



# AO modeling and PSFs

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**ESO**



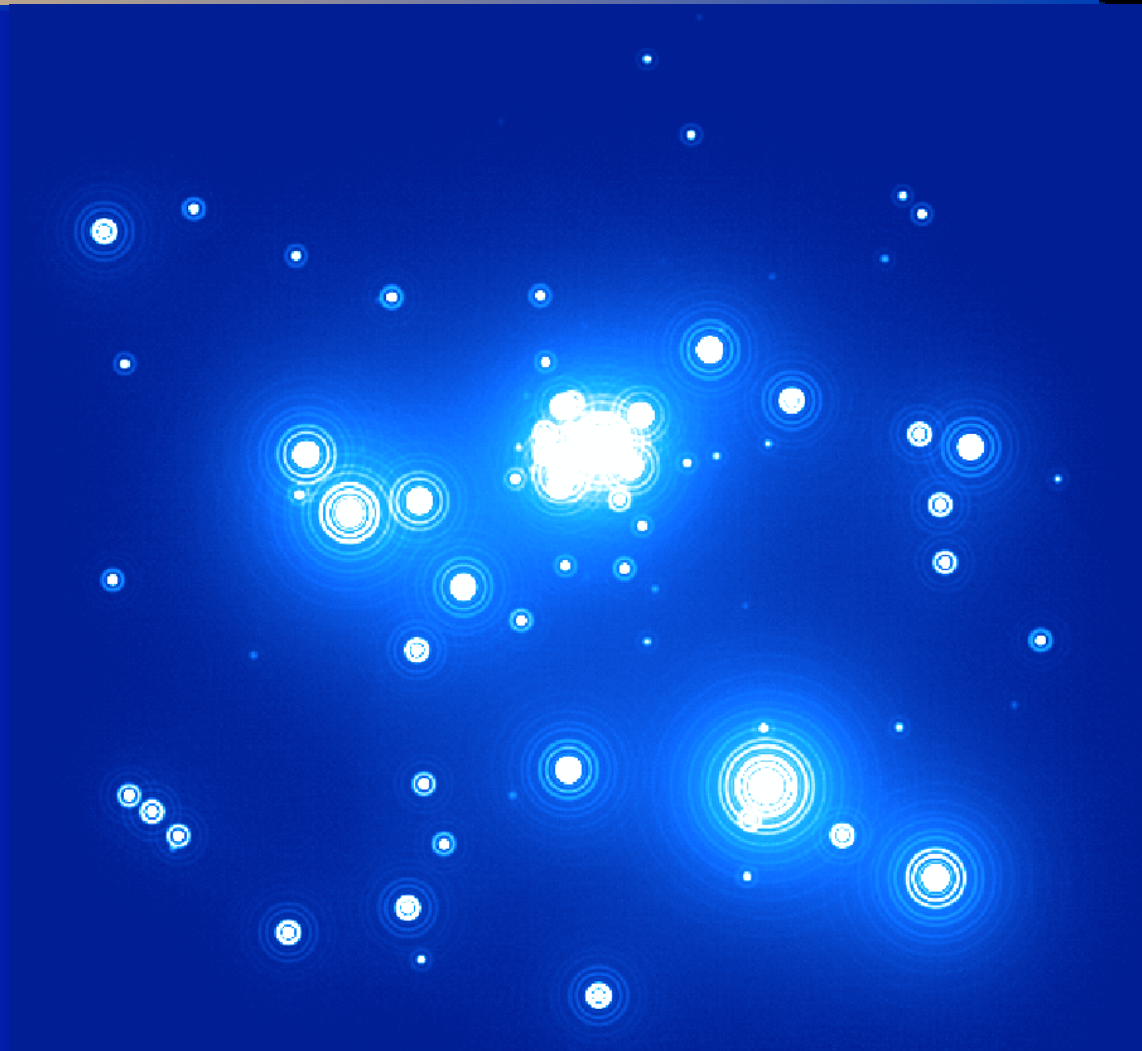
# Why AO simulations ?

- AO **designer** : Guidance on HW choices
  - How many actuators, subaps, laser powers, ...
  - Tolerancing (mis-alignments, jitters, component imperfections)
  - What errors dominate, sensitivity analysis (to physical parameters, like  $r_0$ ,  $C_n^2$ , Na profile...)
  - Development and testing of new algorithms
- **Astronomer** / user:
  - AO & Instrument definition and optimization
    - AO type (SCAO, GLAO, MCAO,...)
    - Instrument pixel scale, wavelength range,...
  - AO system performance requirement definition
    - Simulate science observation and see if you can extract what you want from the data
  - **Simulated observations to prepare data reduction pipeline**
  - **Exposure time calculator**
- “**Debugger**” of a real AO system in the lab / sky
  - Does system reach simulated simulated perf. If not, why ?
  - Allow to better understand AO system & telescope environment



# Astronomical simulations

- Use AO simulated PSFs to generate astronomical observation  
→ verify that astronomical **science goals** can be reached with that level of AO correction



Simulated K band image of a young Star forming region in the LMC. Exposure time=25 hours  
Calamida et al., DRM report, 2010



# Kinds of simulation / analysis tools

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- Error budgets / Analytic (without PSF)
  - Lump Error budget & analytical rms wavefront error
  - Identify error sources, calculate associated error, add effects in quadrature
- Getting PSFs is more important now, because new metrics are not as simple to analytically handle as Strehl
  - Ensquared Energy (→ Spectroscopic applications)
  - PSSn (Point Source Sensitivity – normalized → ELTs)
  - Contrast (XAO)
- Semi-analytic (Fourier) codes provide infinitely long PSFs
  - Some approximations needed (esp. LGS aspects)
  - Excellent to cover a large parameter space in short amount of time
  - Results then refined / confirmed with E2E codes.
- End to End
  - Pretty much as refined as can be
  - Need cluster / super server to run



# What is included in the simulations ?

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- By “default”, AO simulations analyze:
  - Atmosphere
  - AO system
  - Telescope
- Usually, no “instrument” (except in XAO)
- Provides PSF (long exp)
  - Basic coronagraphy option
- E2E, in addition, can provide:
  - Short exposure PSF @ loop rate (i.e. temporal behavior)
  - Short exposure Phase residual → could be sent to instrument model



# Fourier methods

- Analytical / Semi-analytical (with PSF output)
  - E.g. PAOLA, Cibola, Fourier based codes
    - Calculate filter functions for input phase
    - Calculate or simulate the effect of this filter on phase → AO PSF
    - Approximations can be used to address cone effect
  - Pro: fast, accurate, allow simulation of GLAO, Tomographic AO, provide long exposure “smooth” PSFs, **no residual speckles**
  - Con: Some errors difficult to model, correlations of error not necessarily well modeled
    - **Limitations caused by LGSs** (cone effect – beam overlap – finite pupil) because these models are Fourier based...
- Heavily used in “first stage” of project (large parameter space analysis)



# Fourier example: LTAO PSFs

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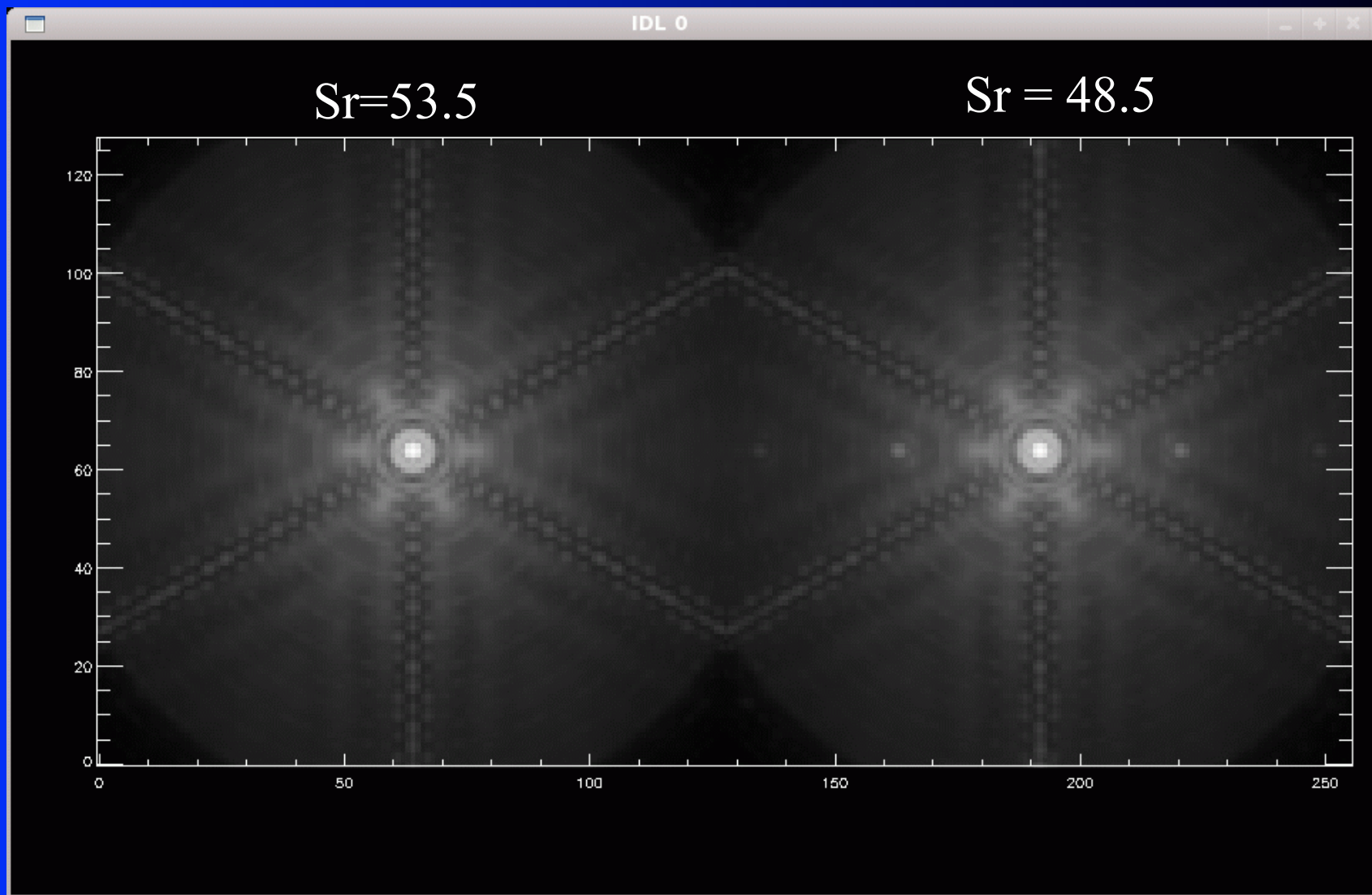
- Calculated @ ONERA (Fusco et al), semi-analytic (Fourier)
- 39m telescope, LGSs @ 1' (radius), 6LGS
- 40 layers simulated, 7 reconstructed
- Different wavelengths available:
  - 0.8, 1.0, 1.2, 1.6, 2.2, 10.0  $\mu\text{m}$
  - On-axis
  - With and without telescope WFE (very preliminary error budget)
  - Seeing=0.67 @ 30 degrees
- Contain some “reasonable” TT jitter ( $\pm 3\text{mas}$  rms for LTAO)
- $\rightarrow$  More realistic than @ phase A (but also less perf)





# ATLAS PSFs by ONERA / K band

Fusco et al.



Without telescope

With telescope





# What can we simulate in E2E?

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- Pretty much any AO system can be simulated:
  - SCAO, GLAO, LTAO, MCAO, MOAO, XAO, ...
- Mostly atmosphere, but telescope effects can be added
  - For example time series provided to instru. consortia have been added for SCAO
  - E-ELT Telescope simulations uses different simulation tools, results included as phase screen time series into E2E
- Each loop step is simulated
- ESO tool: **Octopus** (software & cluster)



# Closer to the physics: End to end models

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- Analytic / Semi-analytic codes have roughly dimensioned system
- Now need deeper analysis, for example:
  - Non linear effects in WFS
  - WFS dynamic range, pixel size, FOV, diffraction effects,...
  - DM stroke, IFs, hysteresis, effect of dead actuators,...
  - Tolerances (alignment errors, displacements...)
  - Spatial filtering for aliasing reduction
  - Loop stability and optimization
  - New control algorithms (Kalman, Predictive,...)
  - Segmentation/co-phasing effects on WFS
  - Speckle subtraction schemes
  - [...]
- “**Monte Carlo**” methods, since input (phase) is random

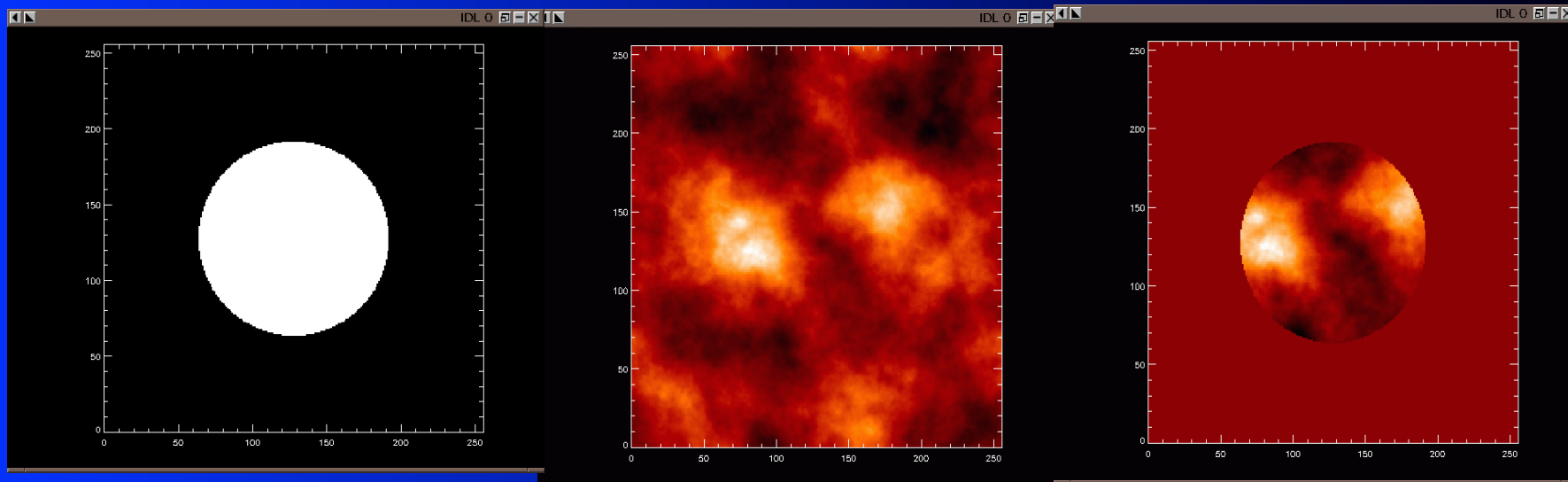


# End to end models

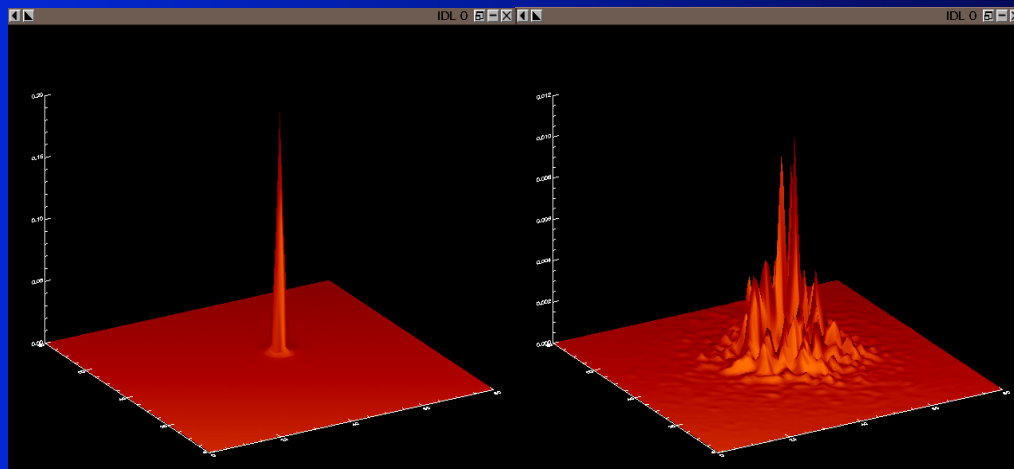
- Simulate as close as possible to the physics
  - Phase screens for atmosphere
  - FFTs to get WFS measurement (to include diffraction)
  - Centroiding process
  - Interaction matrix creation from measurements (if required by reconstructor)
  - Temporal evolution simulated by moving phase screens
  - PSF calculated from residual phase by FFT
- In principle very **accurate**
- Relatively easy to take new effects into account
  - No need for analytical formula, just need to modify phase
- **Heavy** numerically → slow
- Huge amount of work has gone into optimizing these codes (TMT MAOS, yao, Octopus, ONERA,...) to be as fast as possible



# Getting a PSF



FFT



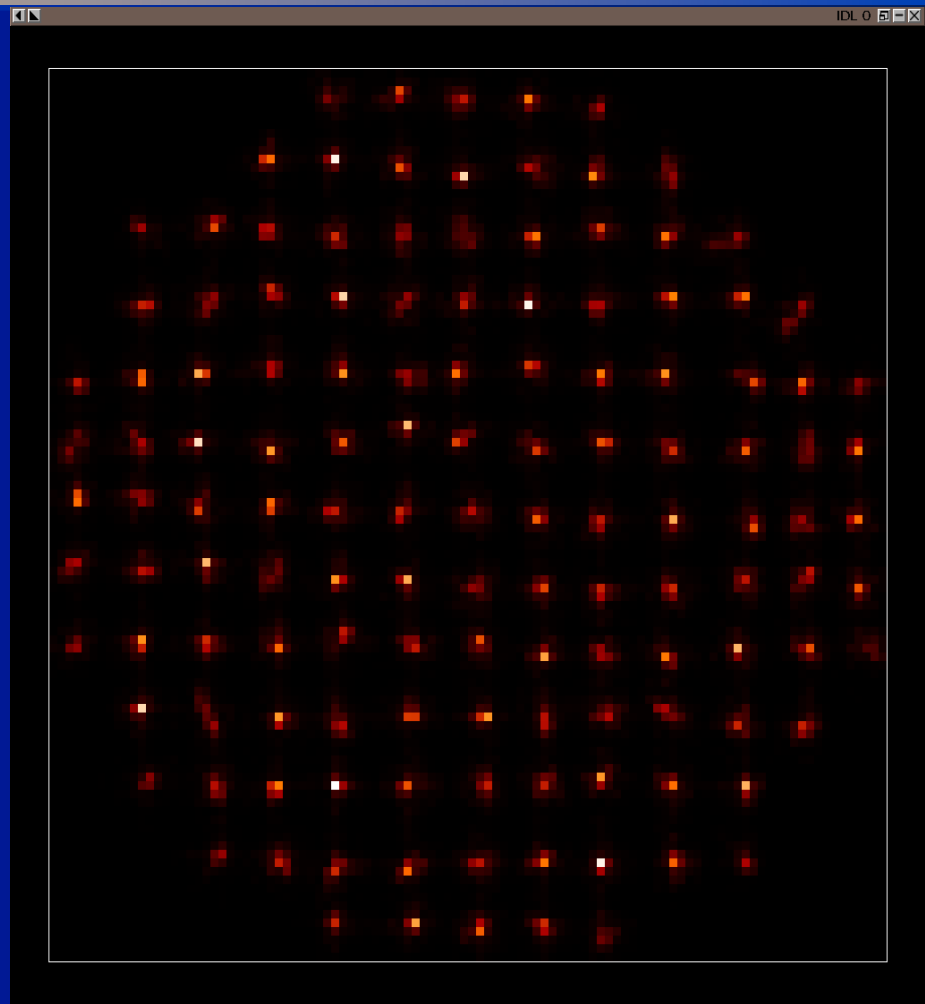
Airy pattern  
(no phase screen)

Speckle pattern  
(with phase screen)



# Wavefront sensor

- SH or curvature can be modeled
- Cut phase screen into sub-apertures
- FFT  $\rightarrow$  SH PSF = SH  
speckles are taken into account
- Add noise (photon, RON, sky, dark...)
- Threshold
- Compute centroids
- Output measurement vector



- At each step **errors** (e.g. flat field or **novel treatments** (eg WCOG, spatial filtering)) can be added.
- For MCAO, WFSs can be **cloned** to look at different stars



# Closed loop / temporal evolution

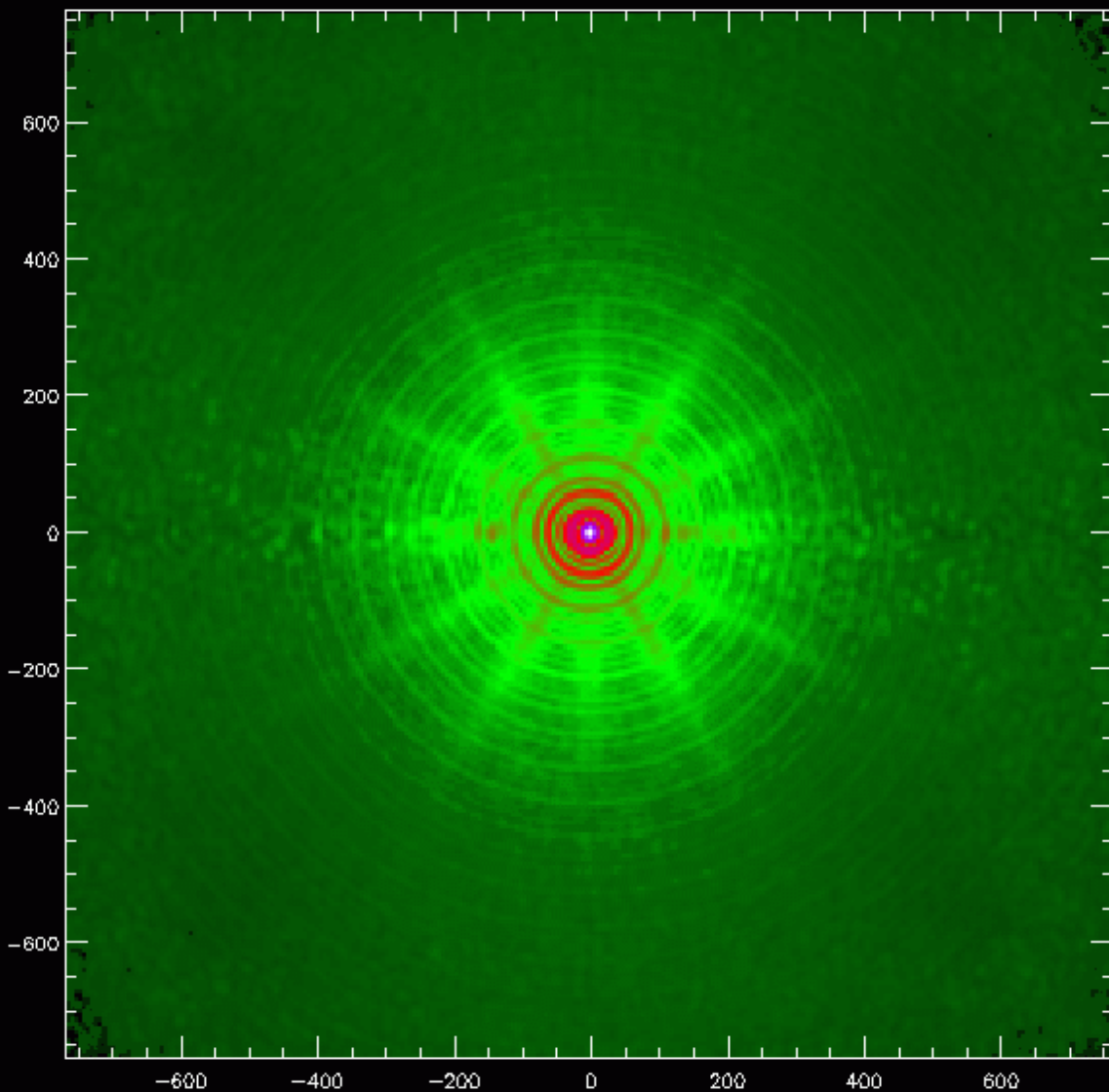
- Temporal behavior:
- Shift phase screens
- Propagate screens
- New WFS measurement
- IM # measurements  $\rightarrow c$
- New DM commands:  $c_n = c_{n-1} + g c$  (g:gain)
- New DM shape
- Atm. phase - DM shape = Residual phase
- Long exposure PSF = Sum(Short exposure corrected PSF)





# LTAO PSF, Atm only

IDL 0



5.9 mas / pixel  
Axis in mas  
Stretch:  $\wedge 0.2$   
K-band  
8s integration  
(4000it@500Hz)

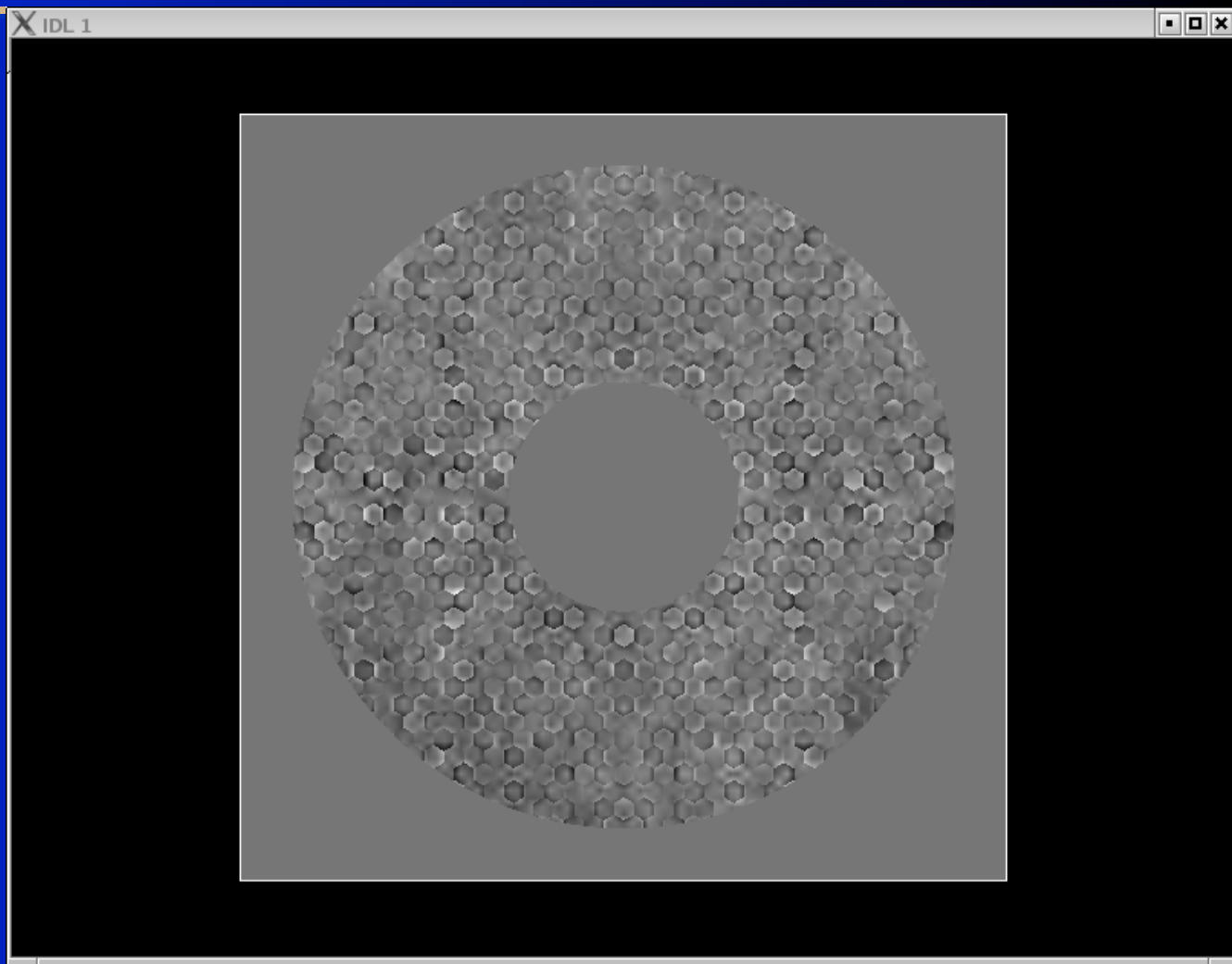
Circular pupil here,  
No segmentation

LGS symmetry seen  
here, not primary





# Interaction with (a more complex) telescope



How the AO corrects a particular mode of the segmented telescope  
→ Only high spatial frequency modes remain, due to segment imperfection  
(exaggerated in this case)



# Parallelization



End to End simulations can be numerically heavy: clusters, GPUs, parallelism, ...



# Simulation validation

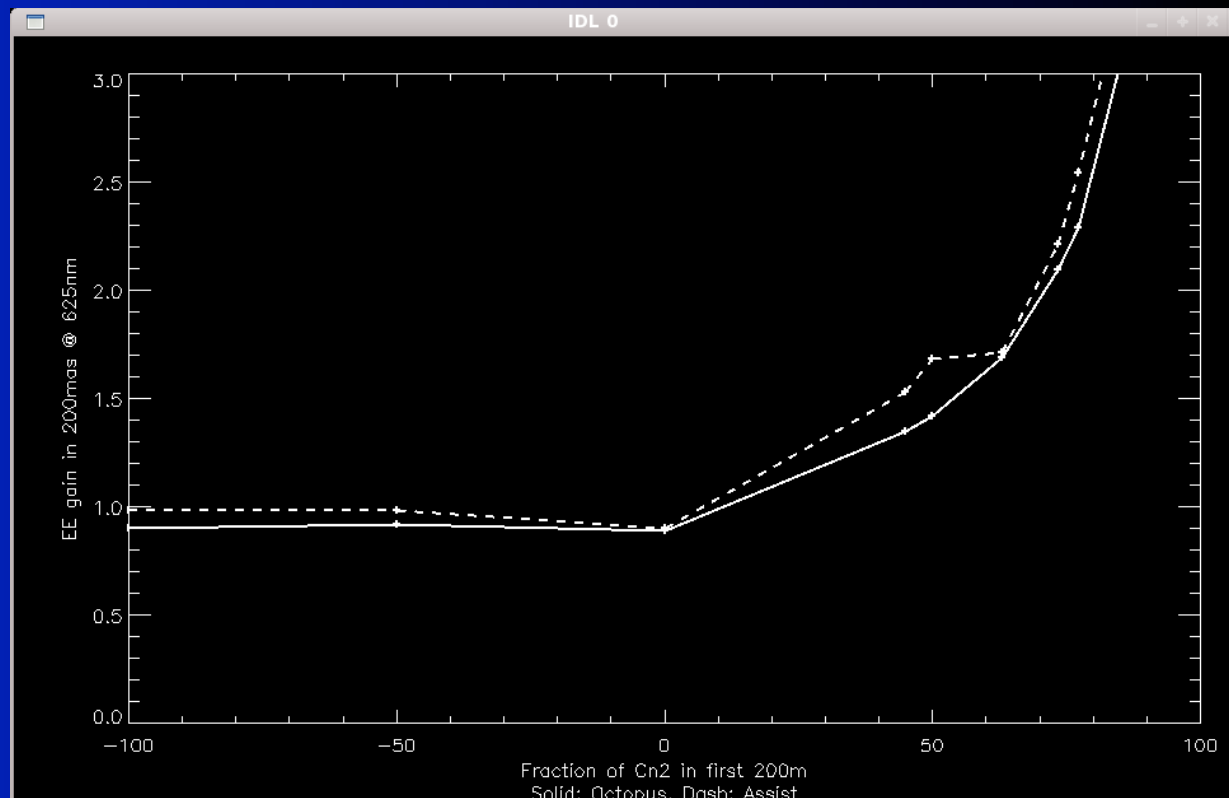
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- How do we know simulations are **correct** ?
- Software against software
  - Classic paper, Rigaut, Ellerbroek & Northcott, Appl. Opt, **36**, 1997
- **Lab** experiments & integration in lab
  - Lab experiment used to validate simulation results
  - Need to simulate the lab experiment & its particularities
  - Some “extra” effects, specific to lab environment are likely
- **Sky**
  - Analyze AO system post-facto, and understand its real life limitation (e.g. van Dam et al, 2004).
  - This validates simulation AND AO system



# Lab validation of Octopus

Here, a lab “bench” is set up  
With the sole purpose of  
validating  
System performance  
→ **Controlled** environment  
→ Known input (phase  
screens) to know output.



GALACSI WFM (for MUSE), on ASSIST. EE in 200 mas gain vs. Cn2 profile used on the bench



## Using E2E simulated PSFs for “astronomers”

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- One problem with E2E PSFs: residual speckles
  - Run simulation @ 500Hz – 1kHz
  - Takes forever (6h – 2days for 1 point)
  - → only some seconds (1-10-100) of data can be simulated “easily”
  - → Residual speckles are still visible on the PSFs
- Science data: 20min-80h.
  - No speckles at all, very smooth PSF
- Total number of PSFs can be parallelized, so producing cubes of PSFs is “easy”. Long ones: not so much.





# How to solve speckle problem in E2E?

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- Use analytic simulated PSFs as “fitting” functions
  - Fudge analytic simul to get same “result” metric as E2E (Strehl, EE,...).
  - Assume image structure is “roughly” the same as E2E
- Use PSFs from lab
  - May also be limited in time span (limited phase screens)
- Use radial averages
  - Assumes centro-symmetric PSF (not true for tomography)
- Use ad-hoc fitting functions (splines,...) to fit E2E PSF
  - May be difficult to say what is speckle, what is PSF structure
- OR: **play with the E2E model**
  - Some tricks can be applied to reduce speckles, like:
  - uncorrelated phase screens to accelerate convergence (but lose time info)
  - Simplify E2E to accelerate code to run many more iterations
  - [...]



# Conclusions

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- Different tools are available to generate AO PSFs
  - Each have their limitations:
  - Analytic: slightly less accurate (but probably good enough ?), smooth PSF, infinite exposure time, some approximations
  - E2E: residual speckles due to short integration time, but more “effects” included, more precise. Overkill ? Or necessary ?
  - “Massaging” PSFs may be necessary
- How accurate do the PSFs need to be ?
  - What criterion to say “this PSF is good for our use” ?
- What and how do you want to use the PSFs ?
  - May dictate which kind of PSF is used
- There are many tools. Choose the right one !
  - There will be work associated to get the PSFs you want