

# Low- and intermediate-mass star evolution: Open problems

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ImBaSE17  
Garching 3-7 July 2017

**ASTROPHYSICS  
RESEARCH INSTITUTE**



How accurately can we predict radii, effective temperatures, chemical stratification (hence surface abundances and evolutionary timescales) of low-intermediate-mass stars?

Convection

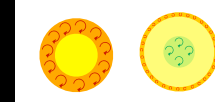
Thermohaline mixing

Element transport in radiative regions

Mass loss

# CONVECTION

- i) How extended is the mixing region beyond the formal convective border (convective boundary mixing -CBM)?



Instantaneous mixing in this region?

Diffusive mixing (following Freytag et al. 1996)?

$$\left. \frac{\partial X_i}{\partial t} \right|_{M_r} = \frac{1}{\rho r^2} \frac{\partial}{\partial r} \left( D_{\text{ov}} \rho r^2 \frac{\partial X_i}{\partial r} \right)$$

with

$$D_{\text{ov}} = D_c \exp\left(-\frac{2z}{fH_p}\right)$$

$$D_c = (1/3)\alpha_{MLT} v_c H_p$$

- ii) What is the temperature gradient in this CBM region?

Adiabatic (overshooting) or radiative (penetration)?

- iii) How do we reduce to zero the extension of the CBM region when convective core masses approach zero?

- iv) What is the temperature gradient in surface convective regions?

**Choices made affect evolutionary times (star counts), luminosities,  $T_{\text{eff}}$ , loops in the Colour-Magnitude-Diagrams, predicted populations of variable stars in stellar populations, chemical profiles, asteroseismic properties.**

# Helium burning core mixing

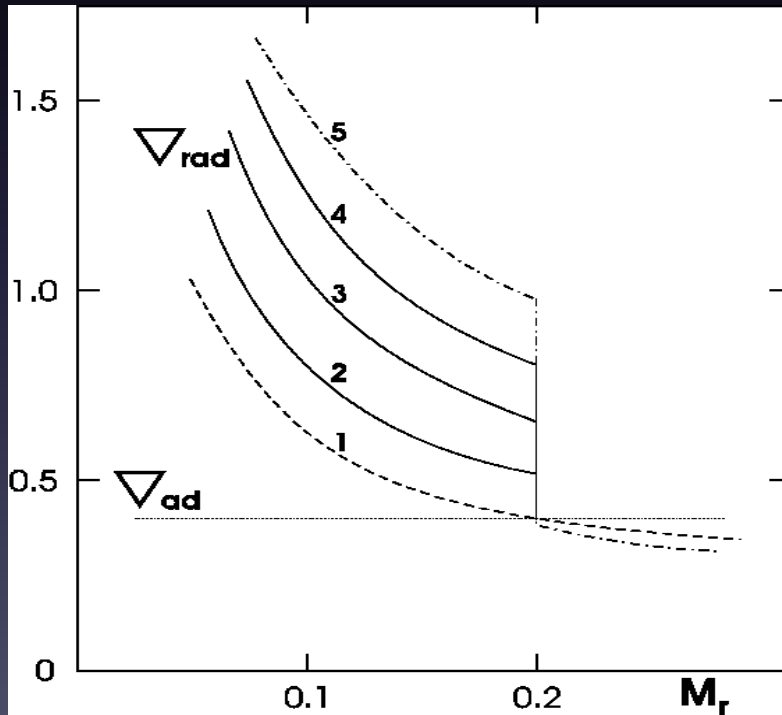
## Core Expansion

C produced by He-burning

Opacity increases

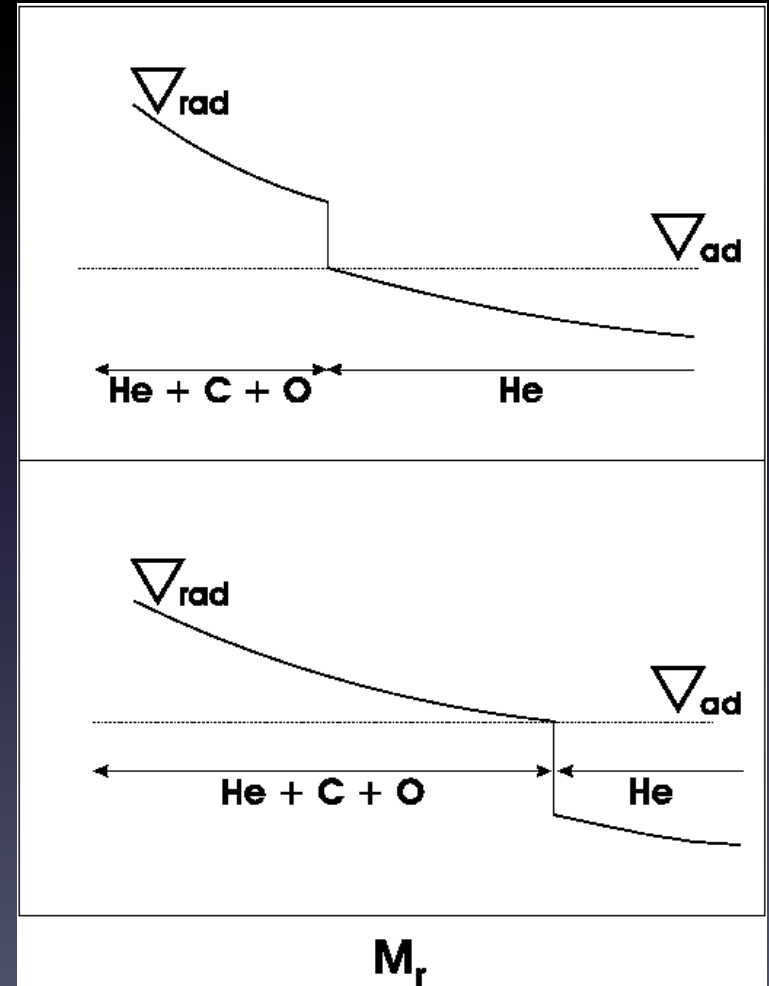
$$F_c \approx \nabla_{\text{rad}} - \nabla_{\text{ad}}$$

Radiative gradient discontinuity at the convective core boundary



See, e.g. Castellani et al. (1971), Gabriel et al. (2015)

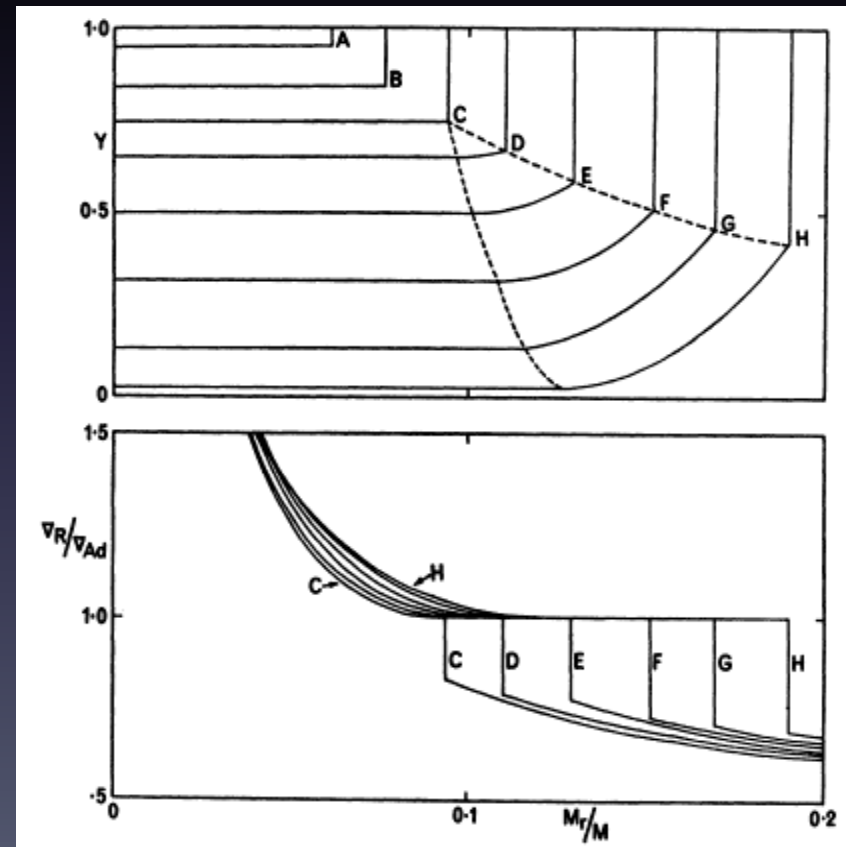
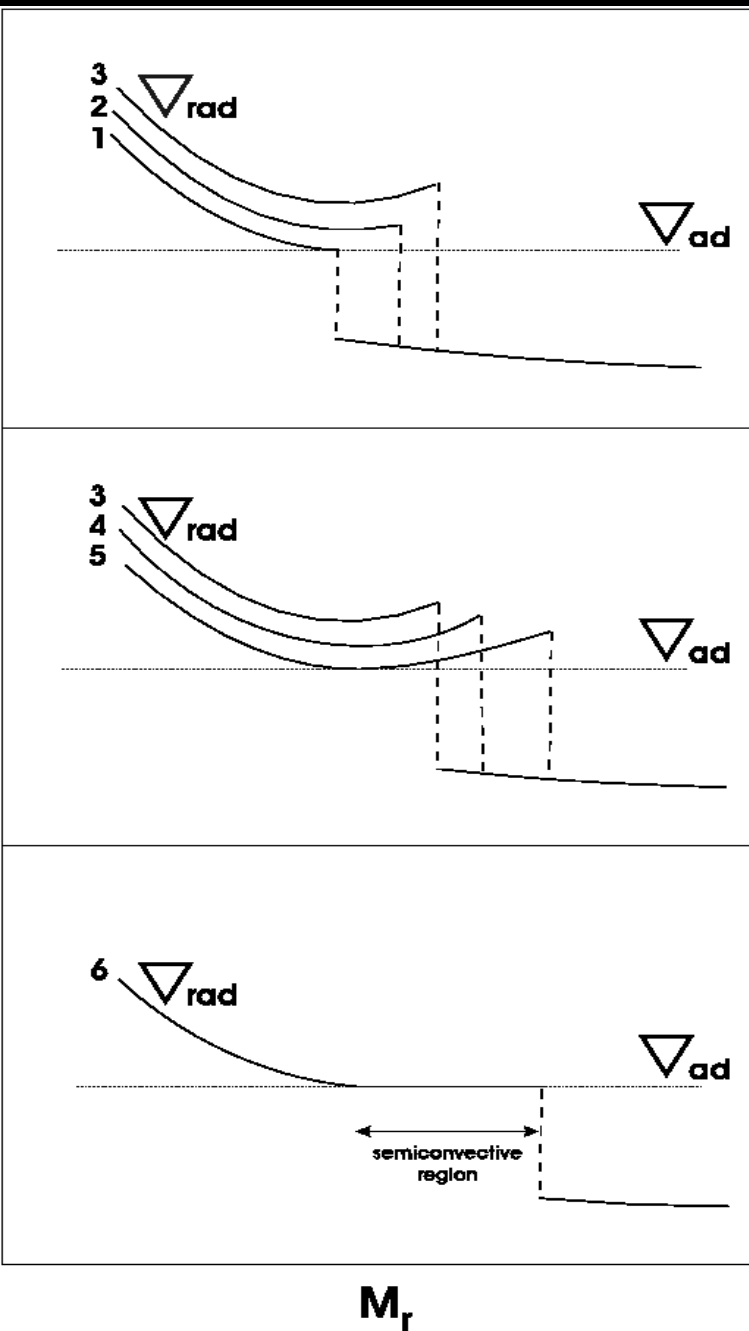
Mass of fully mixed core increases



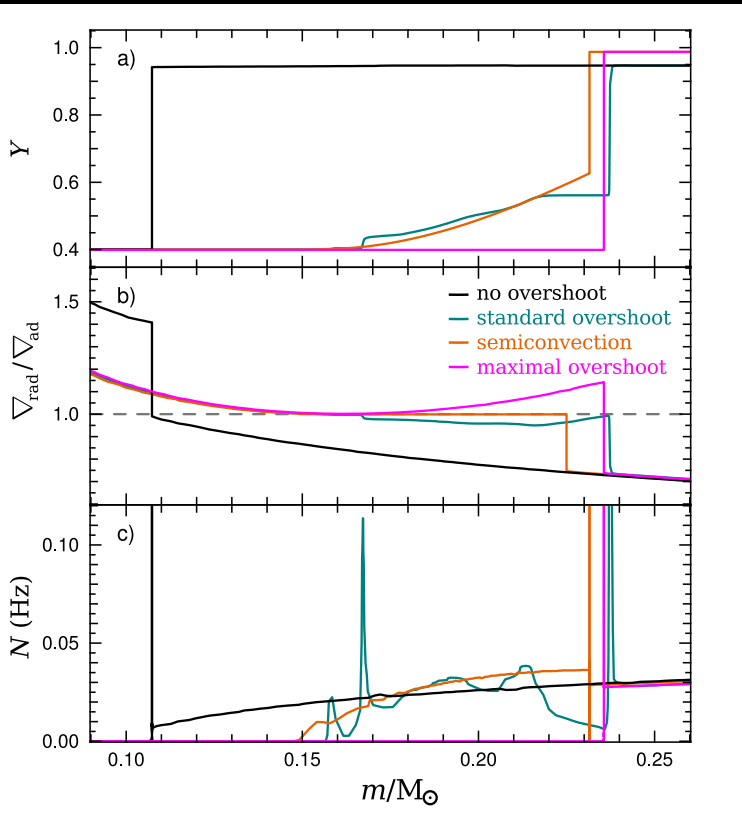
What happens now?

When  $Y_c$  decreases below  $\sim 0.7$ , a 'partial mixing' may be invoked beyond the boundary of the convective core (called semiconvection).

But other options do exist



# 1 M<sub>⊙</sub> solar initial composition

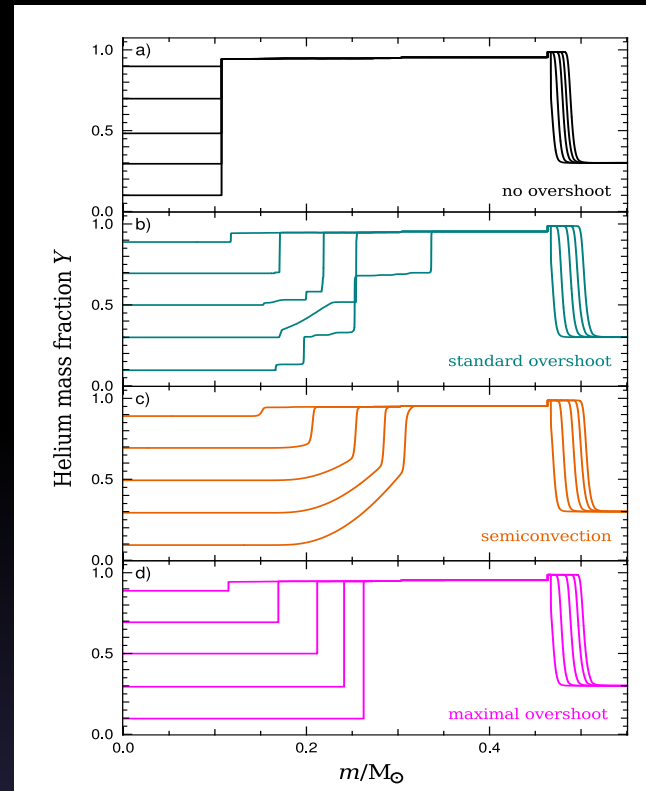


$$N^2 \approx \frac{g^2 \rho}{p} (\nabla_{ad} - \nabla + \nabla_{\mu})$$

$Y_c = 0.4$

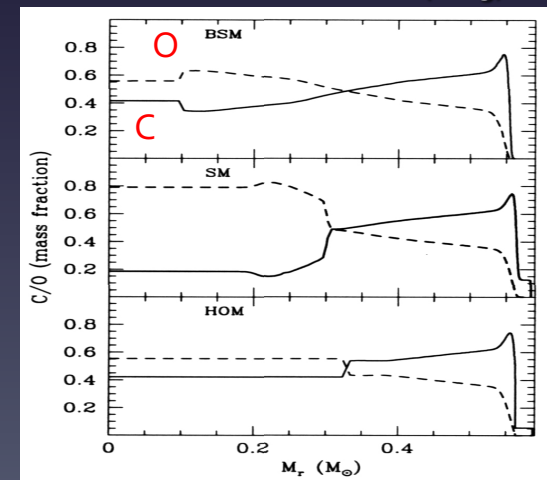
Gravity mode period spacing (same  $l$  and consecutive  $n$ ) from *Kepler* stars favours the maximal overshoot scenario

Studies also by Bossini et al. (2015, 2017)



Constantino et al. (2015)

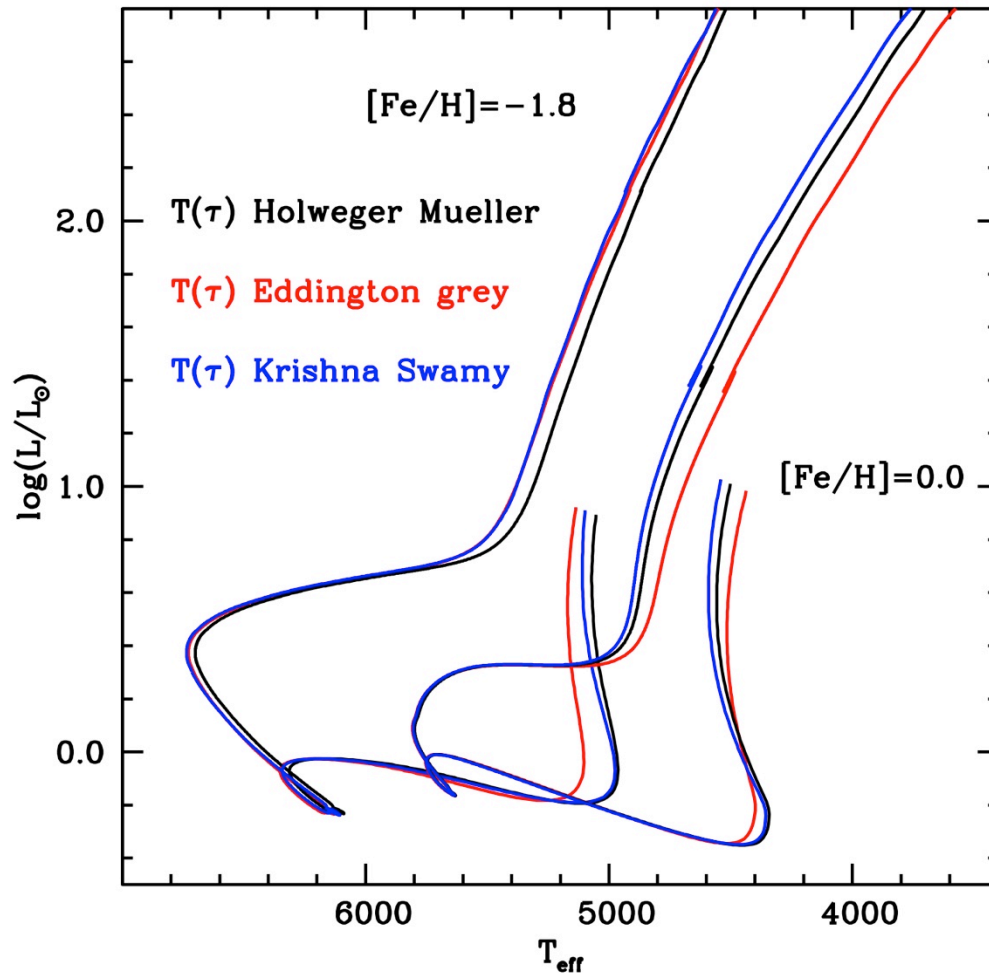
Straniero et al. (2003)



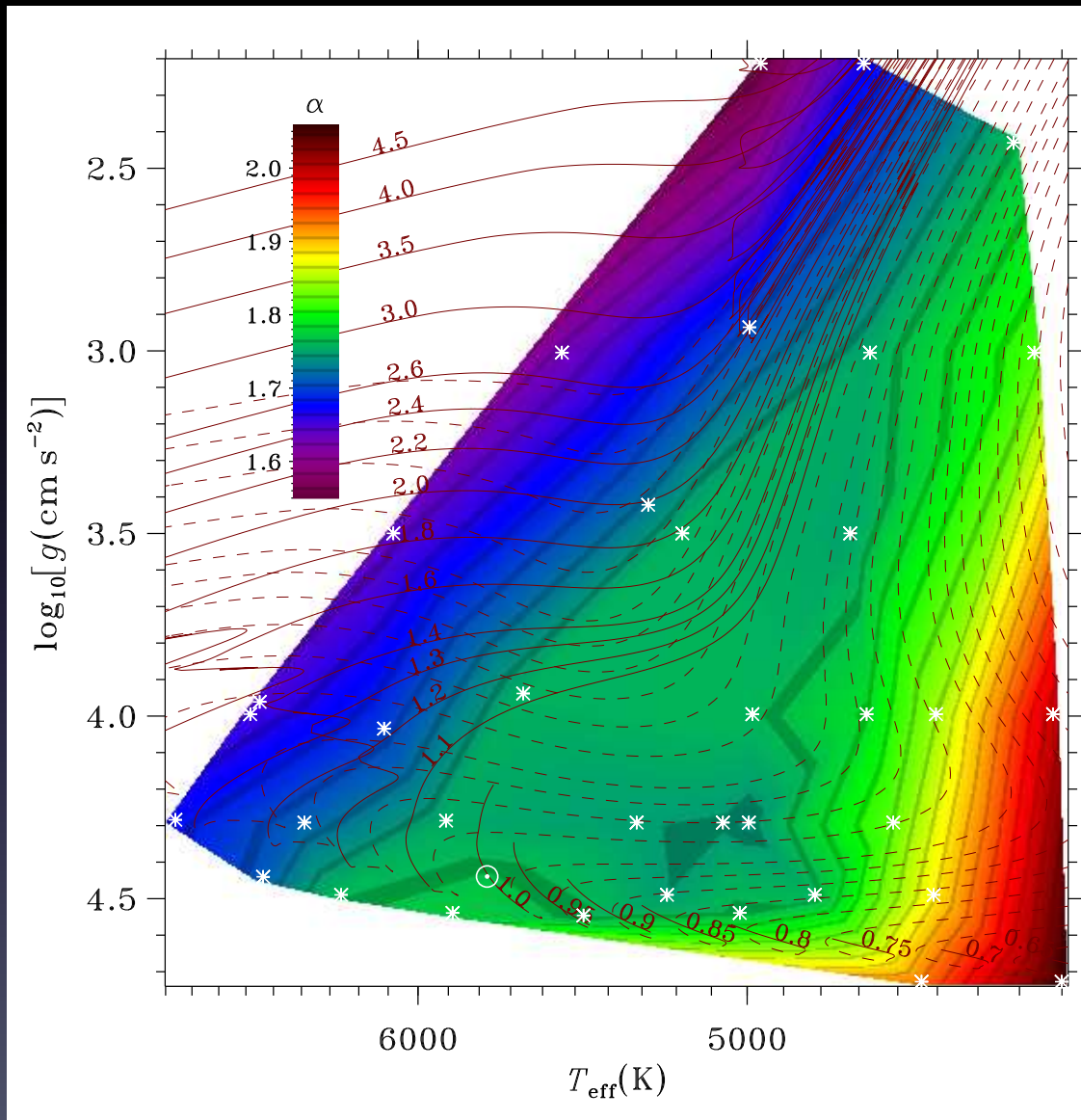
Different mixing schemes, different C/O stratifications

## Superadiabatic gradient : MIXING LENGTH THEORY

$T_{\text{eff}}$  mismatches/trends between theory and observations might have nothing to do with a variation of the mixing length  $\alpha_{\text{MLT}}$



3D radiation hydrodynamics simulations predict a variable mixing length  $\alpha_{\text{MLT}}$



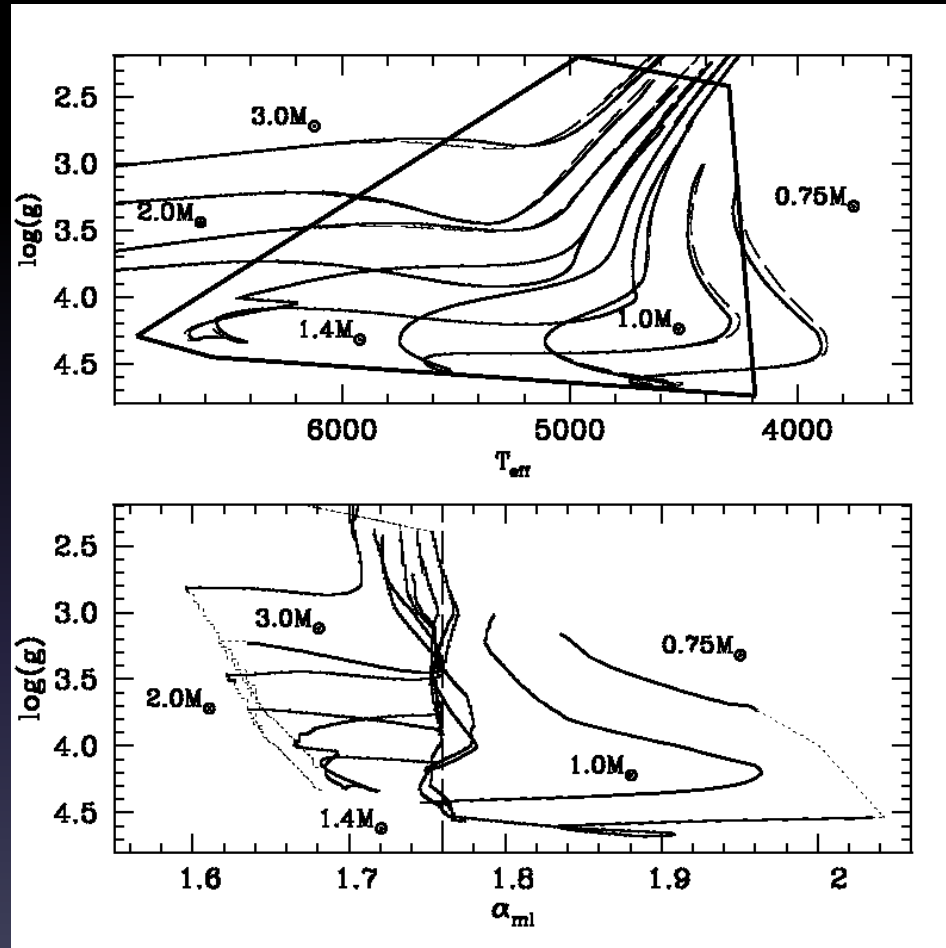
Trampedach  
et al. (2014)



Are stellar models  
very affected by  
the variation of  
 $\alpha_{\text{MLT}}$ ?

3D radiation  
hydrodynamics  
calibration  
(mixing length  
and boundary  
conditions) by  
Trampedach et al.  
(2014)

Solar metallicity  
only  
At most just 30-50  
K difference  
between solar  
and variable  $\alpha$   
calibration

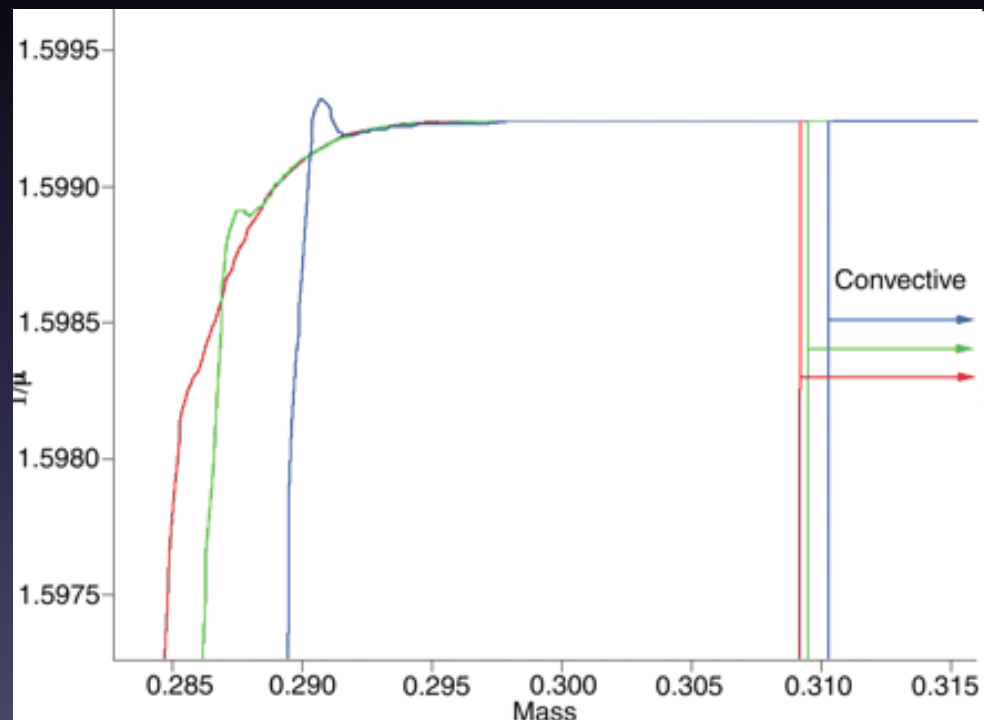


# THERMOHALINE MIXING

*“The H-burning front moves outward into the stable region, but preceding the H-burning region proper is a narrow region, usually thought unimportant, in which  $^3\text{He}$  burns.*

*The main reaction is  $^3\text{He} (^3\text{He}, 2p)^4\text{He}$ : two nuclei become three nuclei, and the mean mass per nucleus decreases from 3 to 2. Because the molecular weight ( $\mu$ ) is the mean mass per nucleus, but including also the much larger abundances of H and  $^4\text{He}$  that are already there and not taking part in this reaction, this leads to a small inversion in the  $\mu$  gradient. “*

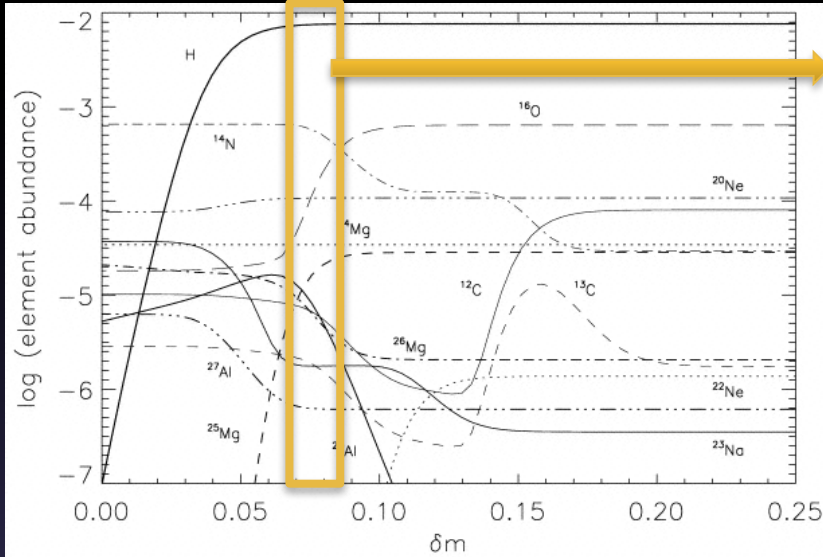
$1M_{\odot}$  solar  
composition



Eggleton et al. (2006)

# RGB extra-mixing after first dredge up

0.8 M<sub>⊙</sub> metal poor RGB model



Salaris et al. (2002)

Bottom conv. envelope at  $\delta m = 1$   
 Bottom H-burning shell at  $\delta m = 0$

0.8 M<sub>⊙</sub> [Fe/H] = -1.58

$$D_{th} = C_{th} \frac{K}{c_p \rho} \left( \frac{\phi}{\delta} \right) \frac{\nabla_{\mu}}{(\nabla_{rad} - \nabla_{ad})}$$

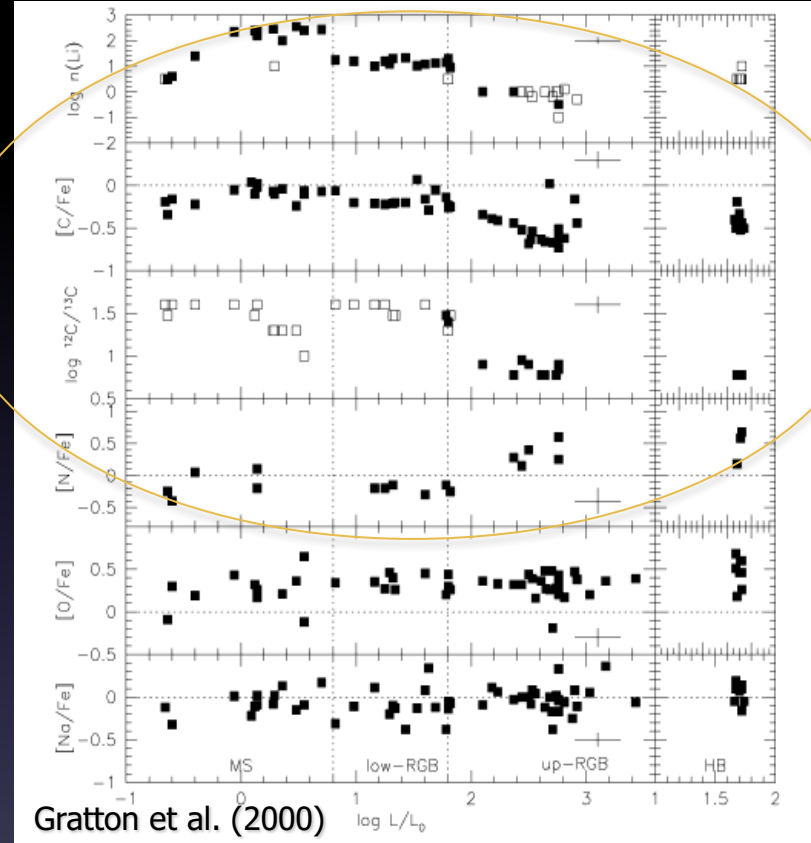
$$C_{th} = (8/3)\pi^2 \alpha^2$$

with  $\alpha$  free parameter  
 (Charbonnel & Zahn 2007)

Field halo stars

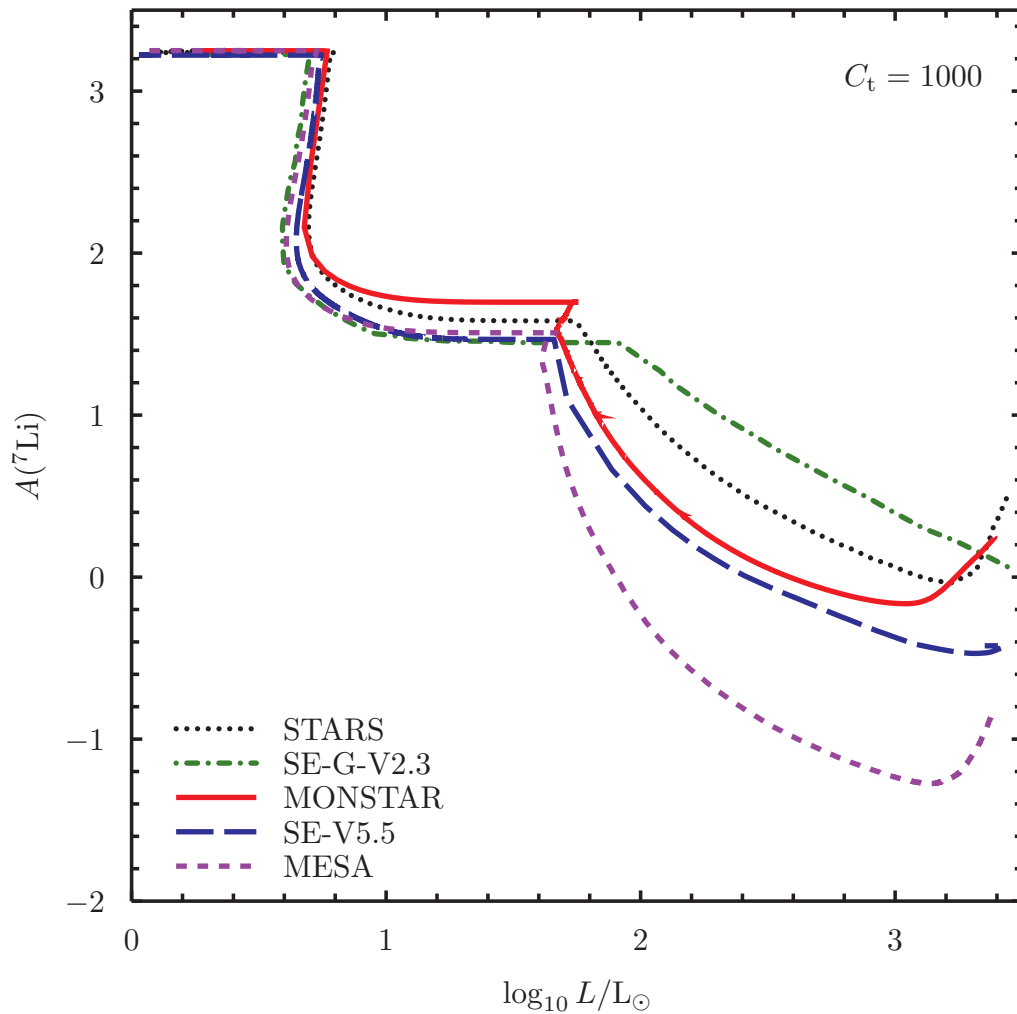


1<sup>st</sup> dredge up



Gratton et al. (2000)

## 1.25 $M_{\odot}$ solar initial composition

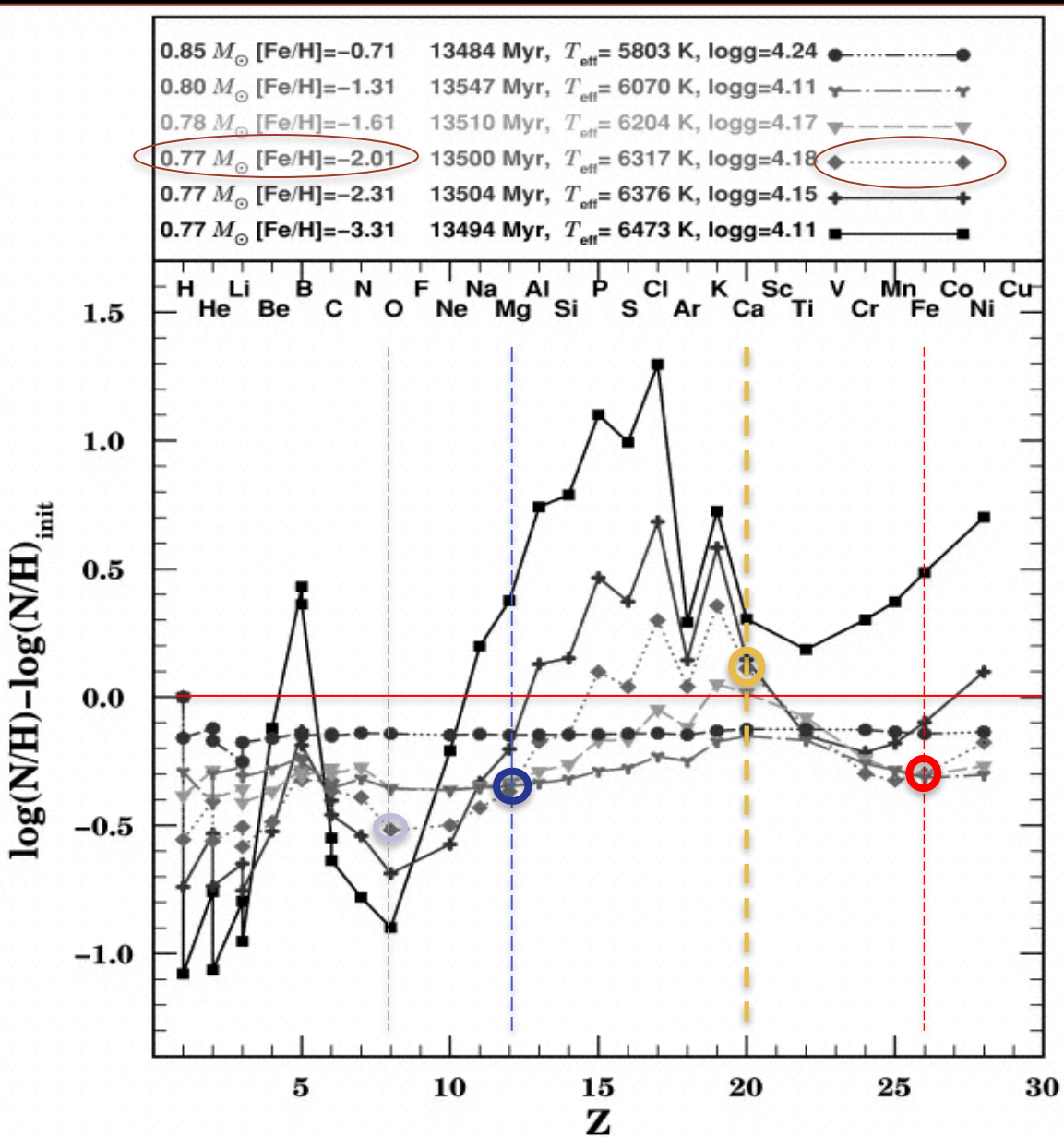


Surface abundances for a given  $C_t$  are very sensitive to timestep and mesh resolution adopted in the stellar model calculations

Also, hydro-simulations of this process do not give definitive results, even though they hint that  $C_t < 1000$

# Atomic diffusion on the Main Sequence

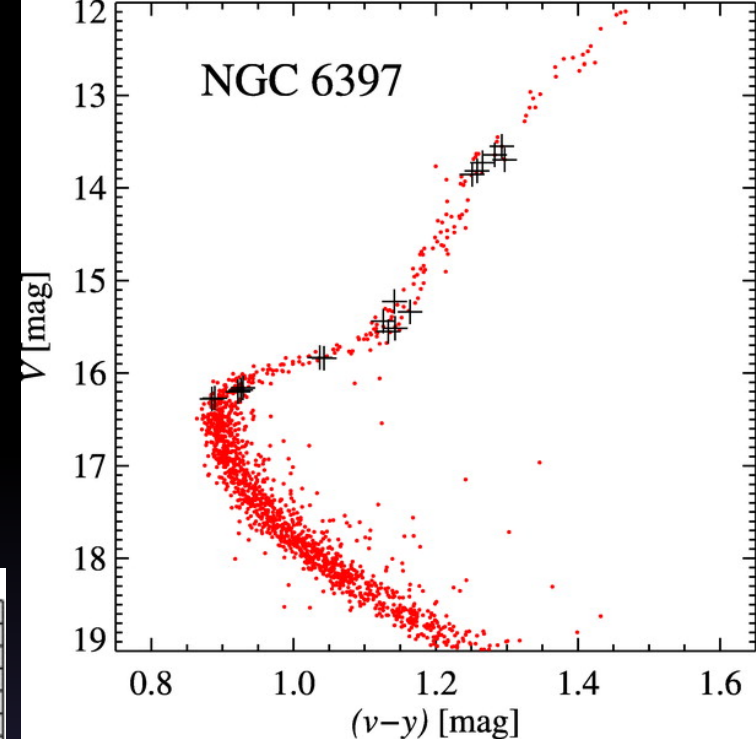
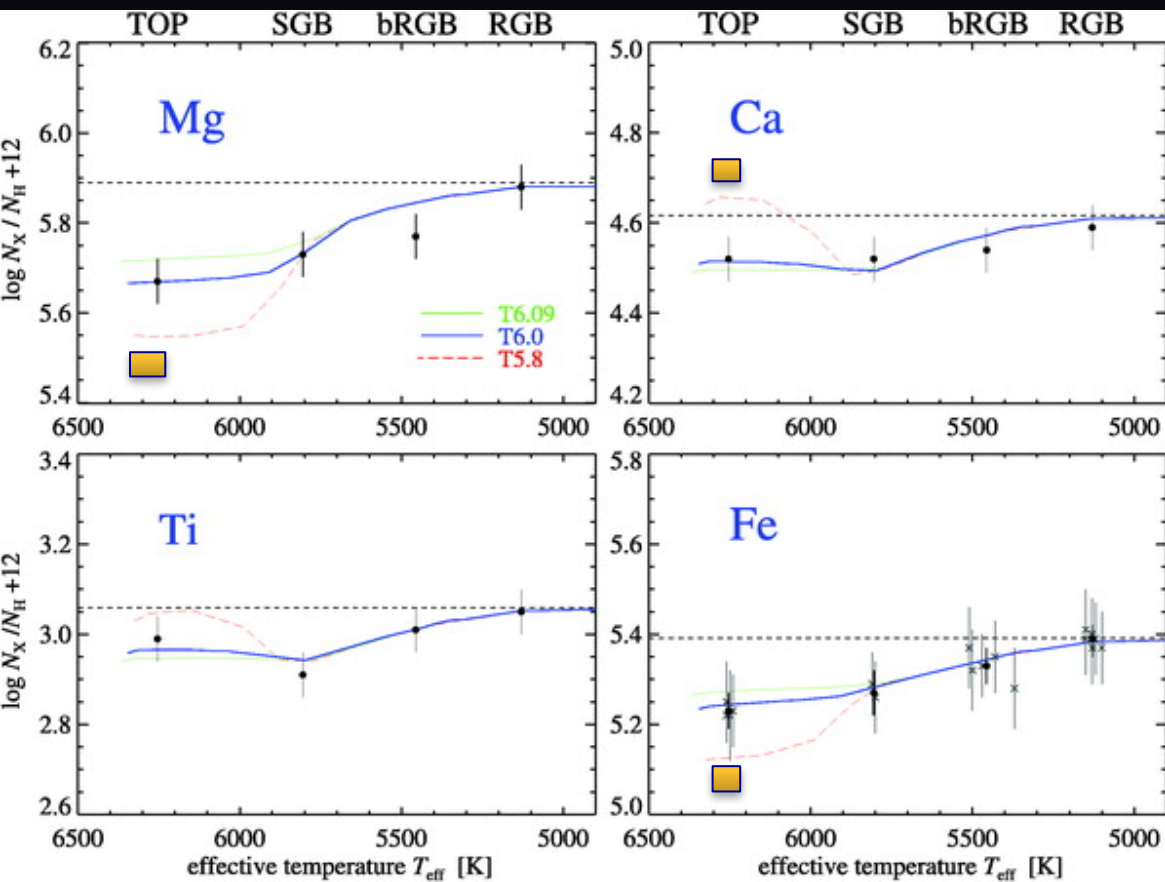
Treatment from first principles



Richard et al. (2002)

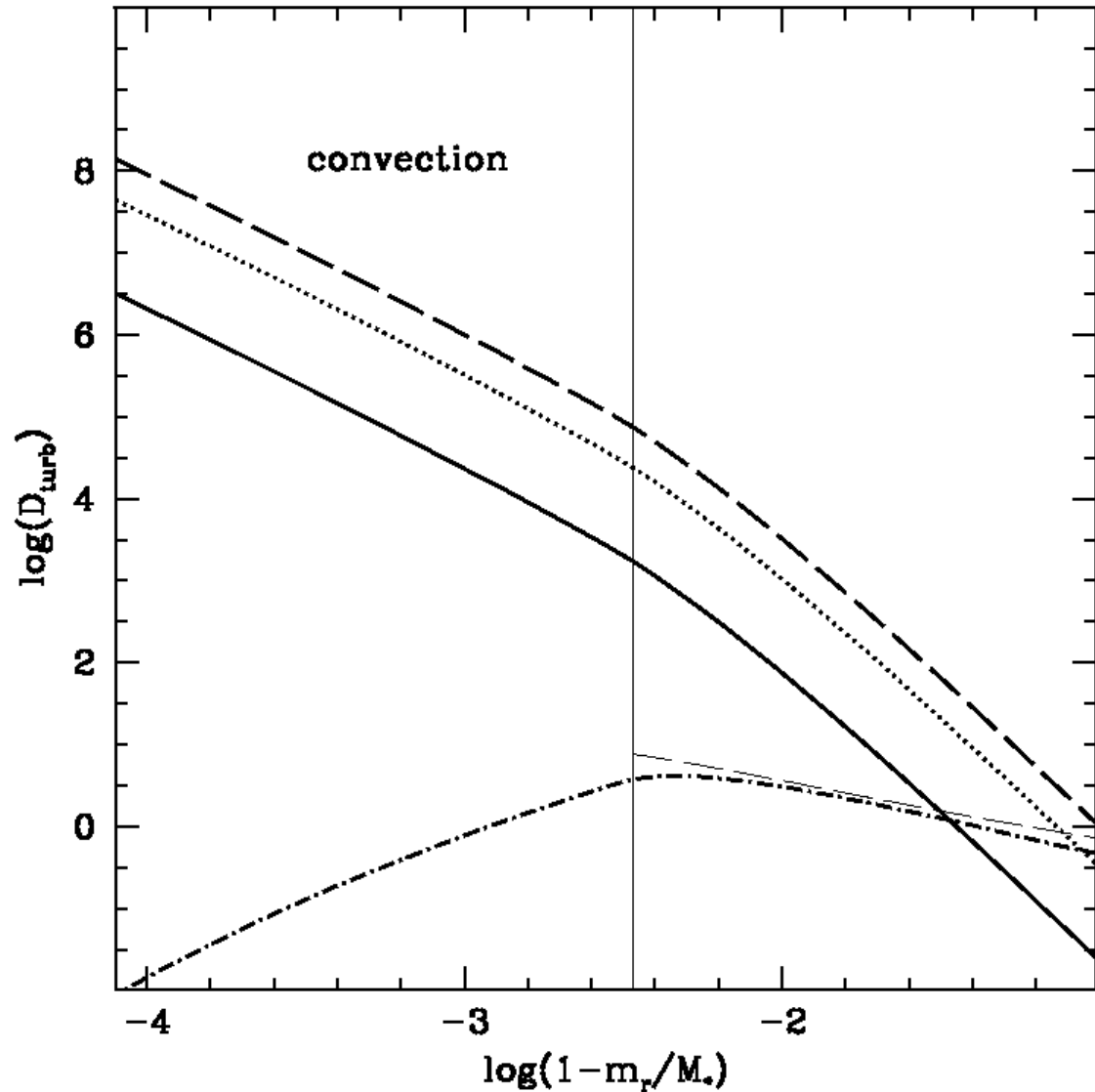
# Puzzling observations

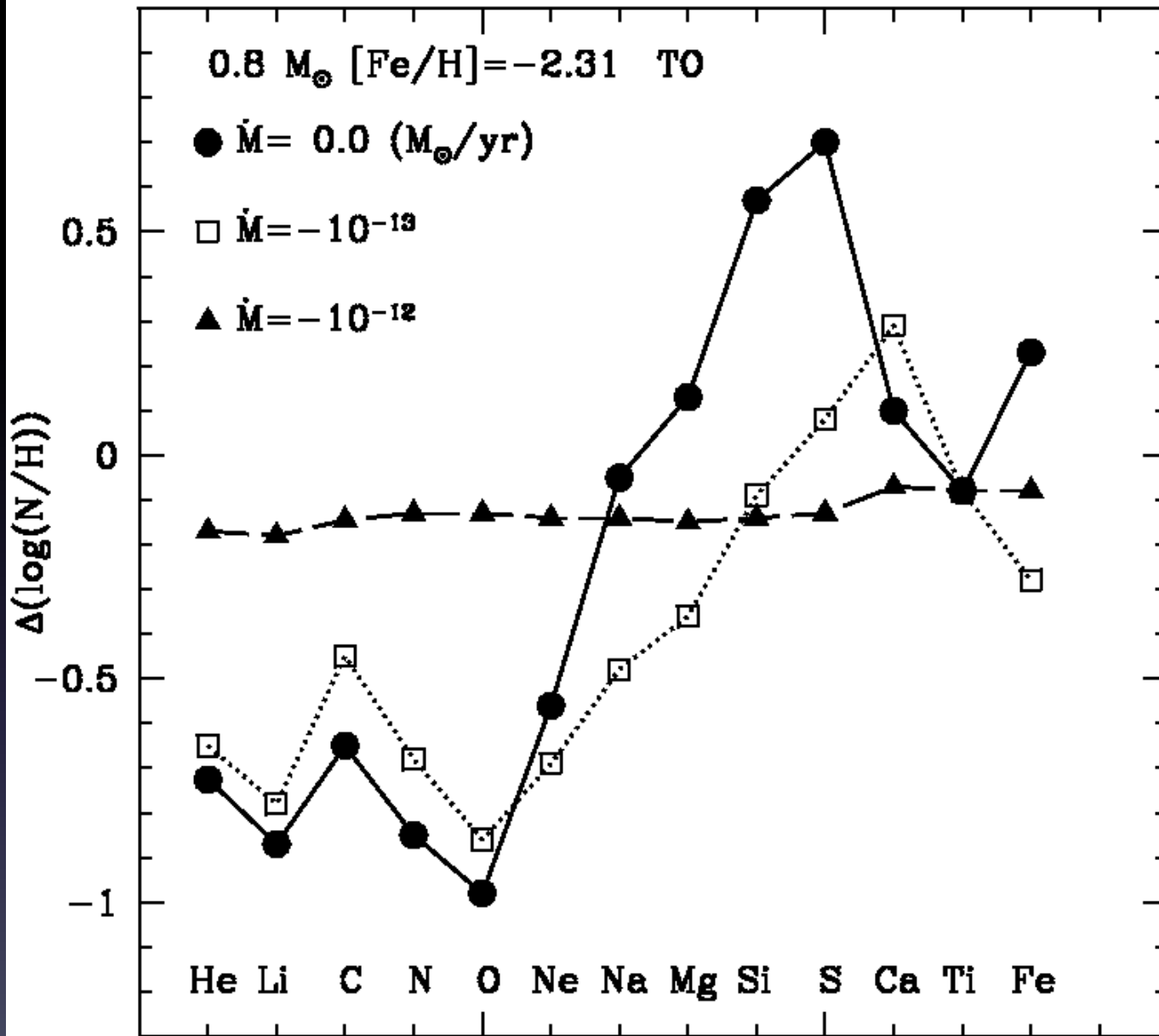
Korn et al. (2007)



Inhibition of diffusion from/into the convective envelopes with *ad-hoc* counteracting diffusive mixing (called generically *turbulence*)

0.8 $M_{\odot}$ , [Fe/H]=-1.3 model, in the latter phase of its MS evolution. The vertical thin line marks the bottom of the convective envelope





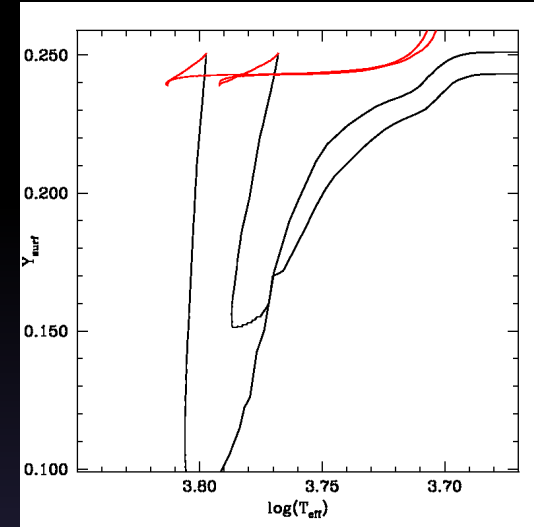
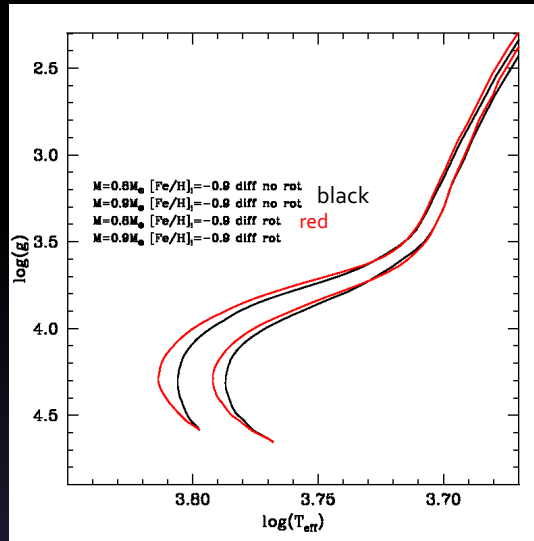
Effect of  
mass  
loss

Data from Vick et al. (2013)

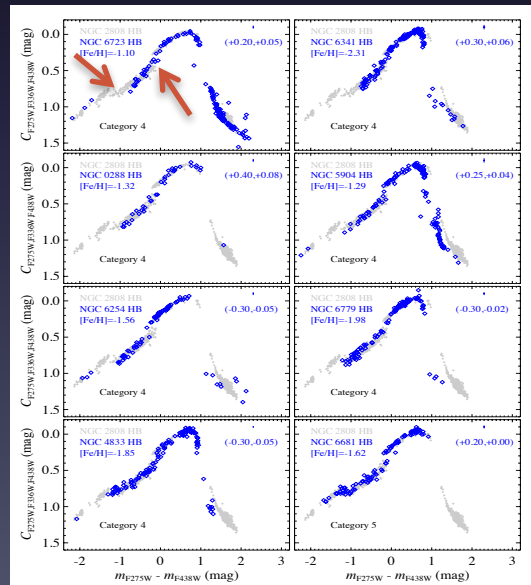


Rotation inhibits atomic diffusion from surface and also increases evolutionary timescales (rotational mixing counteracts the development of chemical gradients)

Georgy et al. (2013)



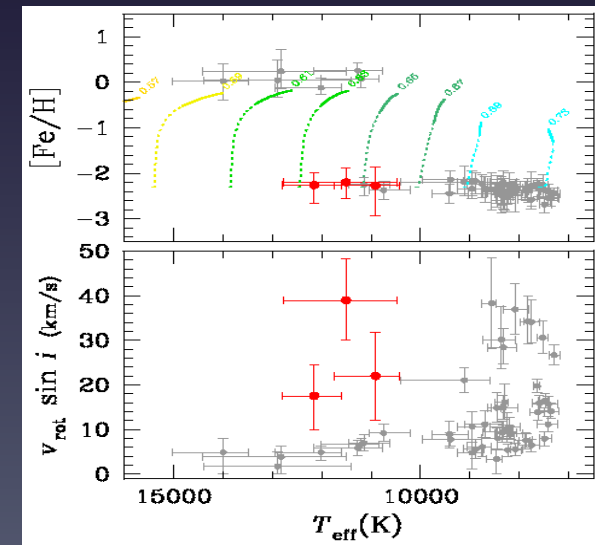
Brown et al. (2016)



Atomic diffusion in HB stars

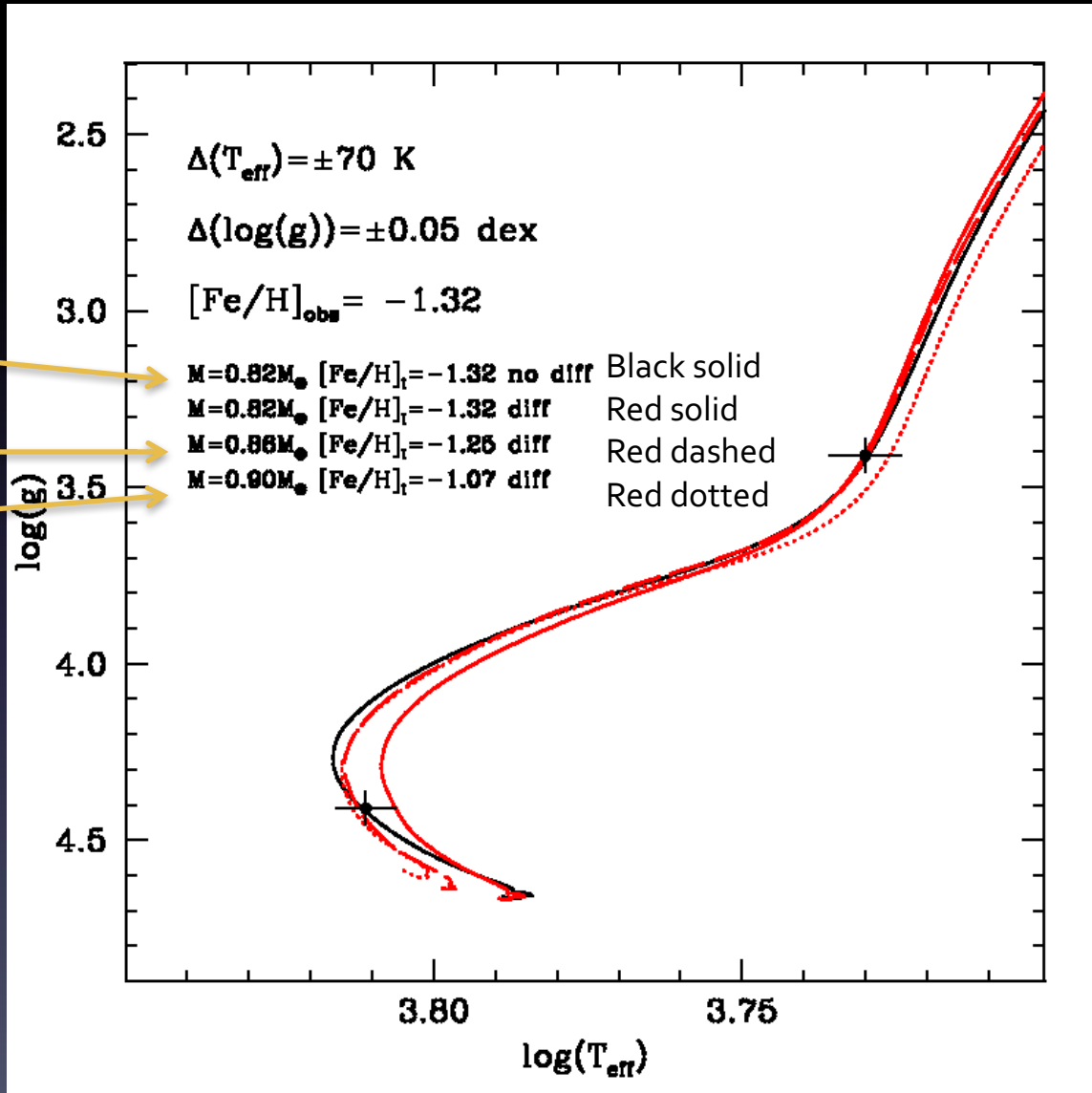
M<sub>15</sub>, M<sub>68</sub>, M<sub>92</sub>

Michaud et al. (2011)



Also problem matching Abundances of sdB stars (Hu et al. 2011)

# EFFICIENCY OF ATOMIC DIFFUSION AND AGE OF FIELD STARS



MS

$\cong 8.5 \text{ Gyr}$

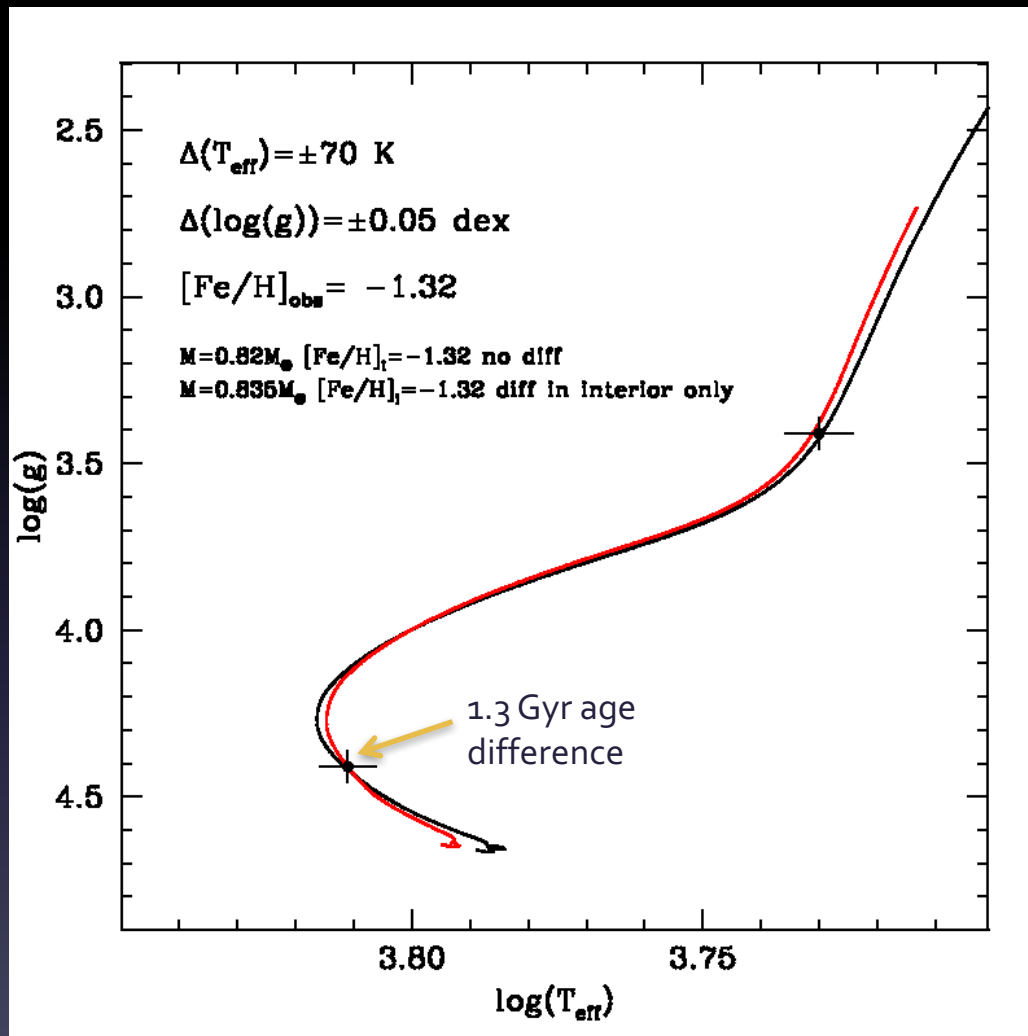
$\cong 6 \text{ Gyr}$

$\cong 5 \text{ Gyr}$

Large age uncertainty if we do not know the stellar mass

# Zero-order test with atomic diffusion inhibited from envelopes

Spectroscopy of GCs tells us that gravitational settling-levitation are strongly inhibited (at least) for the convective envelope

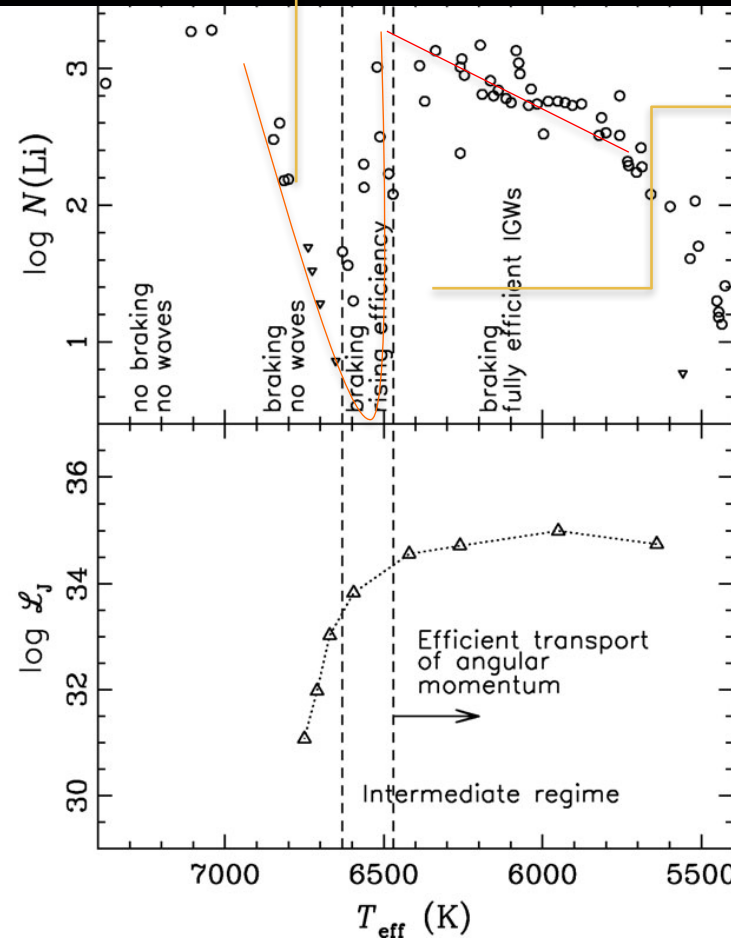
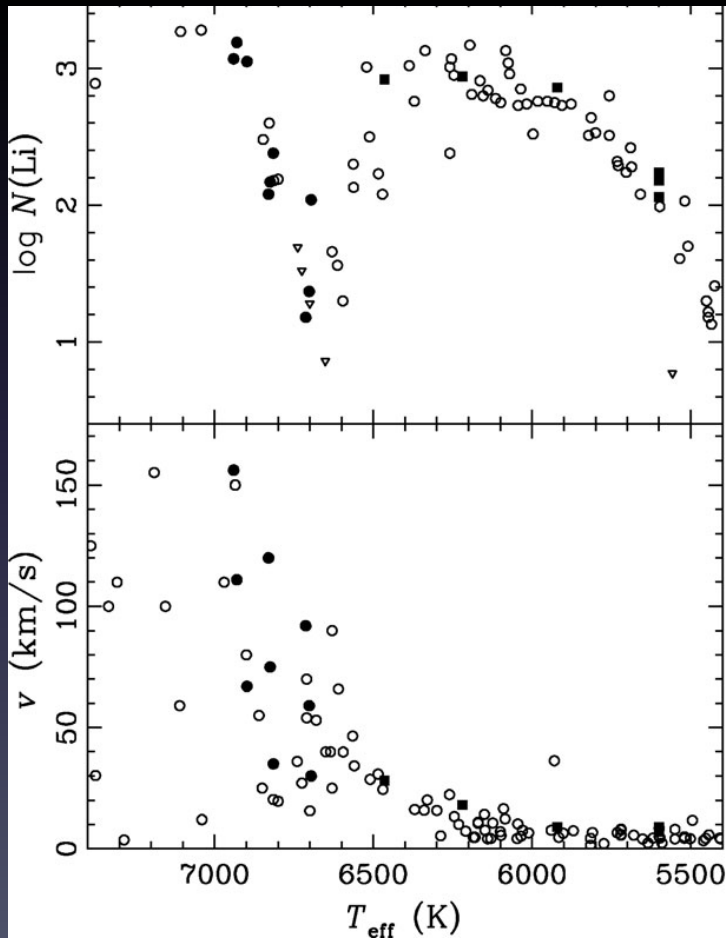


# Diffusion and more in open clusters. An example

Hyades (Turn off mass  $\sim 2.3 M_{\odot}$ )

Charbonnel & Talon (2009)

Surface brakes  
Increase diff rot.  
More rotational mixing and Li  
destruction

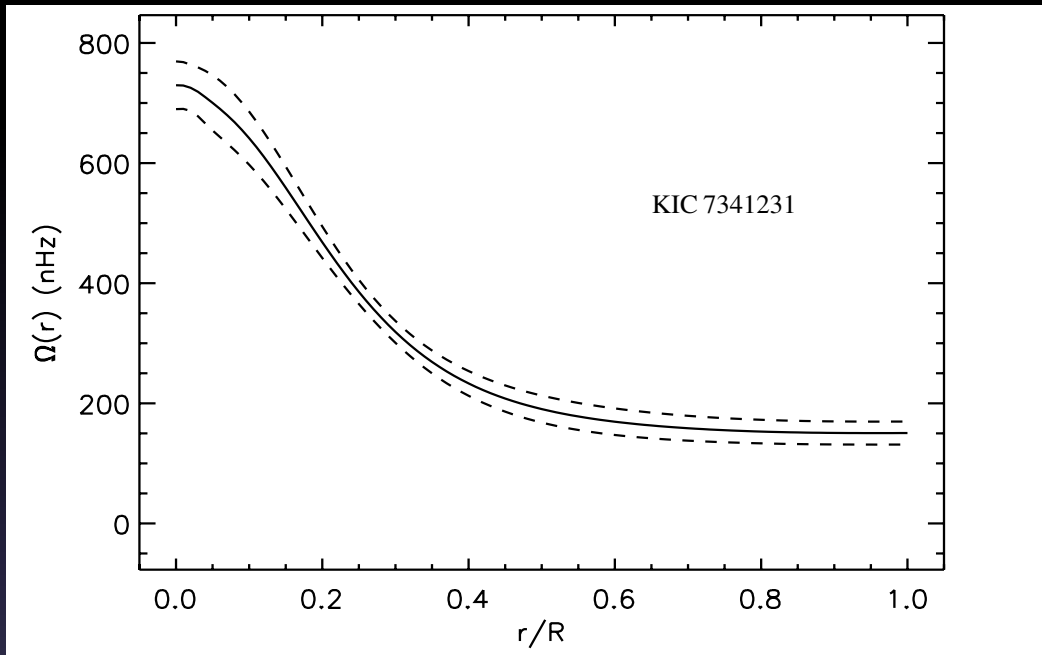


Gravity waves decrease diff. rotation.

Li destruction decreases

Why are we talking about gravity waves?(internal gravity waves - IGWs)

These IGWs are expected to be generated by the injection of kinetic energy from a turbulent region into an adjacent stable region

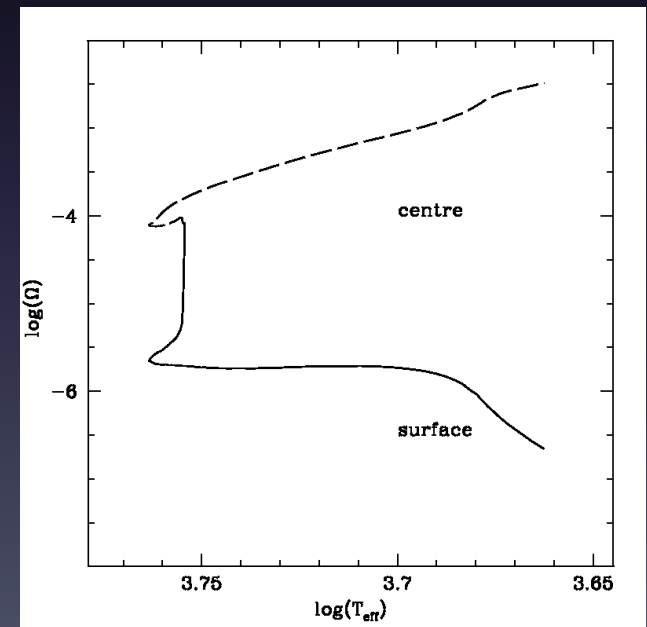


Inferred rotational profile

$0.84M_{\odot}$  lower RGB star

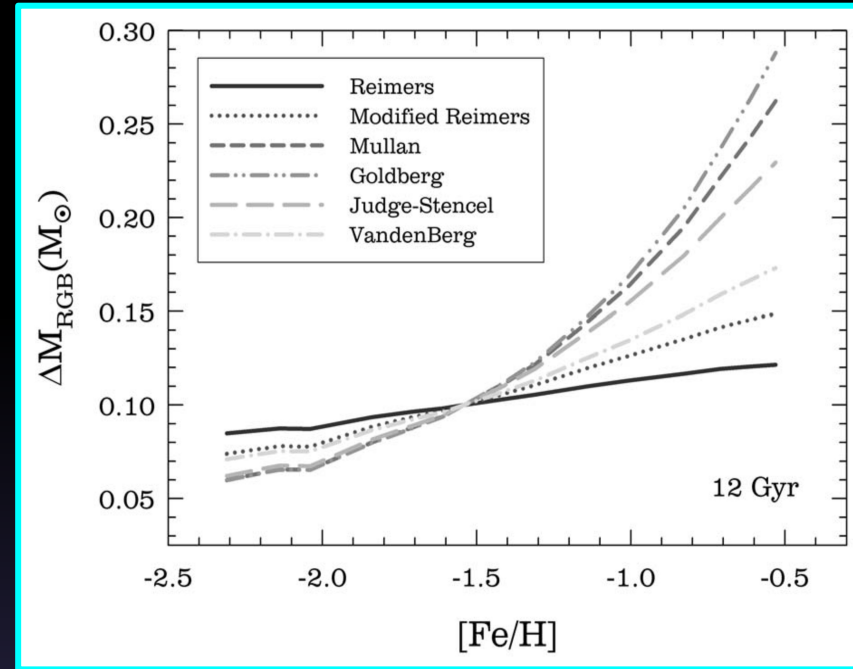
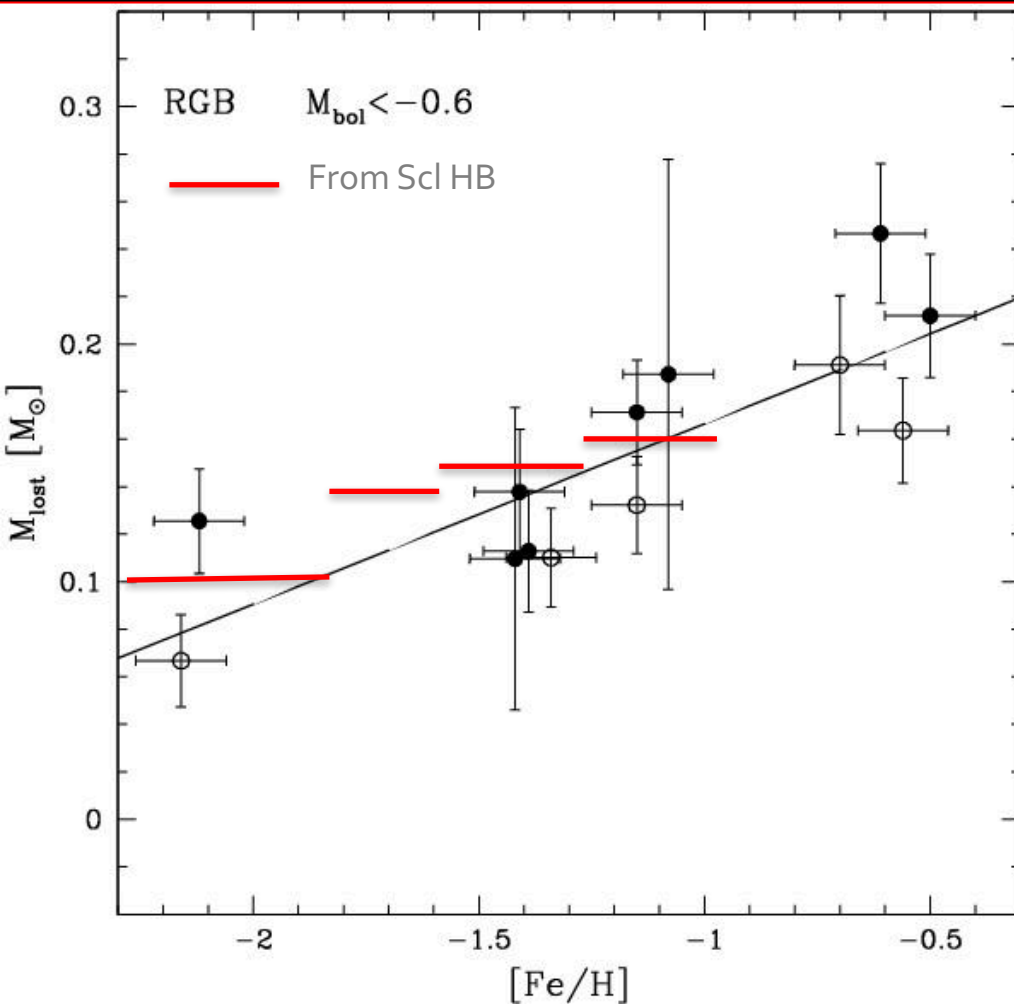
(Deheuvels et al. 2012)

Some extra angular momentum transport needs to be included in the current generation of rotating stellar models, because they predict much larger rotation rates for stellar cores compared to the surface



Model from Ekstroem et al. (2012)

# RGB mass loss



Catelan (2009)

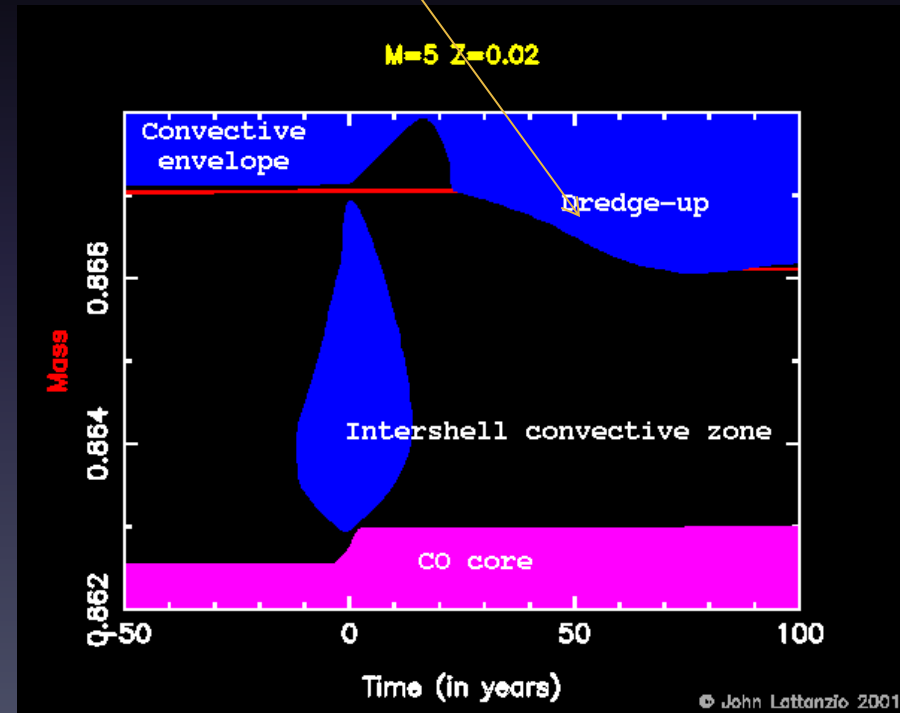
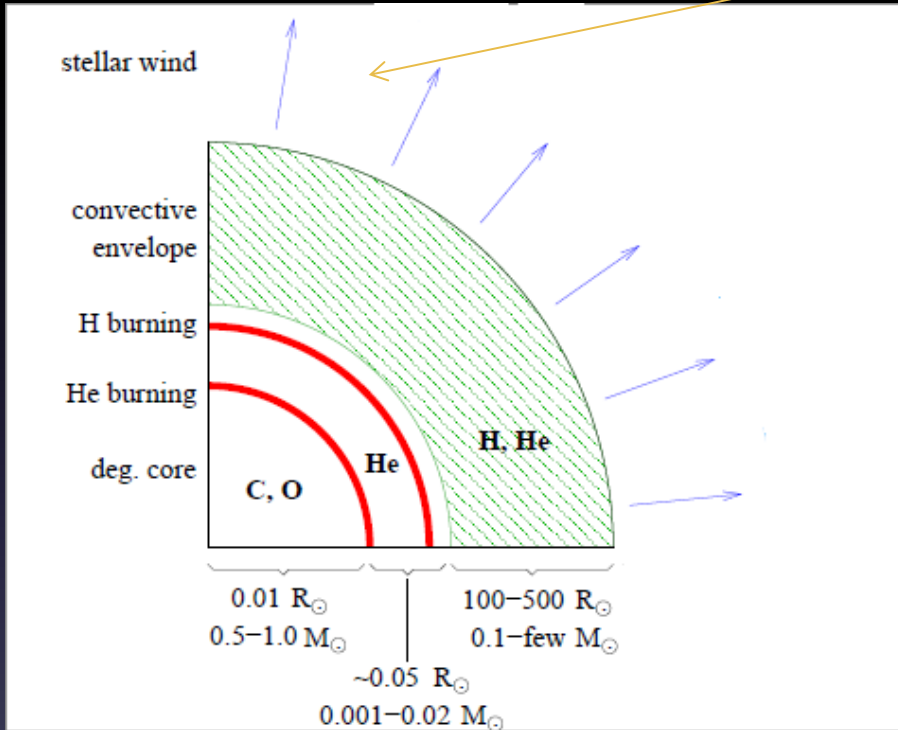
IR excess RGB globular cluster stars (Origlia et al 2014)

Synthetic HB modelling of Sculptor with known SFH (Salaris et al. 2015)

# AGB stars

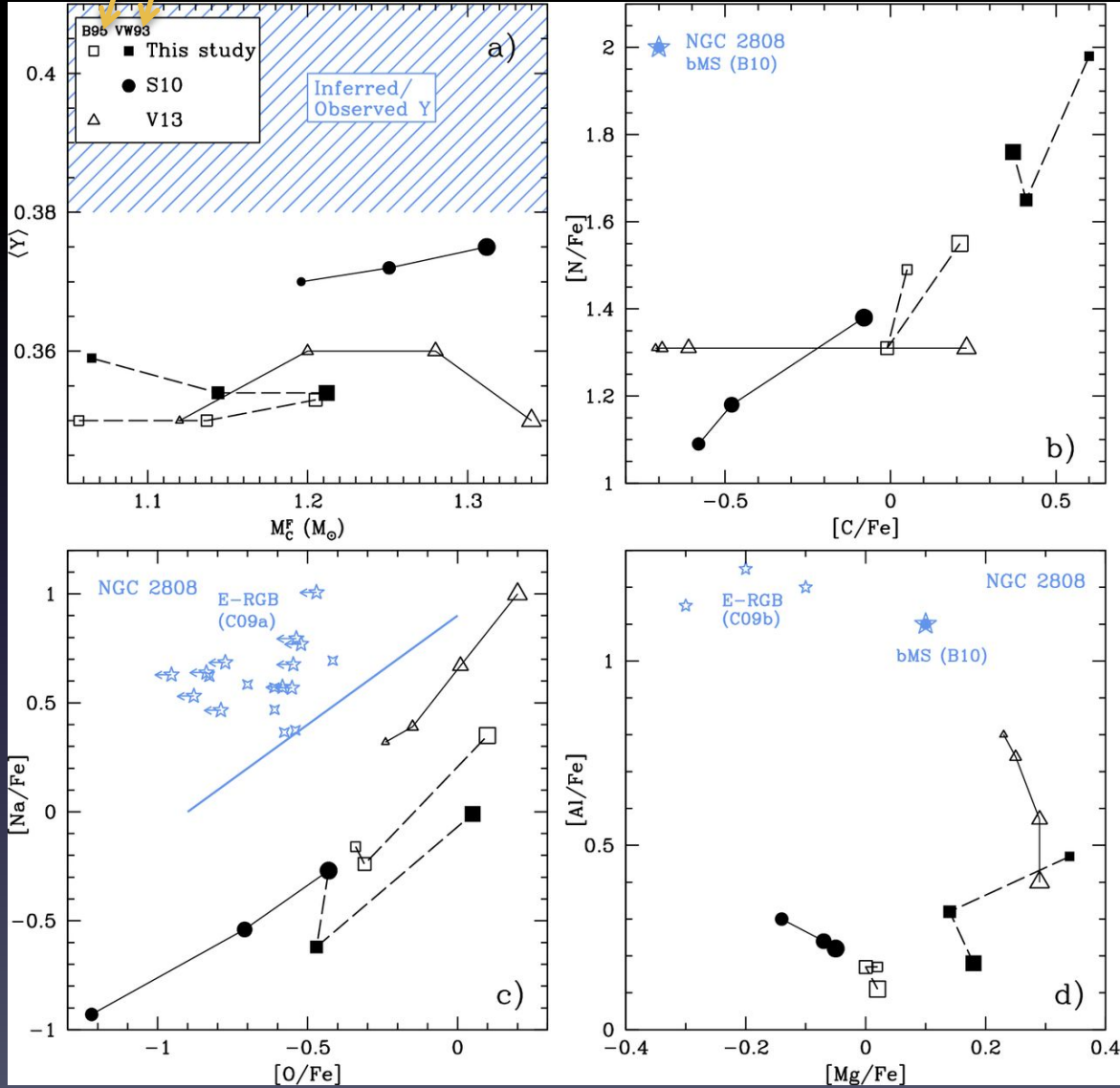
Mass loss, boundaries of convection

UNCERTAIN !!!!!



# Uncertain yields

Different AGB mass loss law



Doherty et al. (2014)

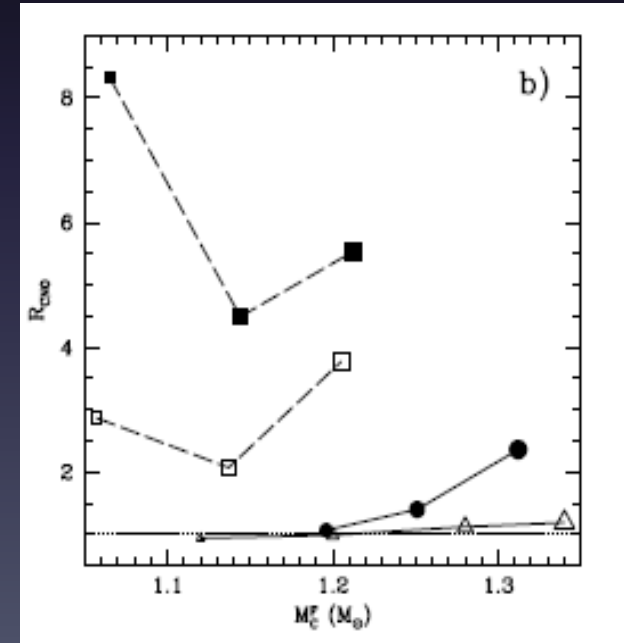
Super-AGB models only

$Z=0.001$

$M=6.5, 7.0, 7.5 M_\odot$

V13  $M=6.0, 6.5, 7.0, 7.5 M_\odot$

S10  $M=8.0, 8.5, 9.0 M_\odot$





# HOPES FOR THE FUTURE.....

## Convection

- test Magic et al. (2015) 3D-hydro  $\alpha_{\text{MLT}}$  calibration (covers a large [Fe/H] range) once they provide their boundary conditions
- Asteroseismology to help for boundary mixing and core He-mixing ?
- Hopefully, increasingly more realistic 3D hydro-simulations
- Eclipsing binaries (M-R diagrams)
- Asteroseismology of WDs

## Thermohaline mixing

More RGB spectroscopy on clusters of varying age to put stronger observational constraints but also improved hydro simulations and also stellar model calculations following criteria set out by Lattanzio et al. (2015)

## Element transport in radiative regions ??

## Mass loss

RGBs ..... hopefully more constraints from modelling of HBs in Local Group dwarf galaxies (e.g. Salaris et al. 2015)





# Instabilities in non-rotating stars

