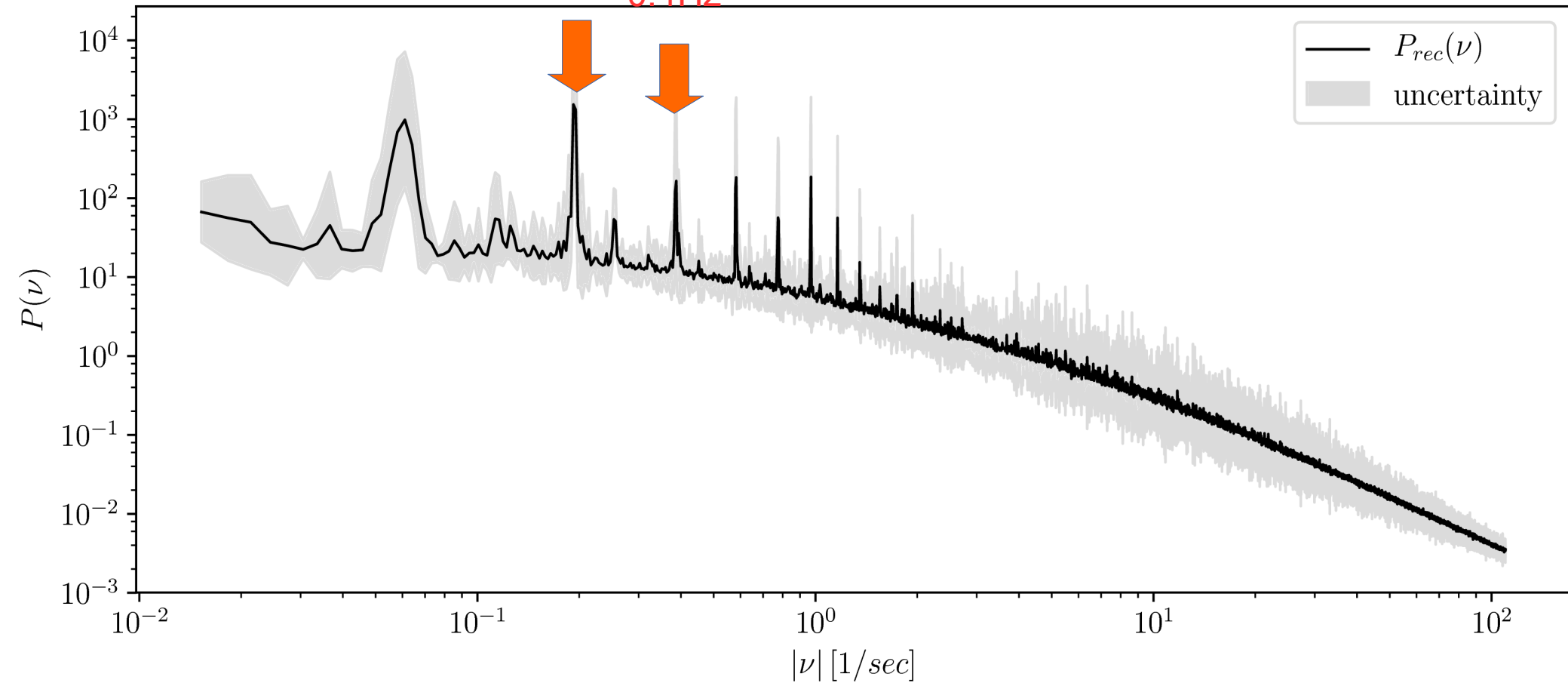
# Magnetar flare SGR 1900+14

Pumpe et al. (2018)



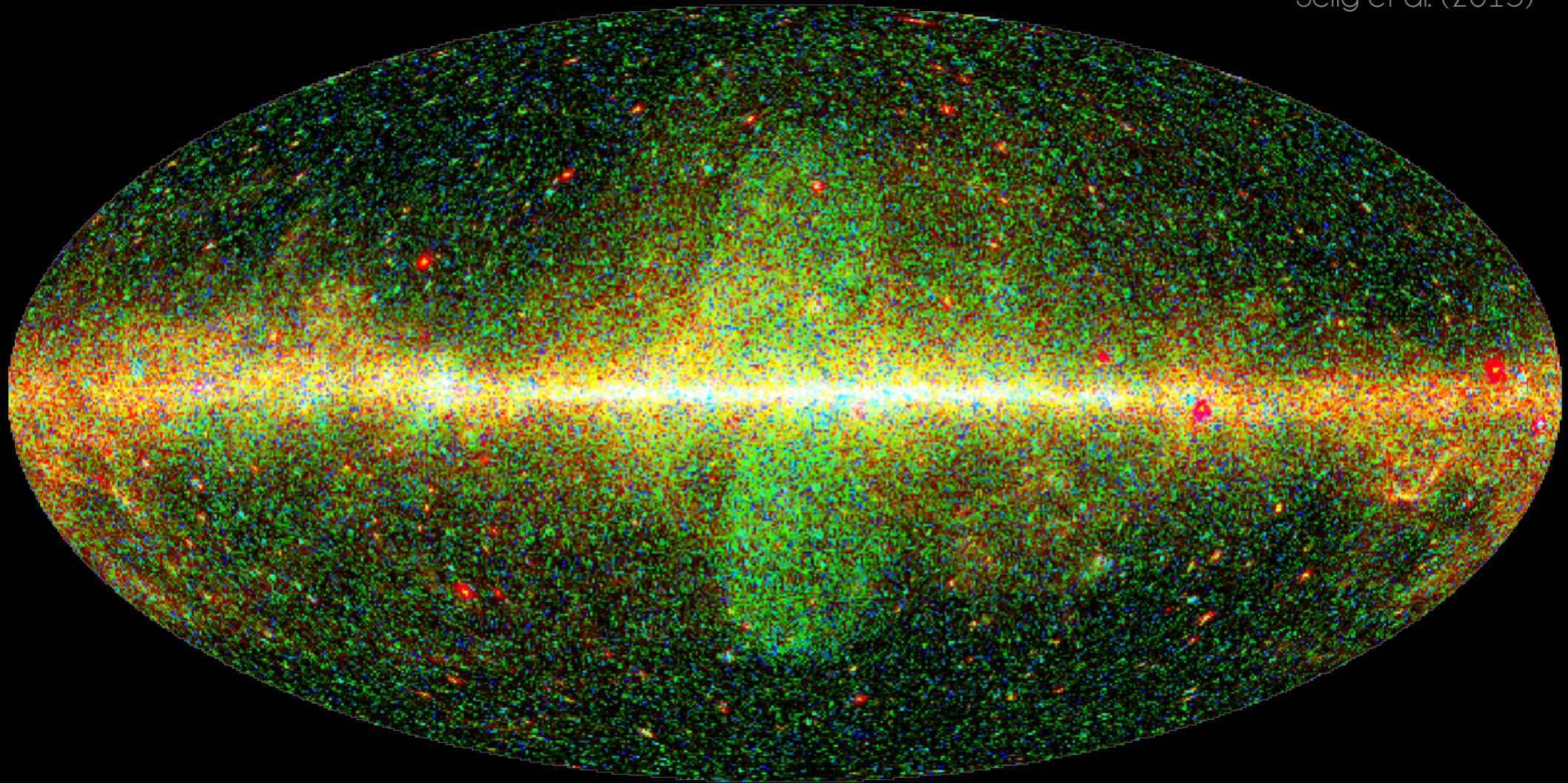
# Magnetar flare SGR 1900+14

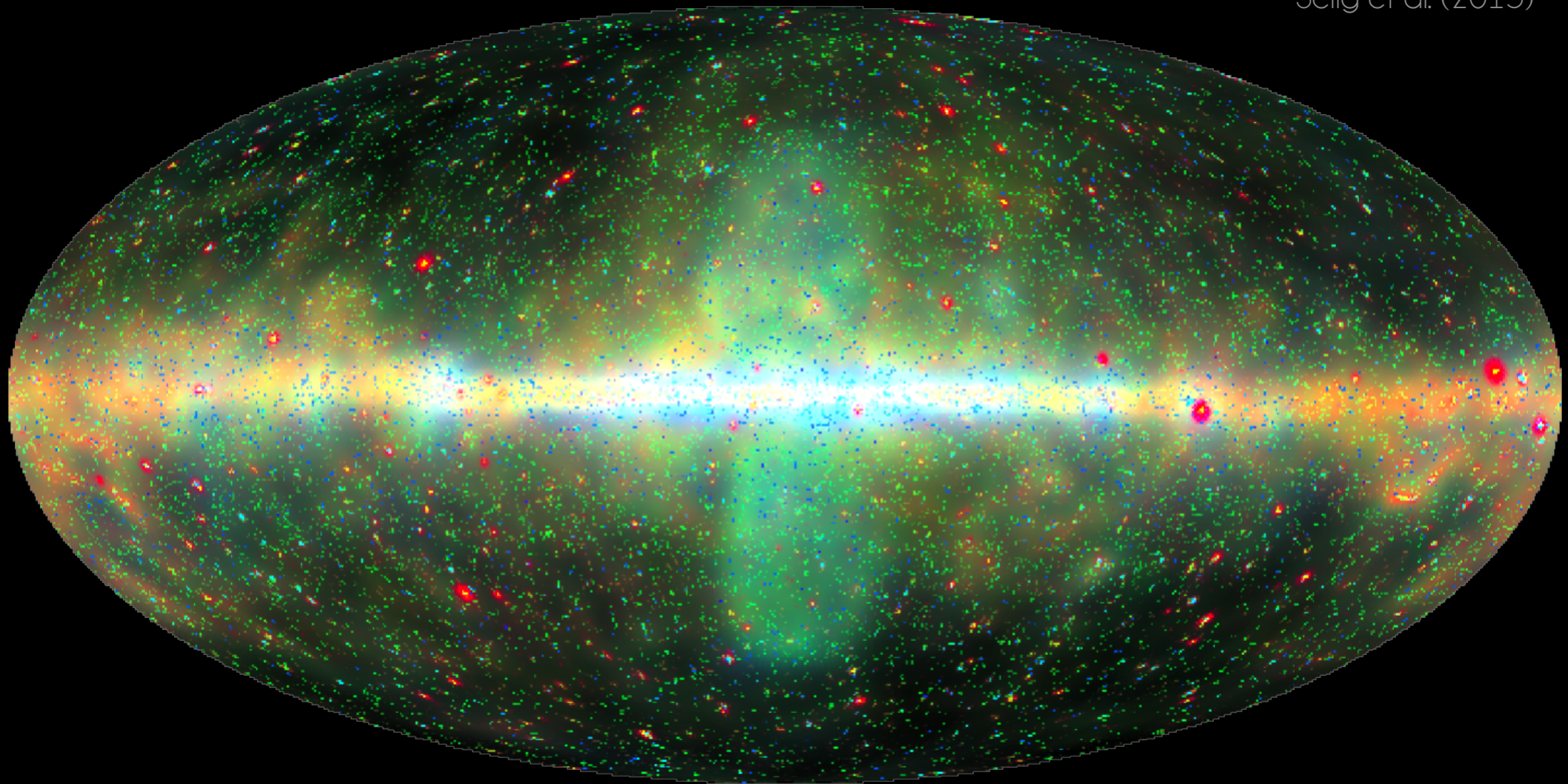
0.2Hz Pumpe et al. (2018)  
0.4Hz

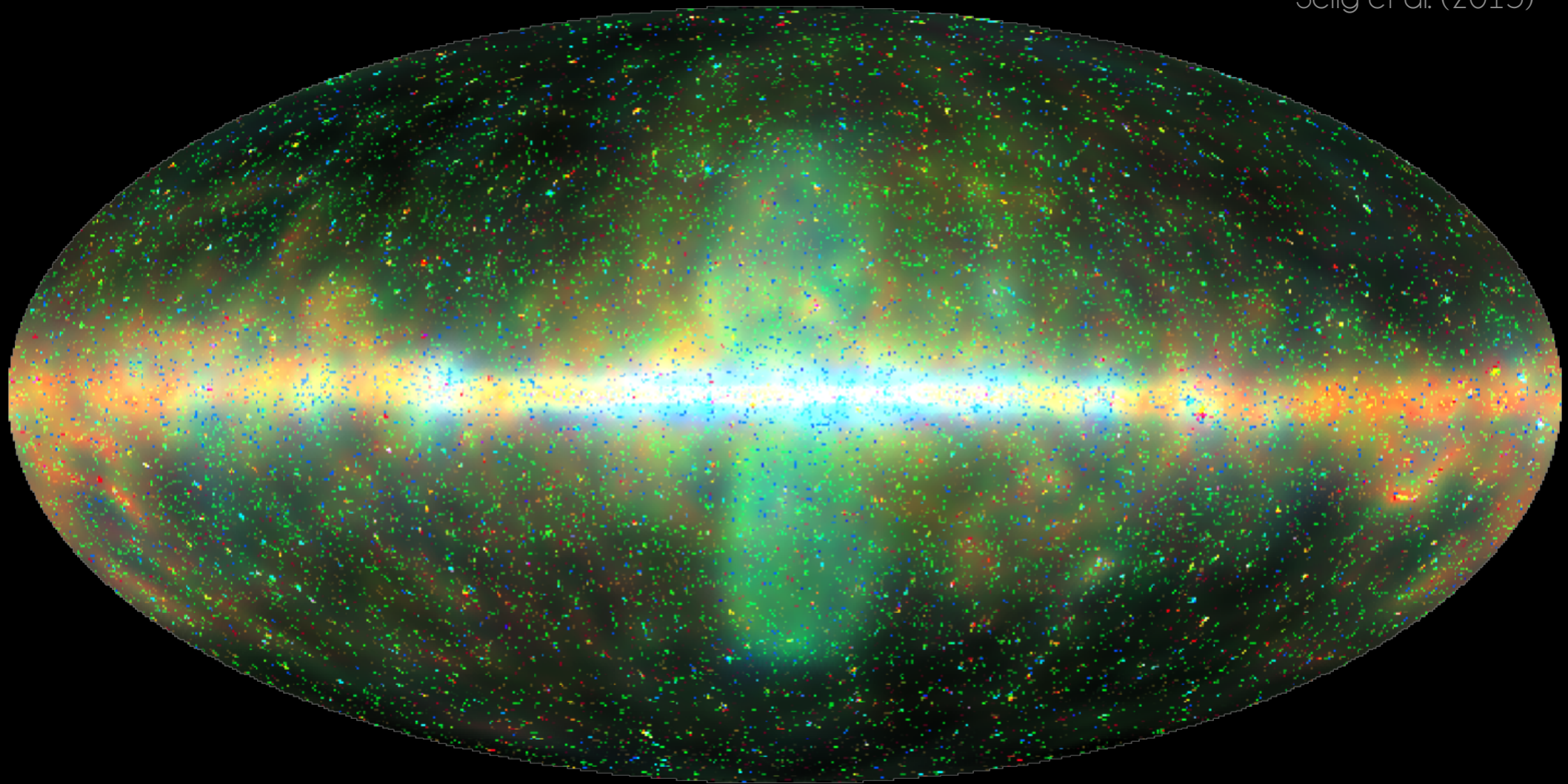


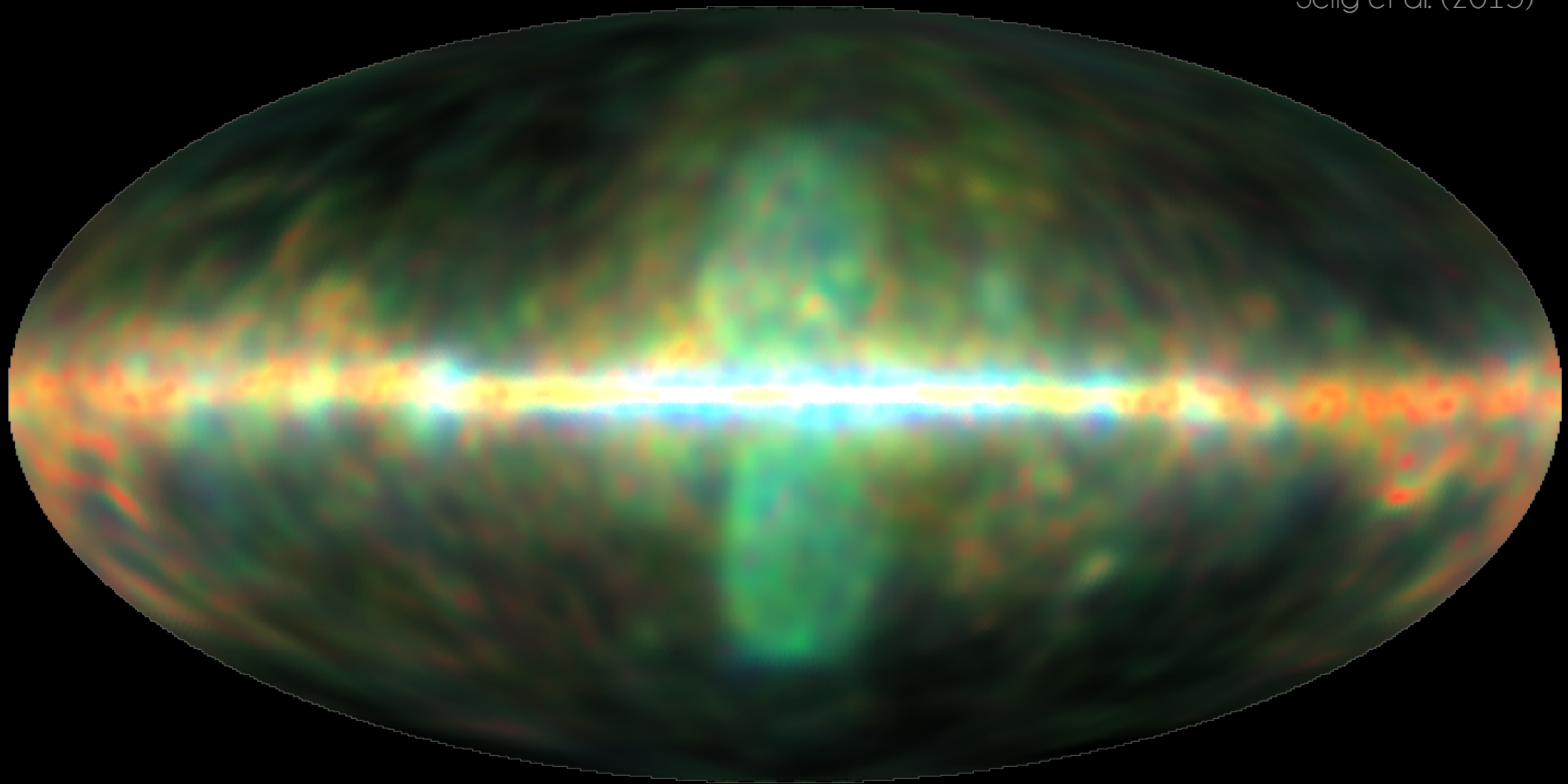
# Information

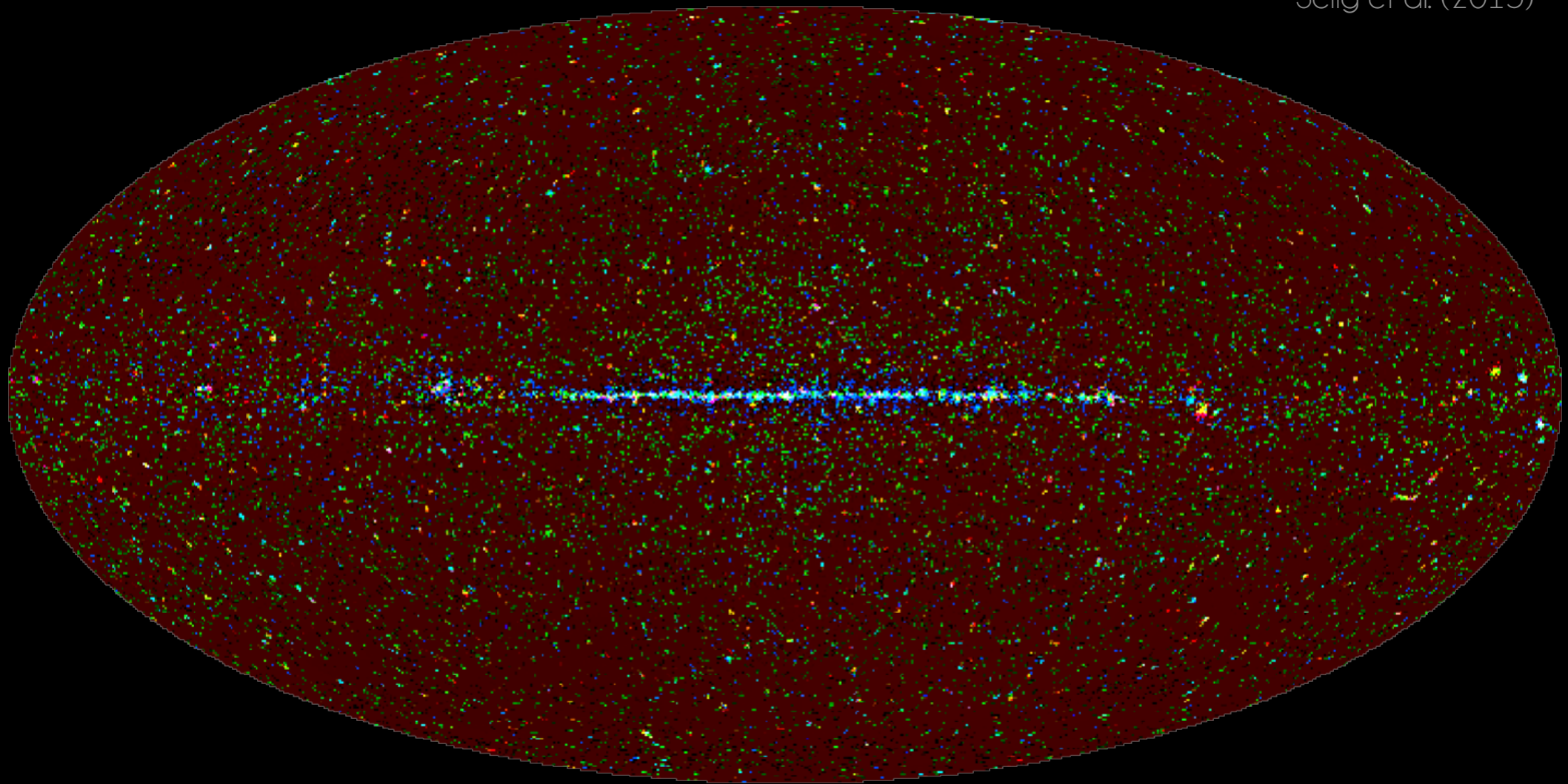
$$\begin{aligned}\mathcal{H}(\mathbf{d}, \mathbf{s}, \boldsymbol{\tau}) &= -\log \mathcal{P}(\mathbf{d}, \mathbf{s}, \boldsymbol{\tau}) \\ &= \mathbf{1}^\dagger [\log(d!) + \mathbf{R} (e^{\mathbf{s}} + e^{\mathbf{u}})] - \mathbf{d}^\dagger \log [\mathbf{R} (e^{\mathbf{s}} + e^{\mathbf{u}})] \\ &\quad + \frac{1}{2} \mathbf{s}^\dagger \mathbf{S}^{-1} \mathbf{s} + \frac{1}{2} \log (\det [\mathbf{S}]) \\ &\quad + (\boldsymbol{\alpha} - \mathbf{1})^\dagger \boldsymbol{\tau} + \mathbf{q}^\dagger e^{-\boldsymbol{\tau}} + \frac{1}{2} \boldsymbol{\tau}^\dagger \mathbf{T} \boldsymbol{\tau} \\ &\quad + (\boldsymbol{\beta} - \mathbf{1})^\dagger \mathbf{u} + \boldsymbol{\eta}^\dagger e^{-\mathbf{u}} \\ \mathbf{S} &= \sum_k e^{\tau_k} \mathbf{S}_k\end{aligned}$$



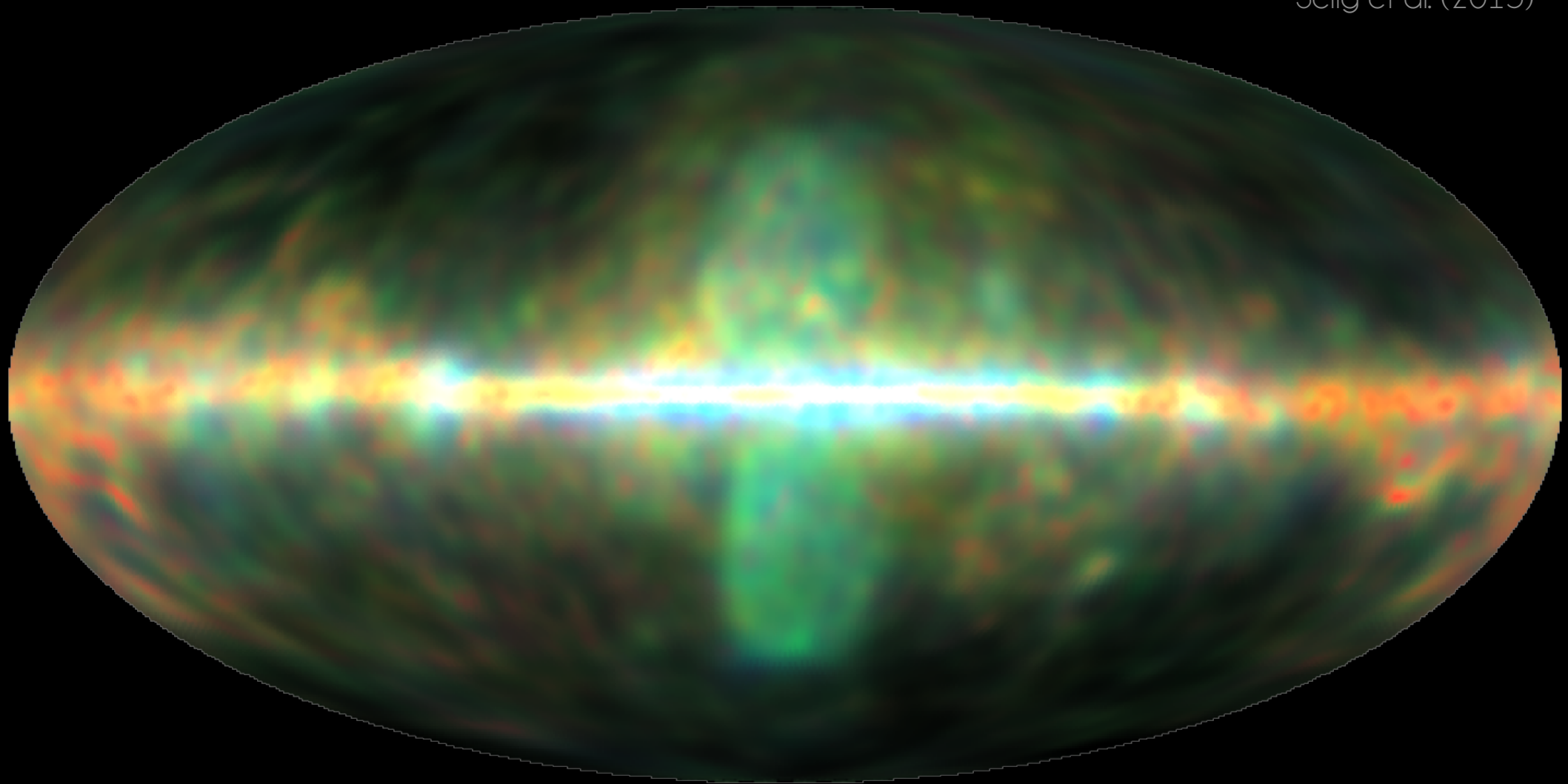


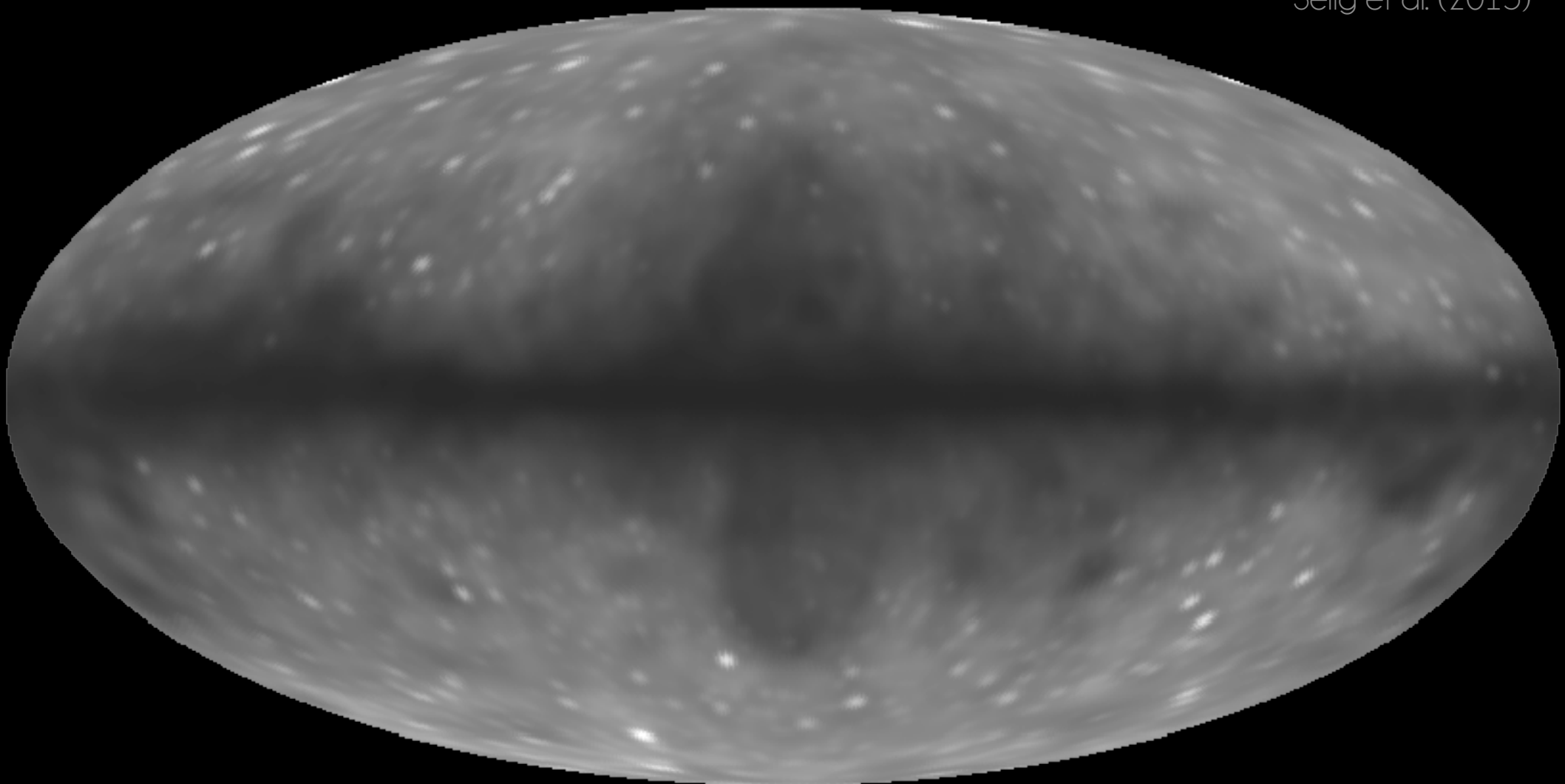


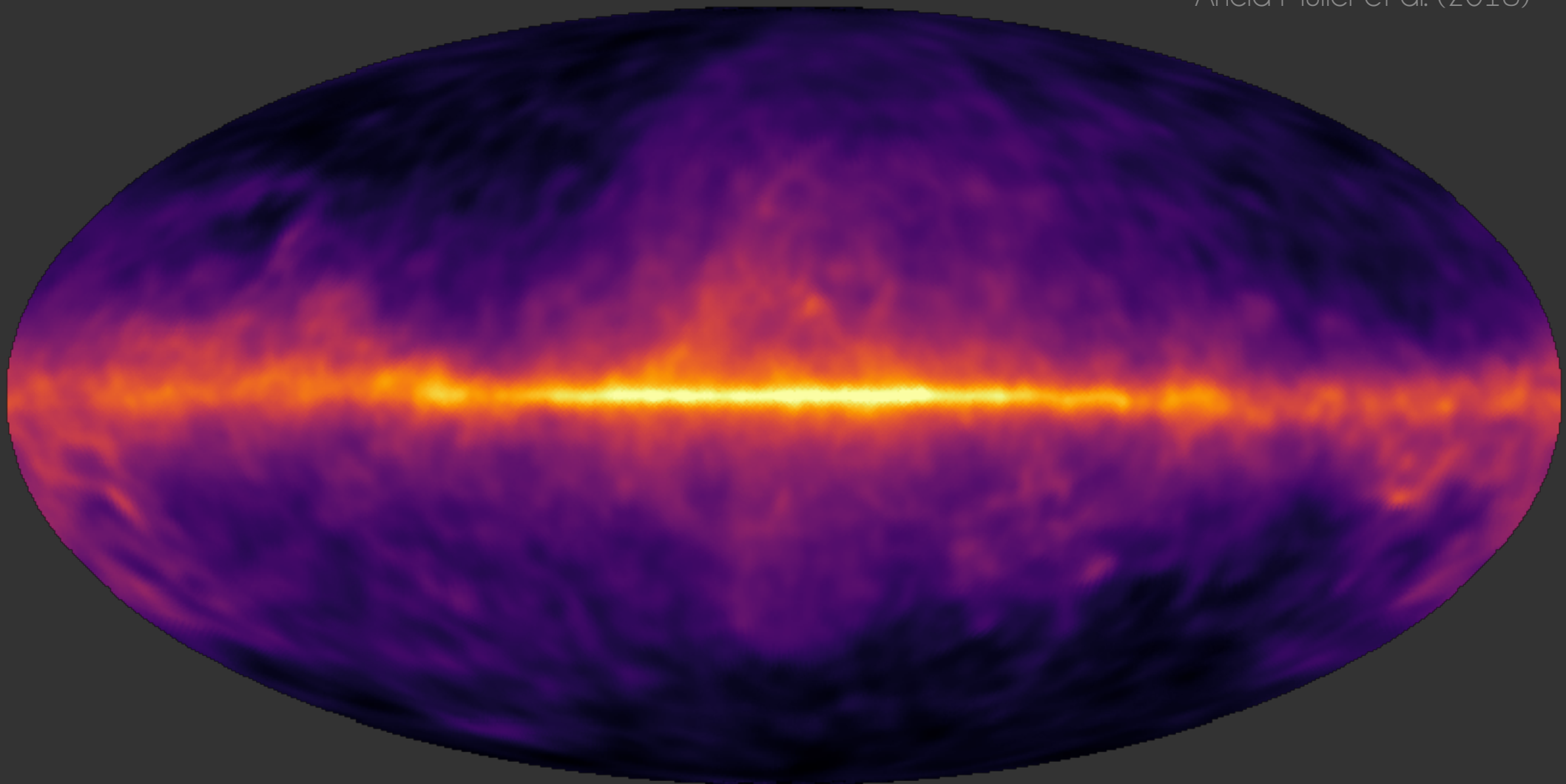


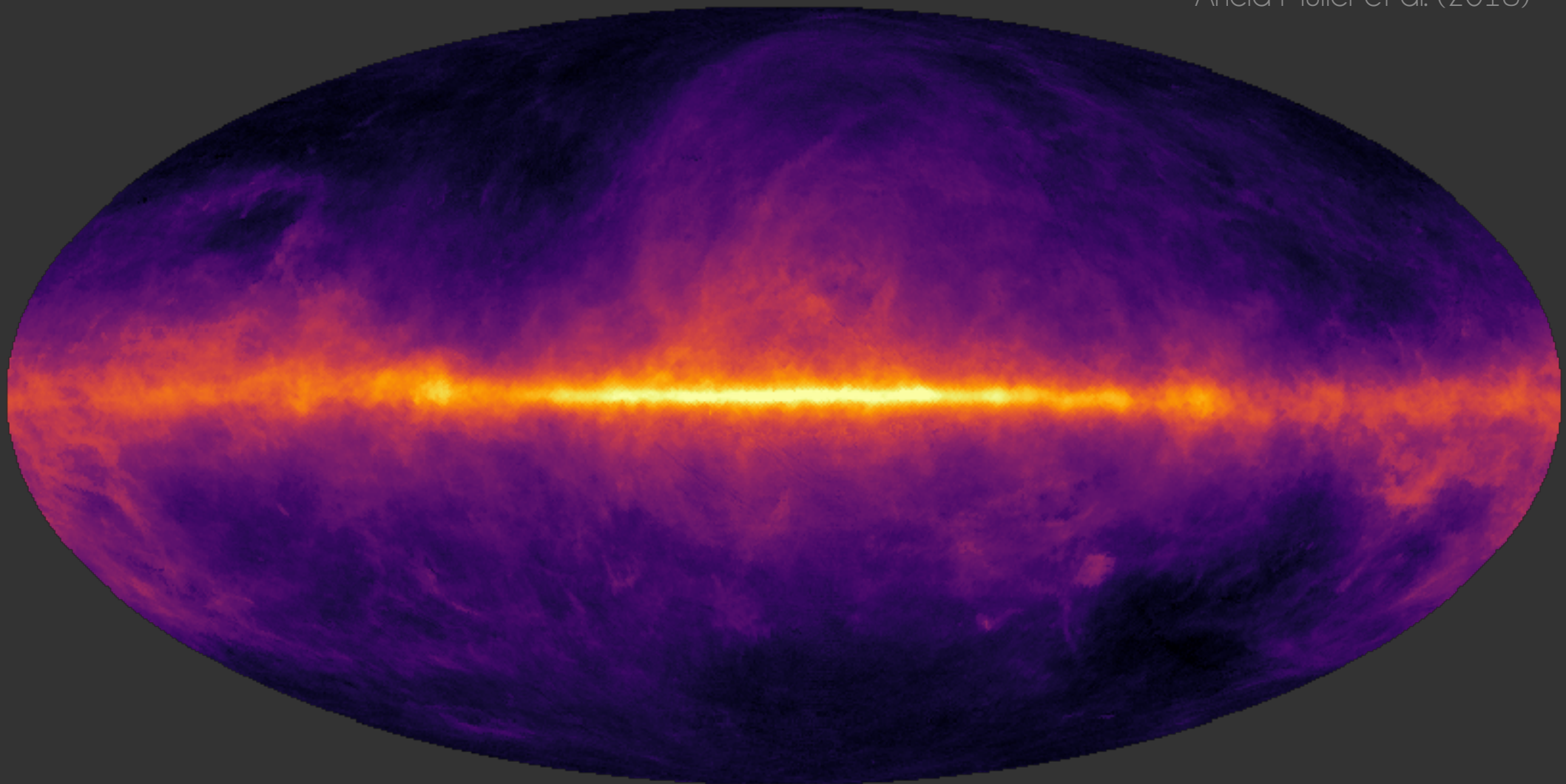




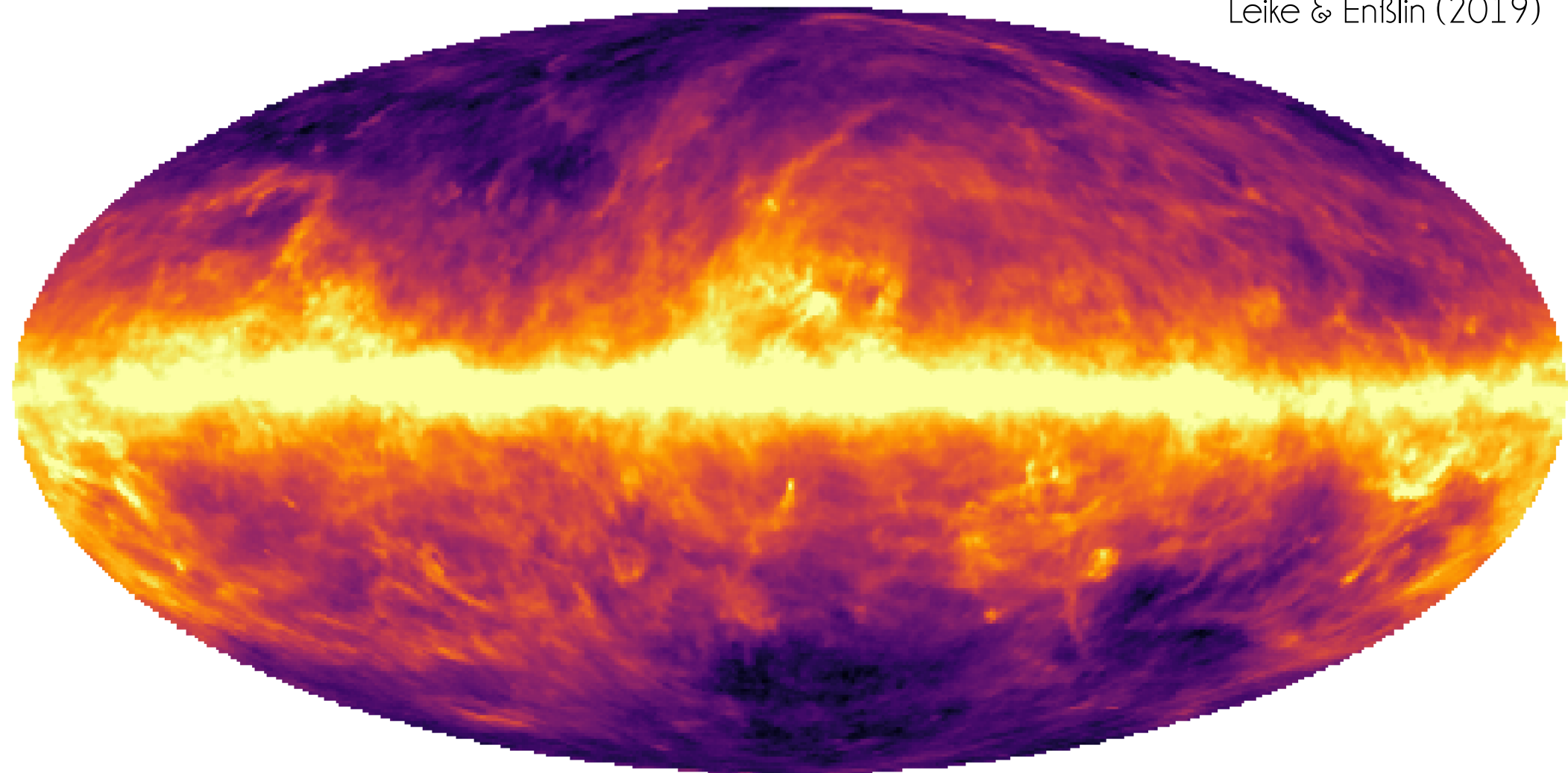




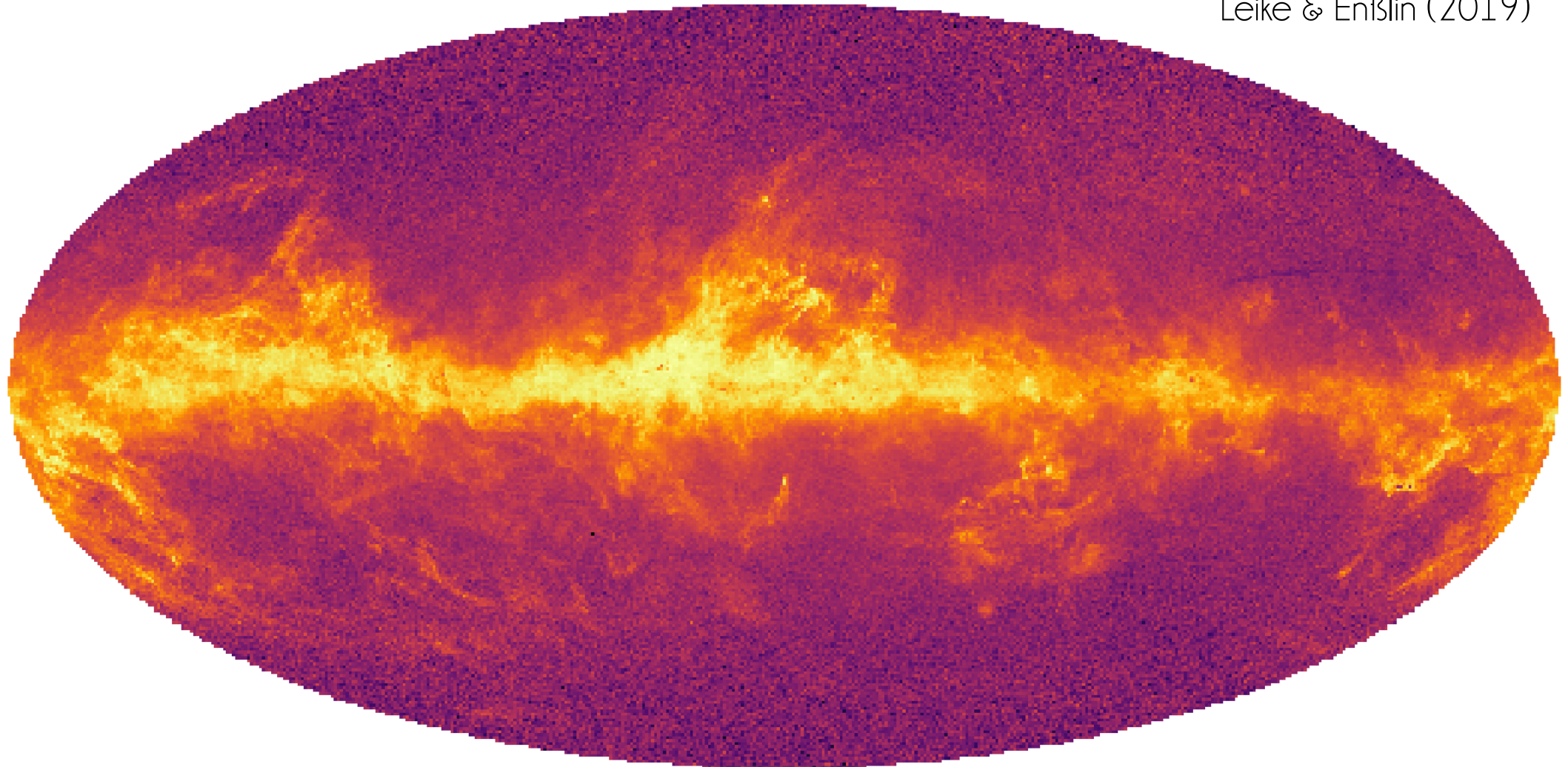




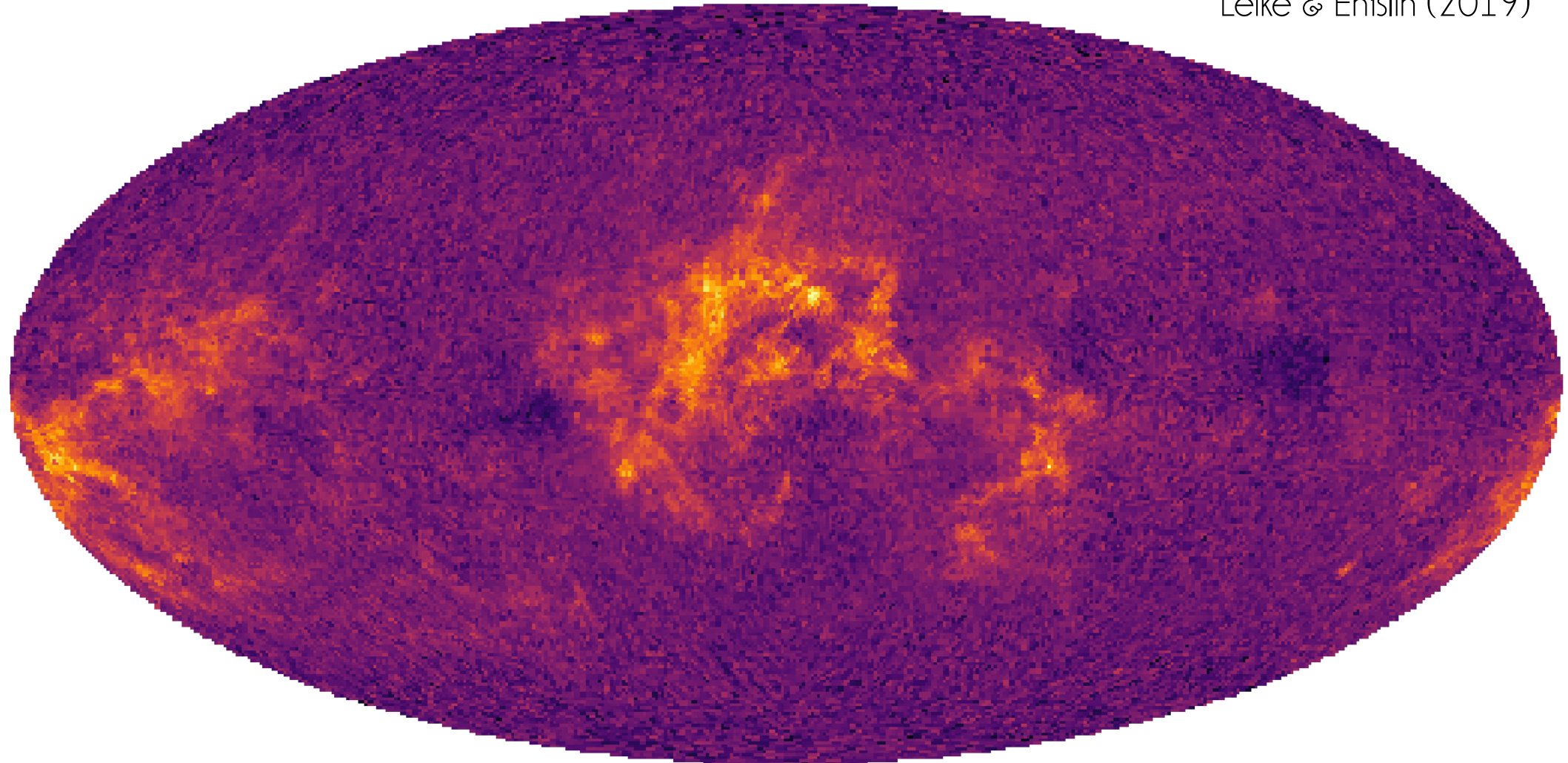
dust emission by Planck  
Leike & Enßlin (2019)



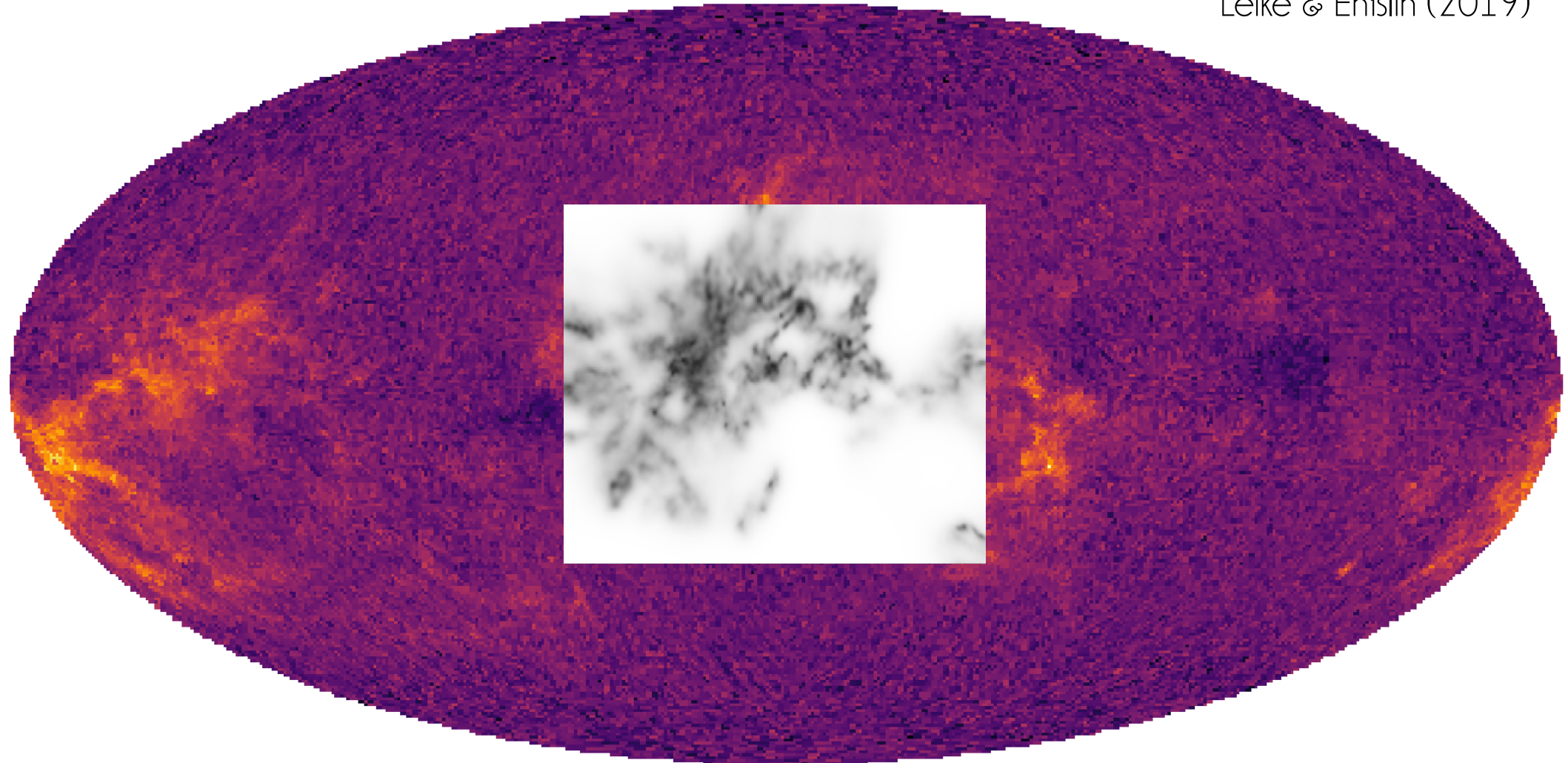
dust absorption by Gaia  
Leike & Enßlin (2019)



dust absorption by Gaia  
Leike & Enßlin (2019)

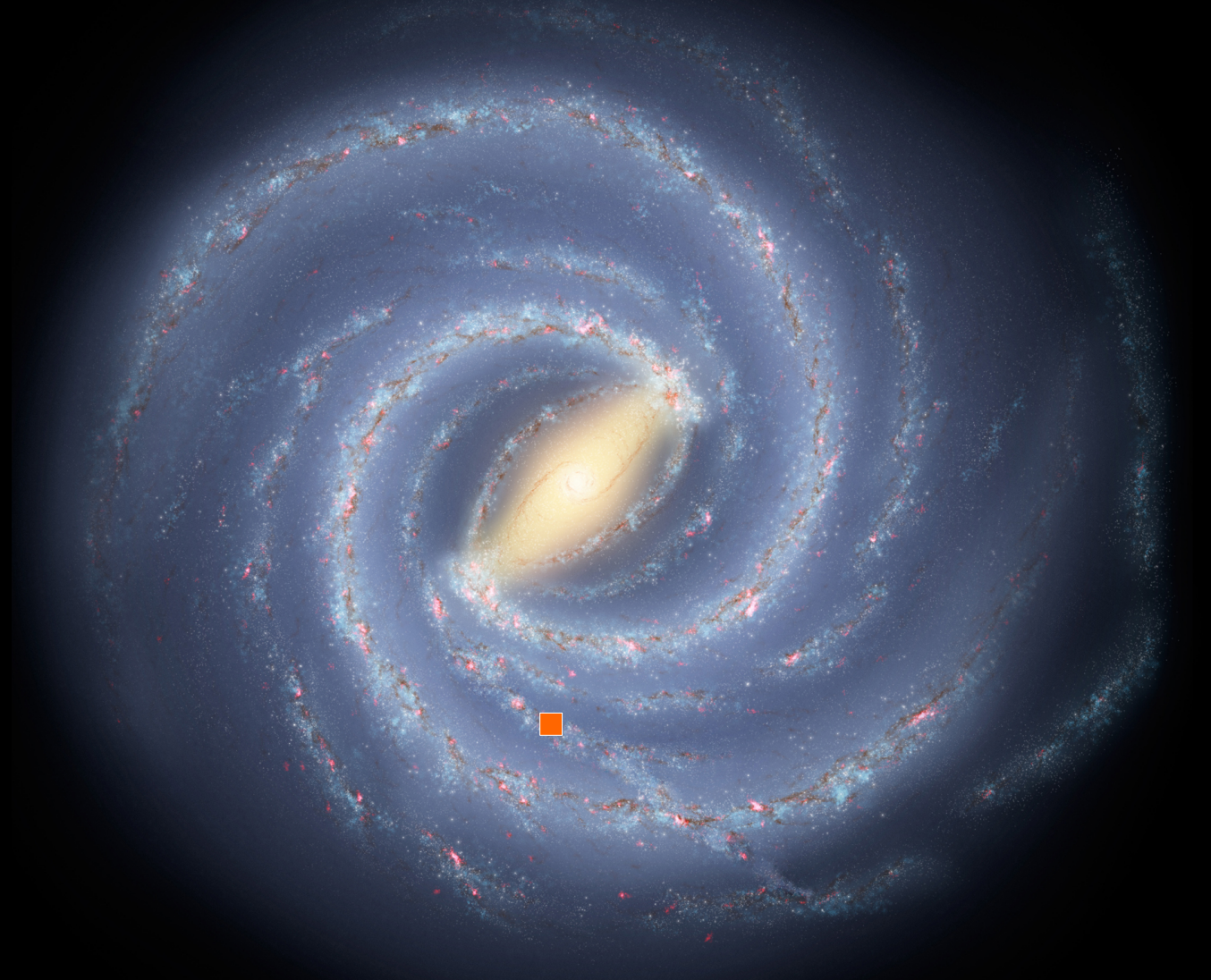


dust absorption by Gaia  
Leike & Enßlin (2019)

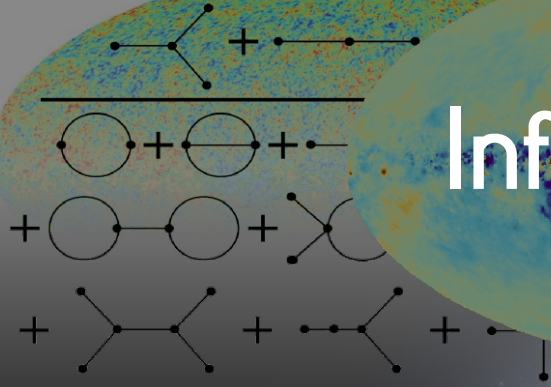








# Information field theory



## Field inference

IFT = information theory for fields

IFT is fully Bayesian

IFT exploits & learns signal correlations & other properties

IFT fuses machine learning & human knowledge

## NIFTy

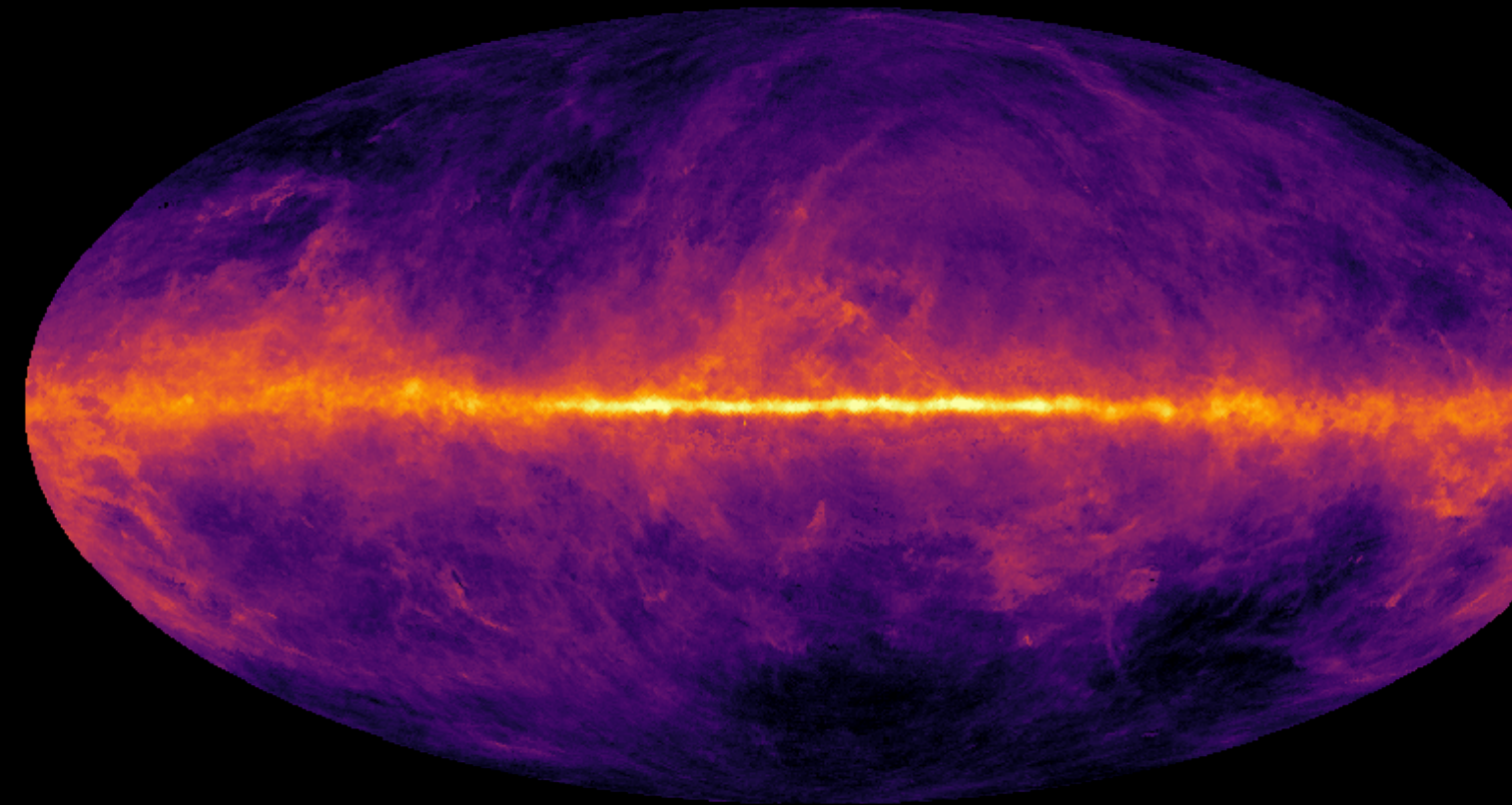
Numerical IFT

Reconstruction of signal fields over Cartesian and spherical spaces and products thereof

NIFTy algorithms are special purpose NN that do not require extra training

## Unified imaging UBIK





Thank you!