

# Halo Occupation Distribution Modeling of AGN Clustering: An Overview

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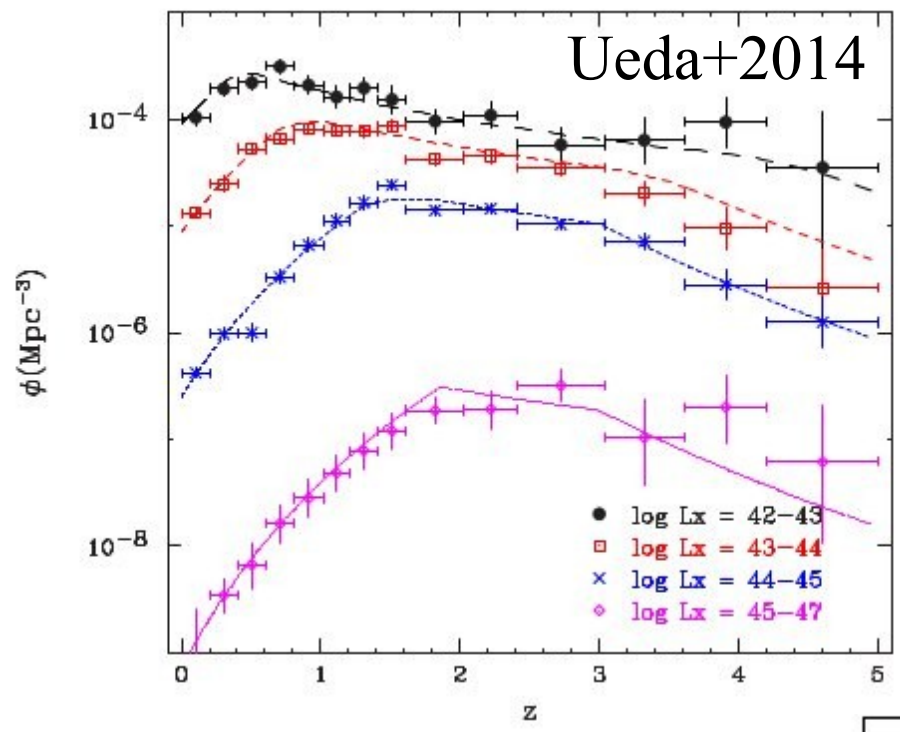
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# Introduction

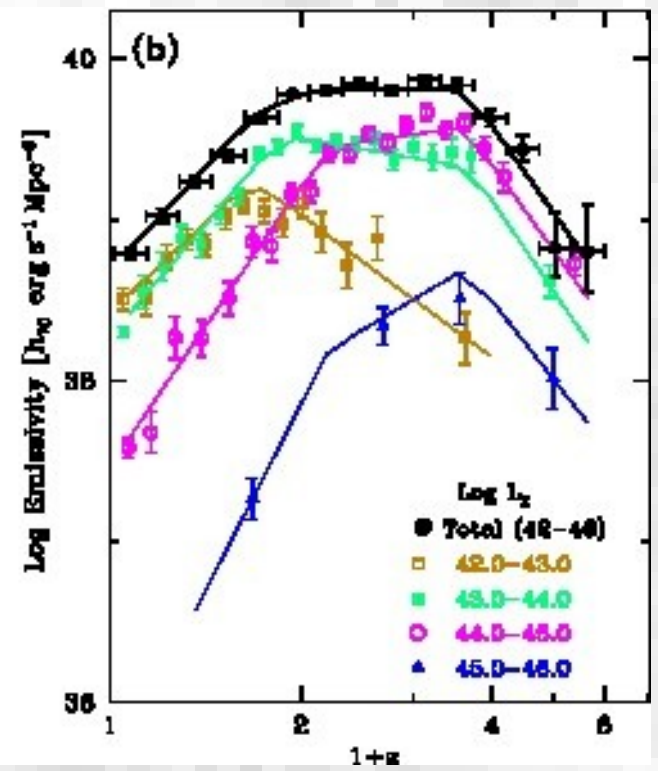
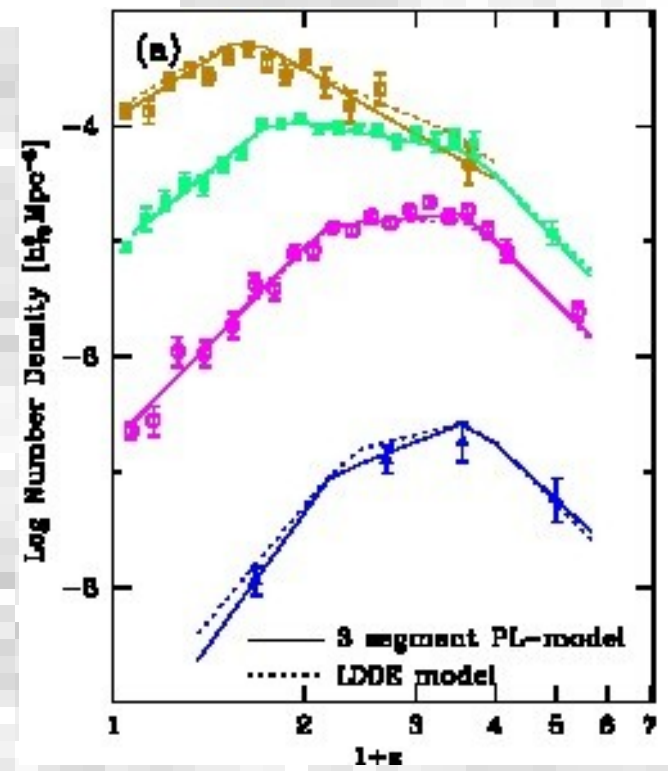
- Why AGN Clustering is important for understanding the accretion history/mechanism?
  - ★ A small fraction of galaxies show AGN activity (It's an event!)
  - ★ When and where, with what mechanism the SMBH accretion occurs? Statistical properties of AGNs give observational clues.
    - Merger driven?
    - Secular Evolution/Internal to galaxy?
  - ★ Observational Clues
    - **Luminosity functions and its cosmological evolution (AGN downsizing)**
    - **Host galaxy properties (green valley, Merger remnant features).**
    - **Black Hole Demography.**
    - **Environment and underlying large scale structure (clustering).**

# Latest determination of X-ray Luminosity Luminosity Function/Evolution



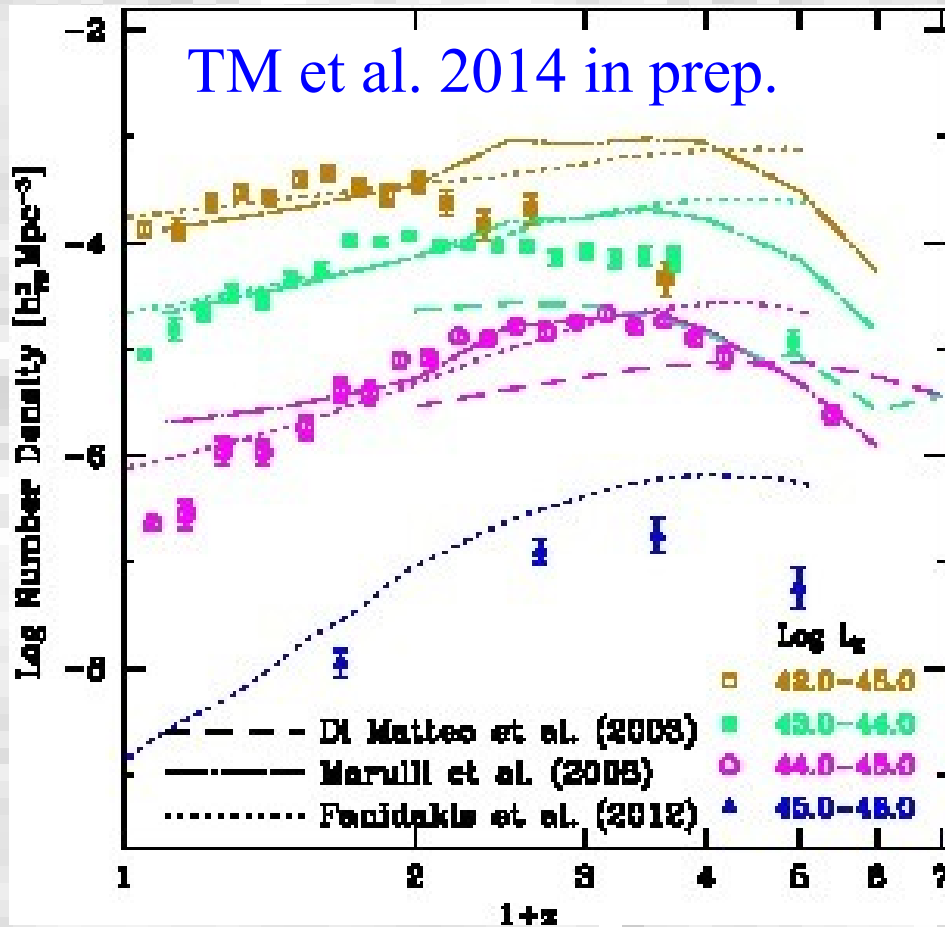
Two redshift break structure revealed.

**AGN**  
Downsizing is still strong!



TM+ to be submitted soon

# Comparison with Semi-analytical models

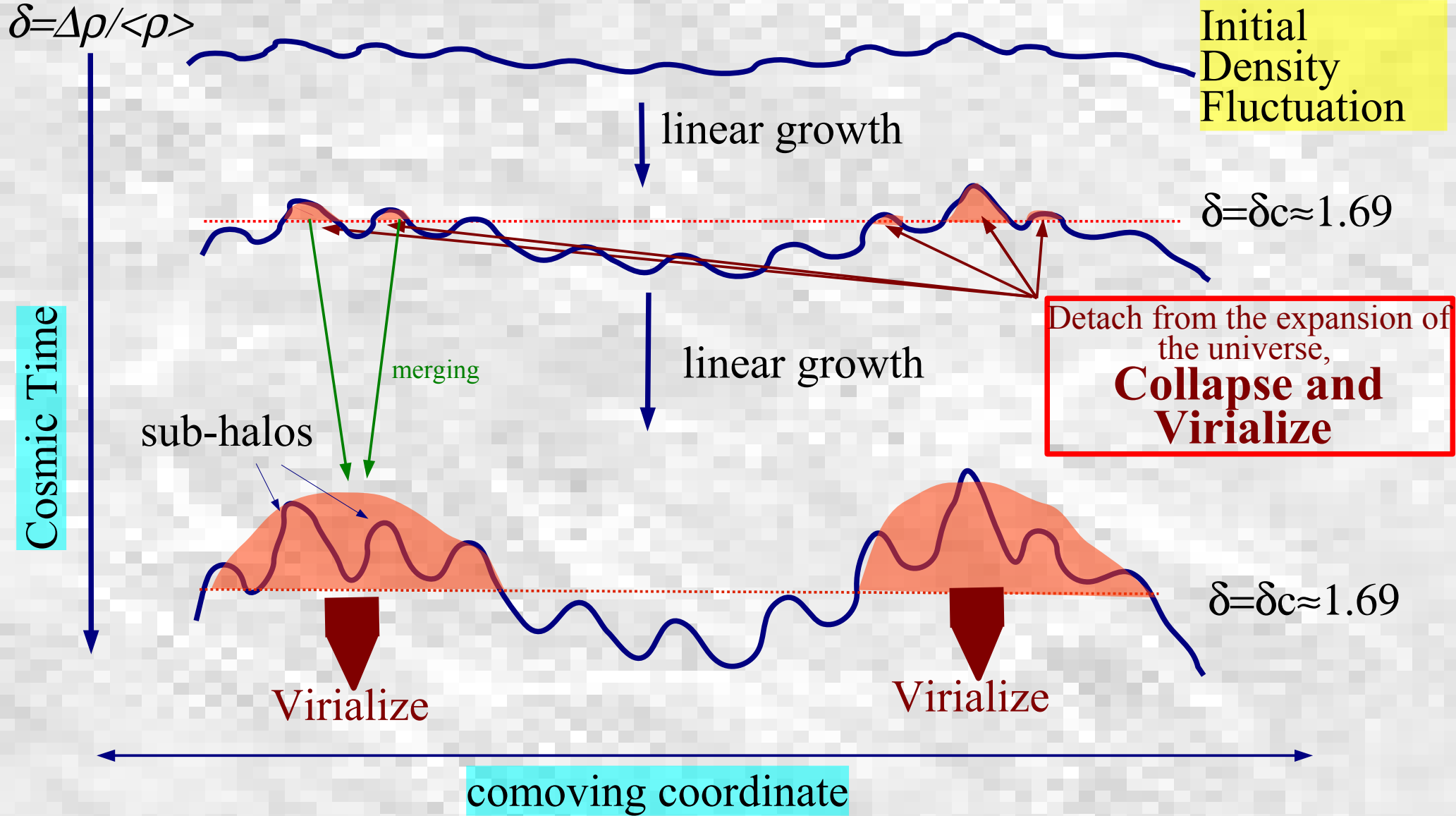


Semi-analytical models of Marulli+2005; Fanidakis+2012 overpredicts number densities of high luminosity AGNs.

## Where in the Cosmic Web do AGNs occupy (accretion occurs)?

- **Observers** see the universe as galaxies, AGNs, clusters etc..
- **Theorists** see the universe as a bunch of Dark Matter Halos (DMH)--(Maybe an outdated comment!)
- How can we relate these halos with observed objects?

# What are the DMHs?



Dark Matter Halos: The collapsed & Virialized structures

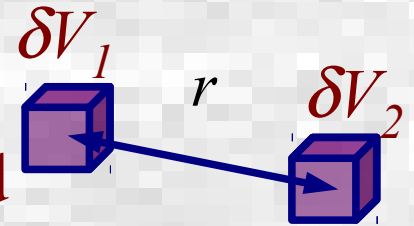
# Two-point Correlation Function

Excess number of pairs separated by  $r$   
over the random distribution

- Joint probability  $\delta P$  of finding an object in both of the volume elements separated by  $r$  is represented by:

$$3D: \delta P = n^2 [1 + \xi(r)] \delta V_1 \delta V_2$$

$\xi(r) = 0$  if objects are randomly distributed



- In the linear biasing scheme, the two point 3-D auto correlation function (ACF) is related to bias parameter by:

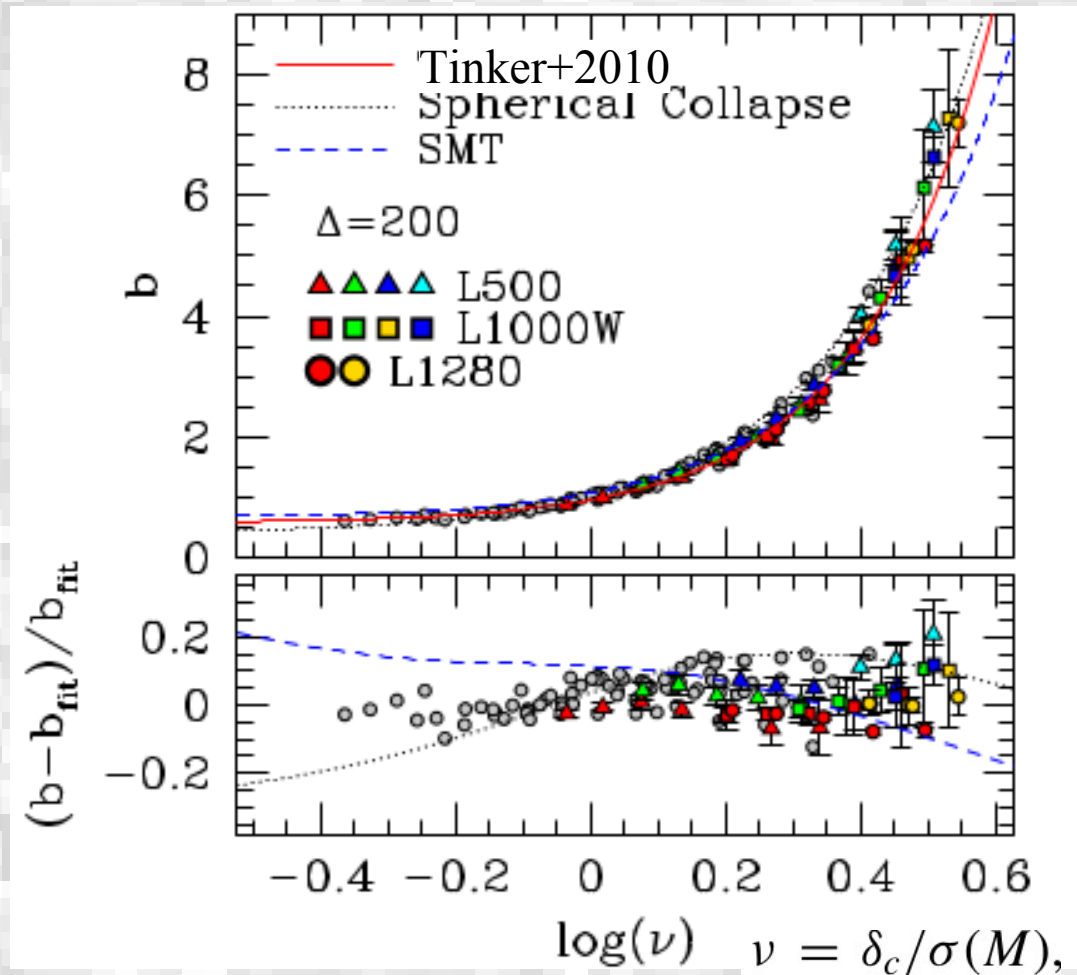
$$\xi_{\text{obj}}(r) = b_{\text{obj}}^2 \xi_{\text{mass}}(r),$$

- and two point 3-D cross-correlation function (CCF) between catalog 1 and 2 is related to the bias parameters of 1 & 2 by:

$$\xi_{12}(r) = b_2 b_1 \xi_{\text{mass}}(r)$$

# Clustering measurements → AGN bias

- The large-scale bias of dark matter halos depends on its mass.
- Here the "Halo mass" means the largest Virialized structure the object in question belongs to, and **NOT** represents the sub-halo mass.
- Measurements of bias of a sample of AGNs is an indicator of the "typical" mass of the DMHs that the sample is associated.

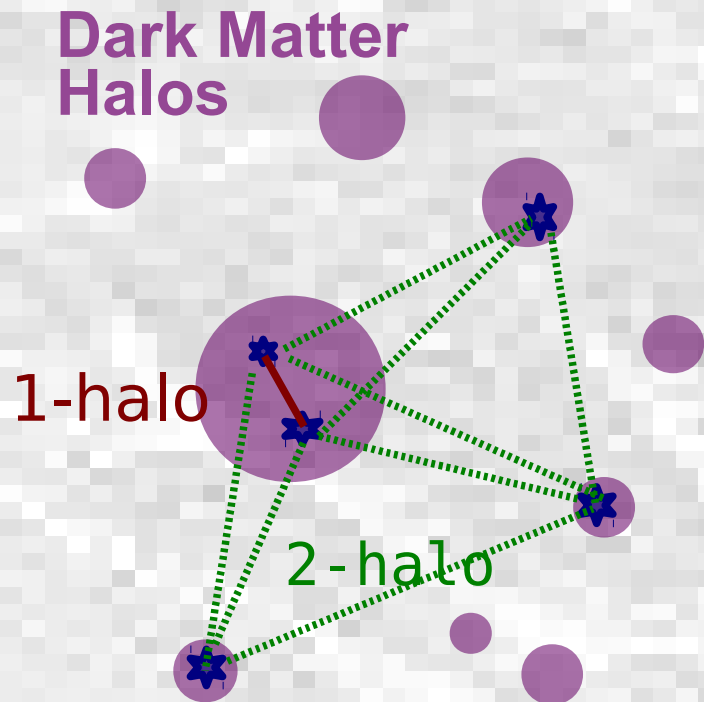


$$b_h(\nu) = 1 + \frac{1}{\sqrt{a}\delta_c} \left[ \sqrt{a}(a\nu^2) + \sqrt{ab}(a\nu^2)^{1-c} - \frac{(a\nu^2)^c}{(a\nu^2)^c + b(1-c)(1-c/2)} \right]$$

**This simple relation is only valid in the linear regime ( $r > \sim 1-2 h^{-1}$  Mpc)**

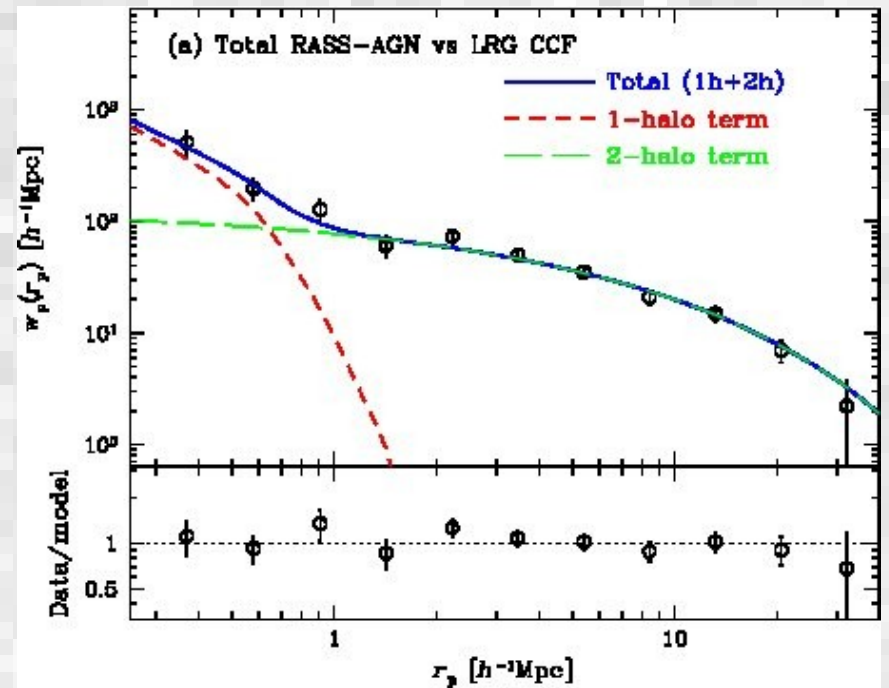


# Modeling of the linear and non-linear regimes with Halo Occupation Distribution (HOD)



$$\xi(r) = [1 + \xi_{1h}(r)] + \xi_{2h}(r)$$

1-halo term                  2-halo term



• Model the correlation function as the sum of the contributions from pairs:

- within the same DMHs
- from different DMHs.

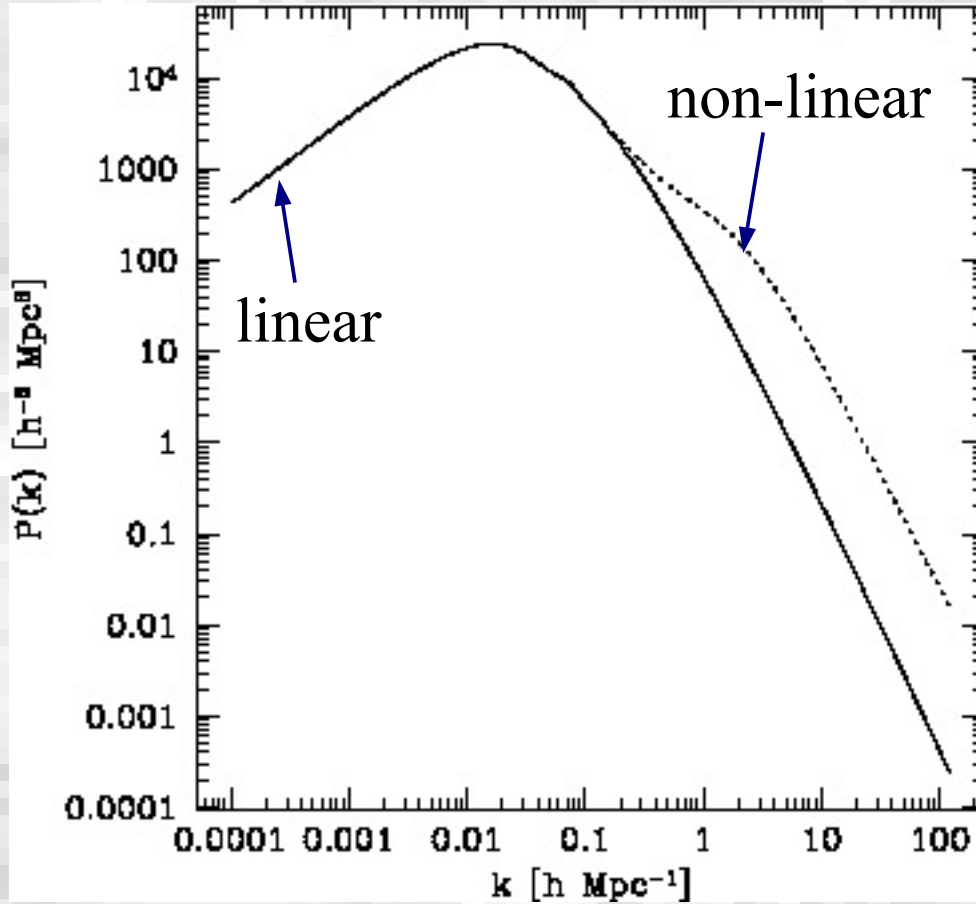
# The HOD modeling is very popular in interpreting galaxy clustering

- Cooray & Sheth (2002) for classical review.
- Tinker+2005; 2010; van den Bosch+13 for recent theory

## Application to AGN 2P Correlation Functions

- Padmanabhan+2009
  - SDSS LRG vs optically selected QSOs CCF; satellite fraction > 25%
- TM, Krumpe, Coil, Aceves 2011
  - SDSS LRG vs X-ray selected AGNs CCF from ROSAT All-sky survey
- Starikova+2011
  - Chandra Boötes field. Consider both  $r_p$  and  $\pi$  directions. Strict upper limit on satellite fraction ( $< \sim 0.1$ ).
- Kayo & Oguri+2012 (previous talk)
- Richardson+2012,2013
  - SDSS QSOs and Alleinato+11 XMM-COSMOS ACFs.
  - Full galaxy HOD-type parameterization+MCMC parameter search.

# Construction of HOD models



- In the power spectrum space  $P(k)$ .

Generated with “camb” (<http://camb.info/>)

# Large Scales (approx 2-h term)

- Matter (linear) power spectrum:  $P_{matter,lin}(k,z) \rightarrow \xi_{matter,lin}(r,z)$ 
  - $P_{lin,matter}(k,z) = D(z)P_{lin,matter}(k,z=0)$ ;  $D(z)$ , linear growth factor
- Linear biasing (i.e. Scale independent) at large scales
  - $P_{lin,sample}(k,z) = b_{sample}^2 P_{lin,matter}(k,z)$
  - $\xi_{lin,sample}(k,z) = b_{sample}^2 \xi_{lin,matter}(k,z)$
- DMH bias  $b(M_h, z)$  (e.g. Sheth, Mo, Tormen '01; Tinker+'05,'10)
- DMH mass function  $\phi(M_h)$  (e.g. Sheth & Tormen '99; Jenkins et al. 2001; Tinker+'05)
- **$\langle N(M_h) \rangle$ : Halo Occupation Distribution (HOD)**
  - Mean number of sample objects per DMH as a function of  $M_h$ .
- The sample bias  $b_{sample}$  is the weighted mean  $b(M_h, z)$  over DMHs
  - $b_{sample} = \int b(M_h) \langle N(M_h) \rangle \phi(M_h) dM_h / \int \langle N(M_h) \rangle \phi(M_h) dM_h$

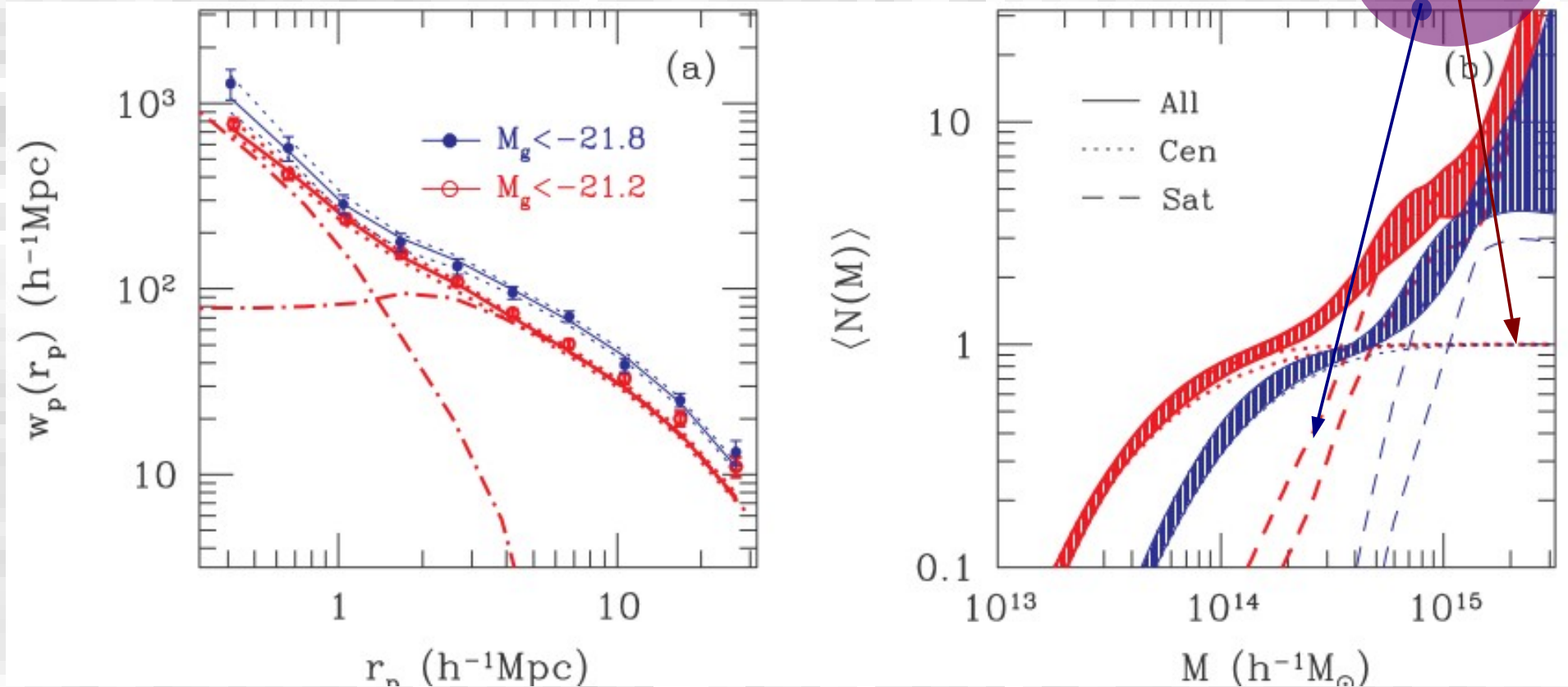
# Small Scales (1-halo term)

- $\langle N(M_h) \rangle = \langle N_c(M_h) \rangle + \langle N_s(M_h) \rangle$ 
  - $\langle N_c \rangle(M_h)$  for the objects occupying at the **center** of the host DMH.
  - $\langle N_s \rangle(M_h)$  for “**satellites**”, occupying non-center location of the host DMH.
- **Assume that** the mean radial distribution of “satellite” objects follows the mass profile of the DMH (e.g. Navarro, Frenk & White [NFW] profile).
- Contribution of the same DMH pairs to  $[1 + \xi_{1h}(r)]$ .
  - Central-satellite pairs follow the DMH mass profile
  - Satellite-satellite pairs follows the DMH mass profile convolved by itself.
  - Central-central pairs: No such pairs.

# HOD Analysis of Galaxies

## Example of Luminous Red Galaxies (Zheng+2009)

$\langle N_c(M_h) \rangle$  center: smoothed step function saturated to 1.  
 $\langle N_s(M_h) \rangle$  satellite: power-law\* $\langle N_c(M_h) \rangle$  or spline



# Application to SDSS Luminous Red Galaxies (LRGs) vs RASS AGNs

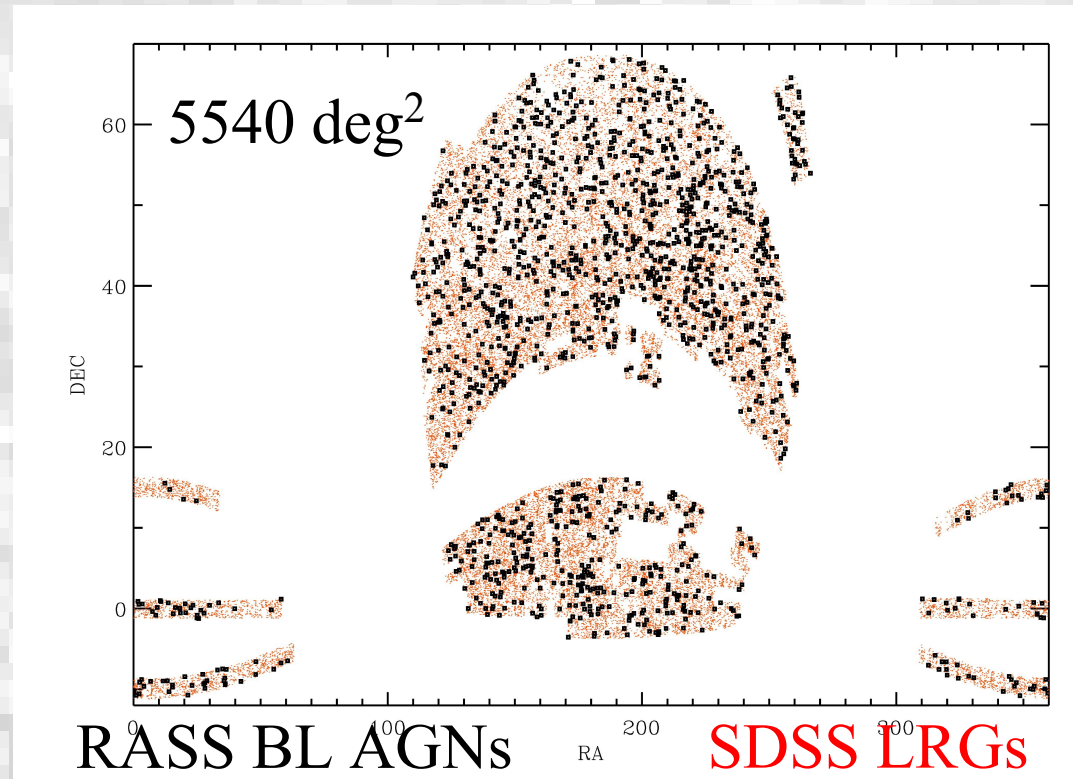
TM, Krumpe, Coil, Aceves (2011)

## Galaxy Sample

- SDSS LRG Volume Limited Sample
- Defined by Eisenstein et al. (2001), redrawn by us for DR4+
- $M_B < -21.2$ ,  $0.16 < z < 0.36$
- 45899 LRGs Galaxies

## X-ray AGN sample:

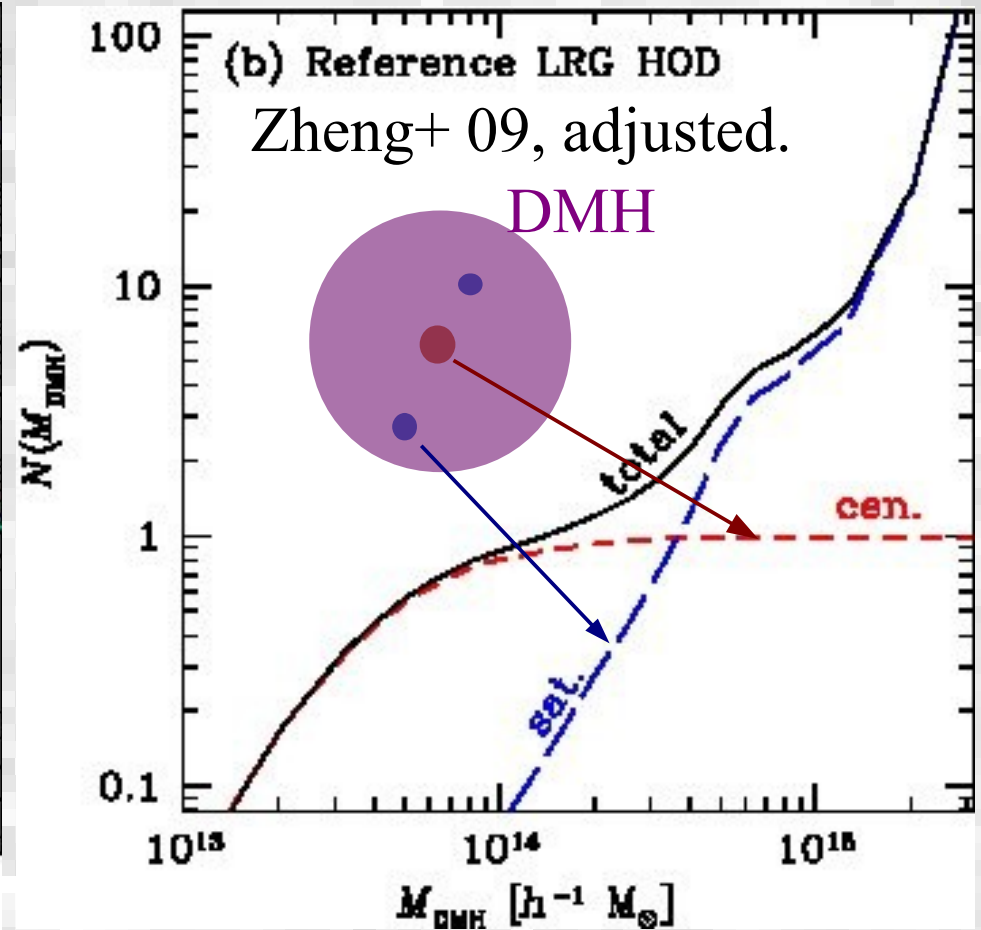
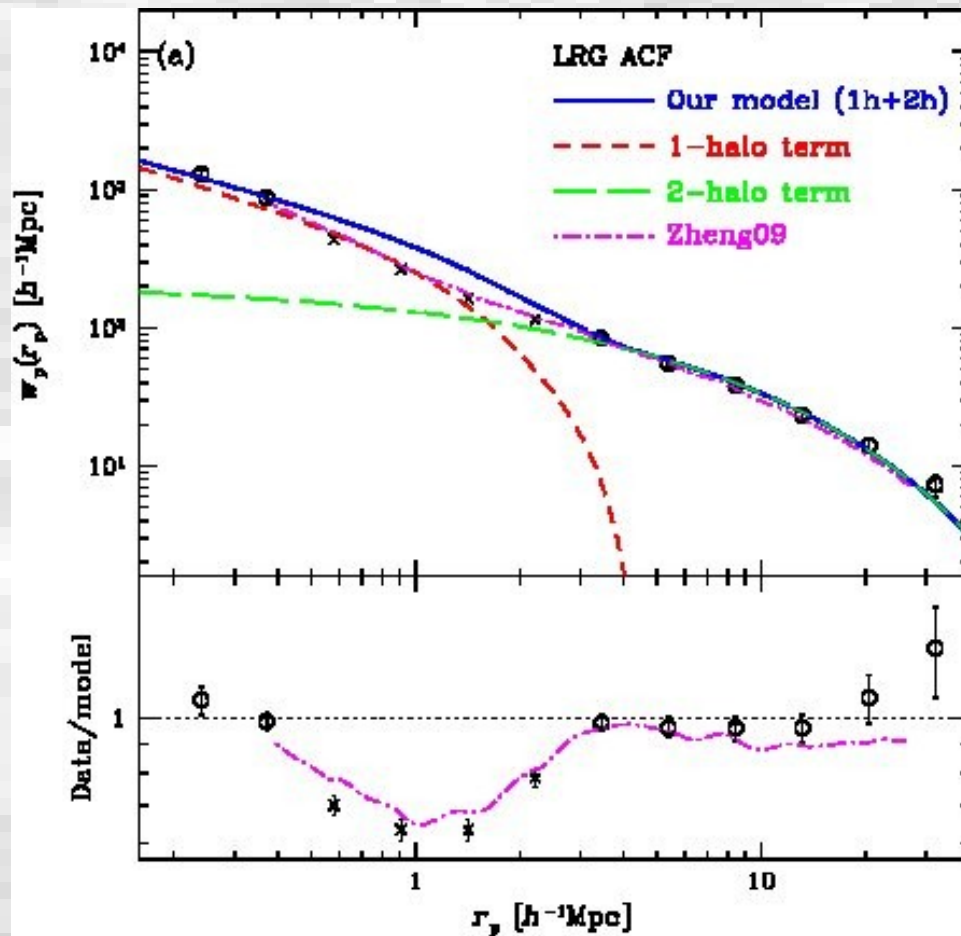
- ROSAT All-Sky Survey (RASS) sources matched with the SDSS broad-line AGNs (Anderson et al. 2003; 2007).
  - 1552 AGNs in  $0.16 < z < 0.36$
- Excluded Narrow-line AGNs.
- Flux limited sample.



**These two samples are completely separate. No common object.**



# HOD of LRGs as our Tracer Set





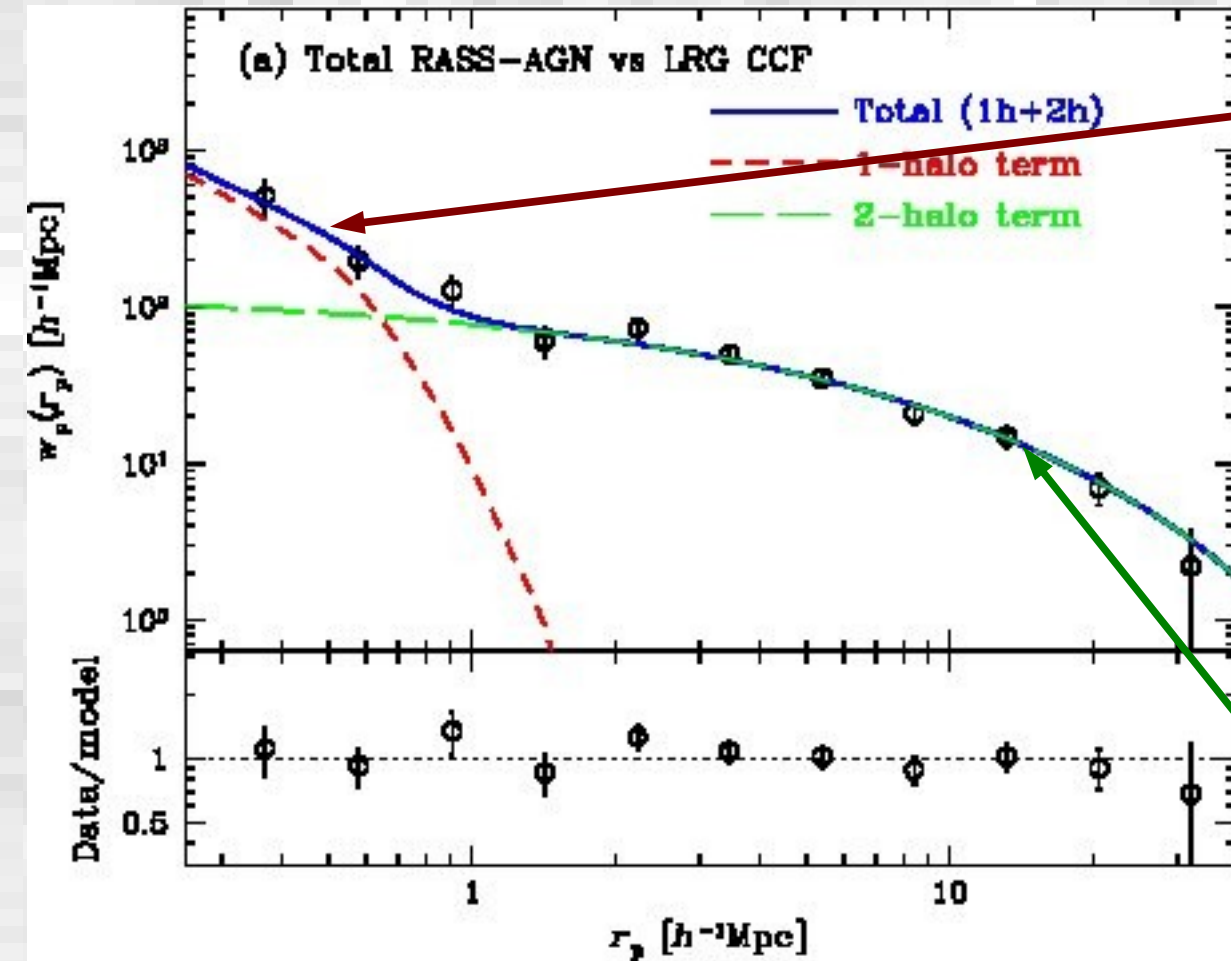
# Applying HOD modeling to the AGN-LRG CCF

When modeling our CCF, we consider four HODs

- $\langle N_{\text{LRG},c} \rangle(M_h)$  &  $\langle N_{\text{LRG},s} \rangle(M_h)$  for the central and satellite LRGs respectively.
- $\langle N_{A,c} \rangle(M_h)$  &  $\langle N_{A,s} \rangle(M_h)$  and for the AGNs.
- First, we derive  $\langle N_{\text{LRG},c} \rangle(M_h)$  and  $\langle N_{\text{LRG},s} \rangle(M_h)$  using the ACF of the LRGs.
  - ➔ They can be determined with a much better statistics.
- Then, using the resulting (fixed) LRG HODS, we constrain  $\langle N_{A,c} \rangle(M_h)$  &  $\langle N_{A,s} \rangle(M_h)$  by fitting to the AGN-LRG CCF.

# Model A: Simple model

Assumption: All AGNs that reside in halos containing LRGs (or contributing to the 1-h term) are satellites.



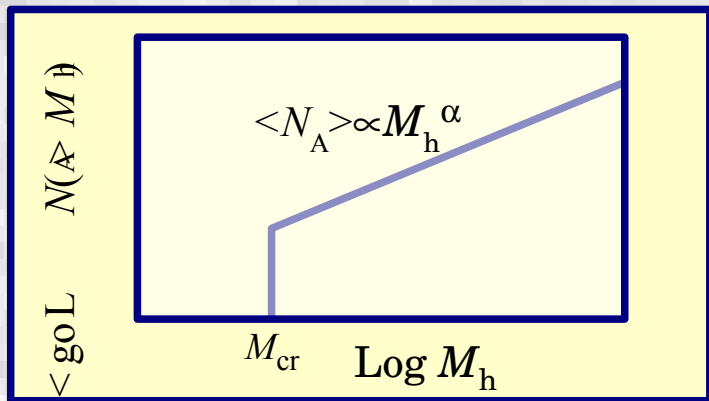
The 1-halo term is from AGN-LRG pairs in the **same DMH**.

- LRGs are in  $M_h > \sim 10^{13.5} M_{\text{sol}}$  halos.
- The 1-halo term measures AGNs in  $M_h > \sim 10^{13.5} M_{\text{sol}}$  halos.

The 2-halo term  $\propto b_A b_{\text{LRG}}$ .

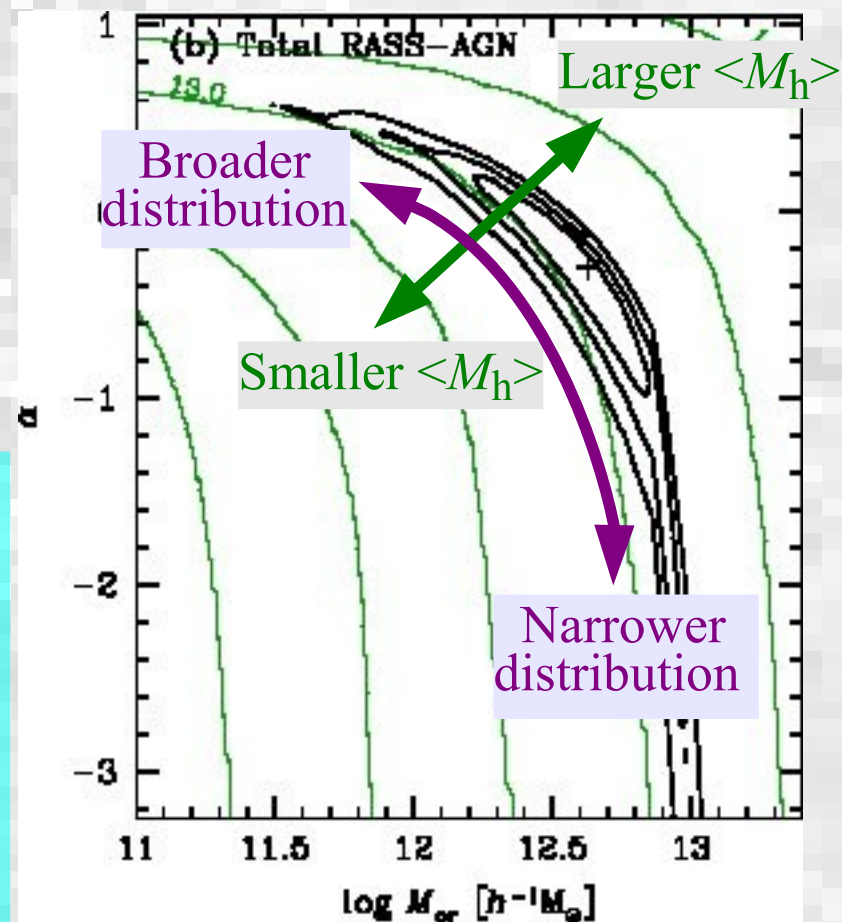
- Determines AGN bias  $b_A$
- Indicates the mean DMH mass with AGNs.

# Constraints on HODs for AGNs

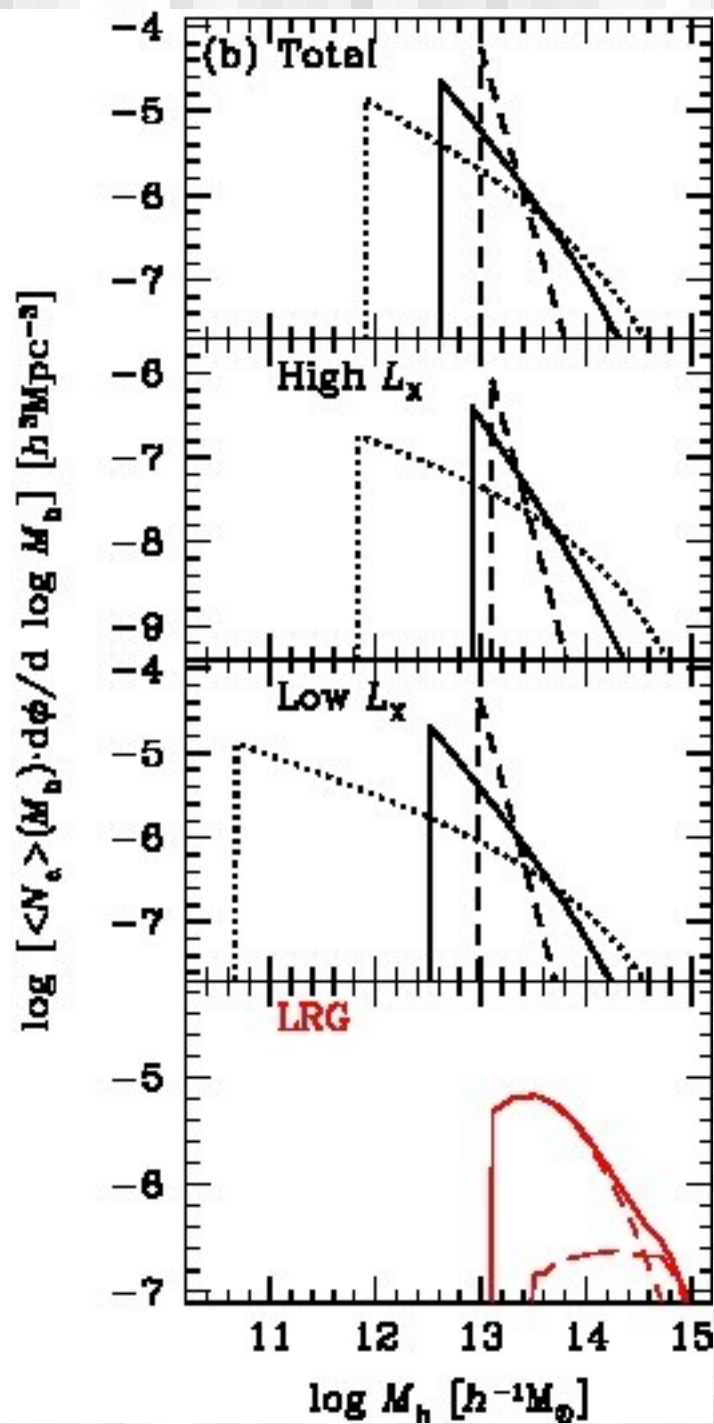
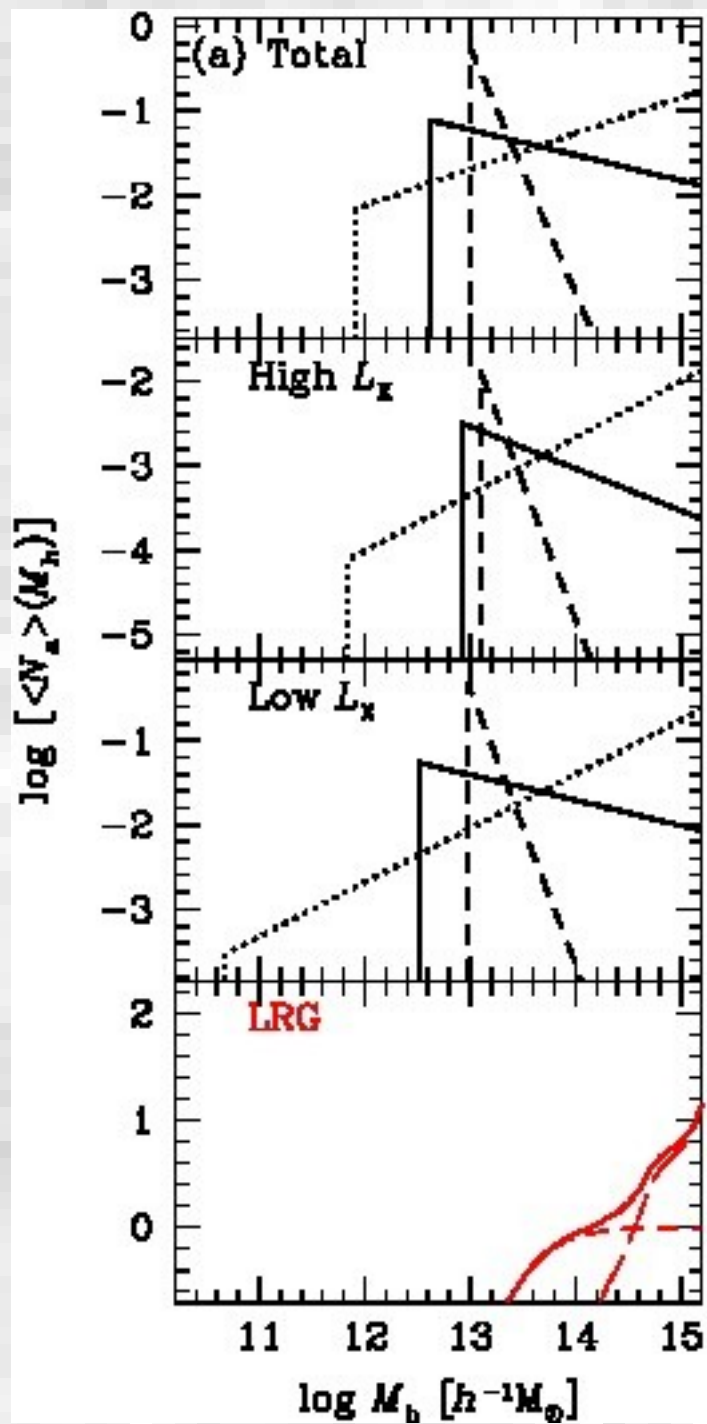


Simple HOD model for AGNs

- Constraints roughly along  $\langle M_h \rangle \sim \text{const.}$ 
  - ★ Constraint from the 2-halo term ( $b_X$ )
- $\alpha < 0.4$  ( $\Delta\chi^2 < 2.3$  limit)
  - ★ Constraint from the 1-halo term



- Confidence contours (black,  $\Delta\chi^2=1;2.3;4.6$ )
- Mean DMH mass (green contours).



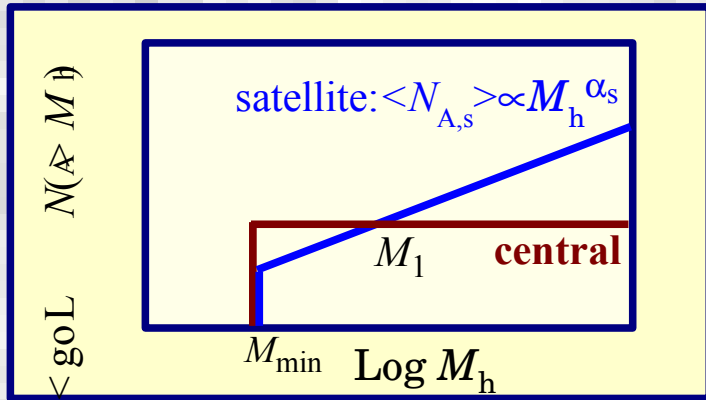
Left:  
number per halo.

Right:  
Number density

Three possible  
HODs within  
errors.

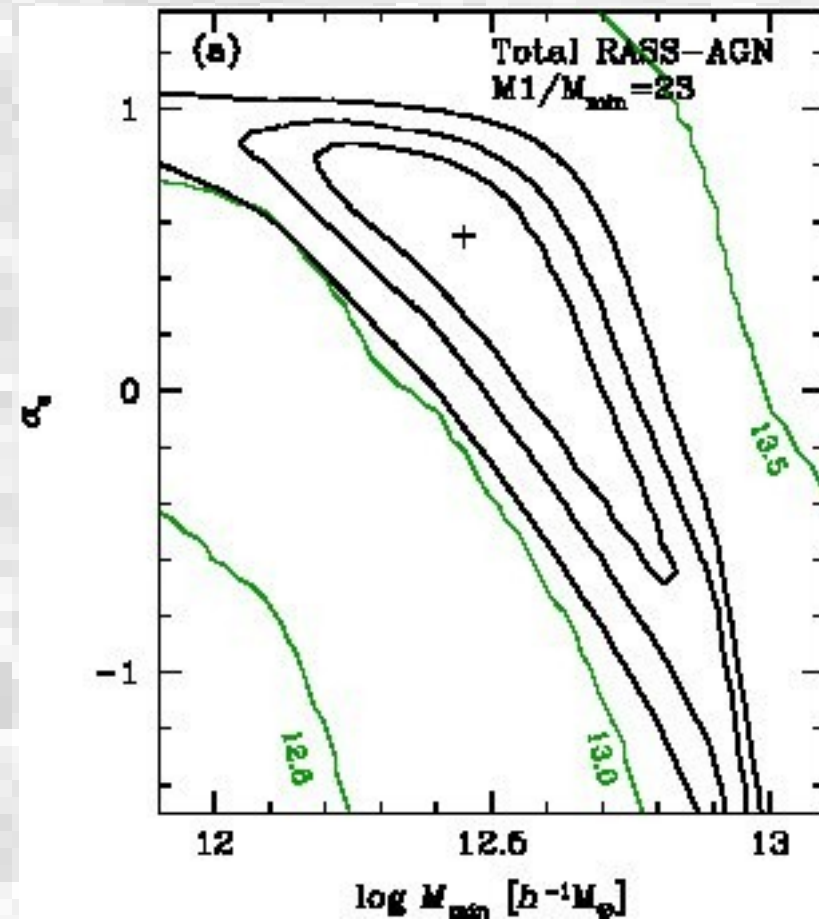
TM+2011

# Model with separate central+satellite AGNs



Model B:  
A model with galaxy-like central+satellite components

cf. SDSS Galaxies  
(e.g. Zehavi et al. 2005)  
 $M_1/M_{\min} \approx 23$ ,  $\alpha \approx 1.2$

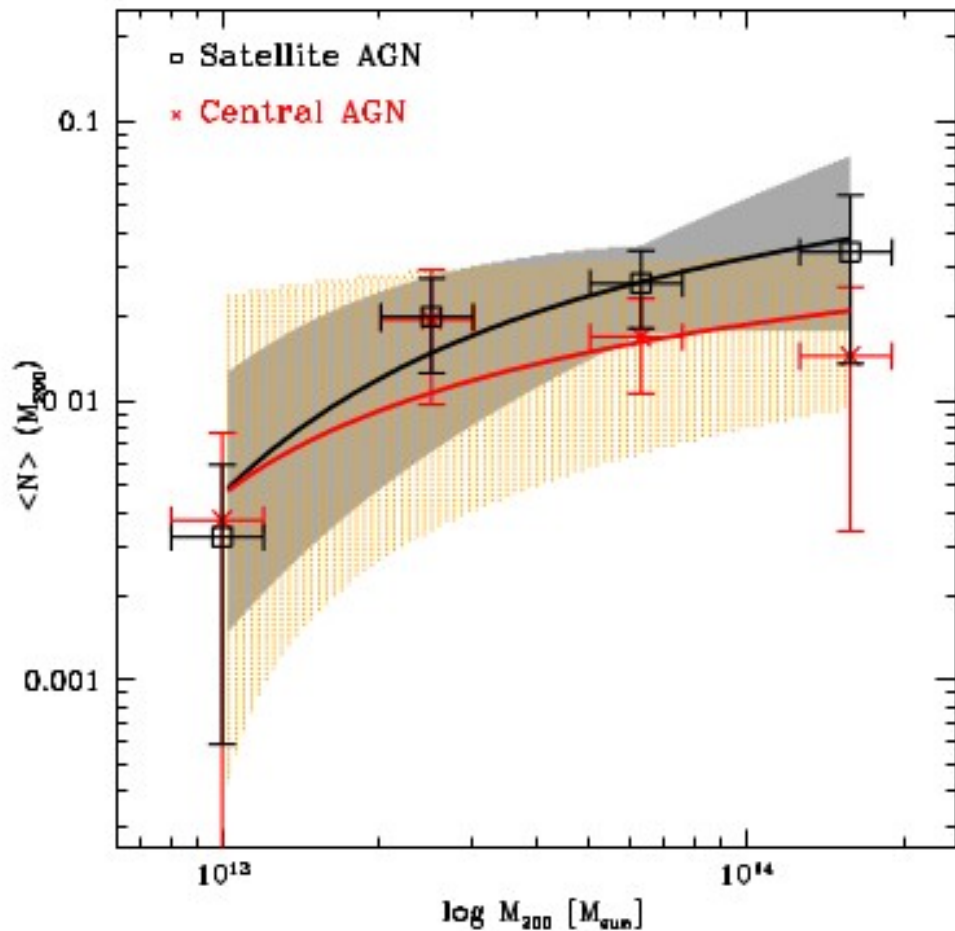


# Implication of the HOD Analysis

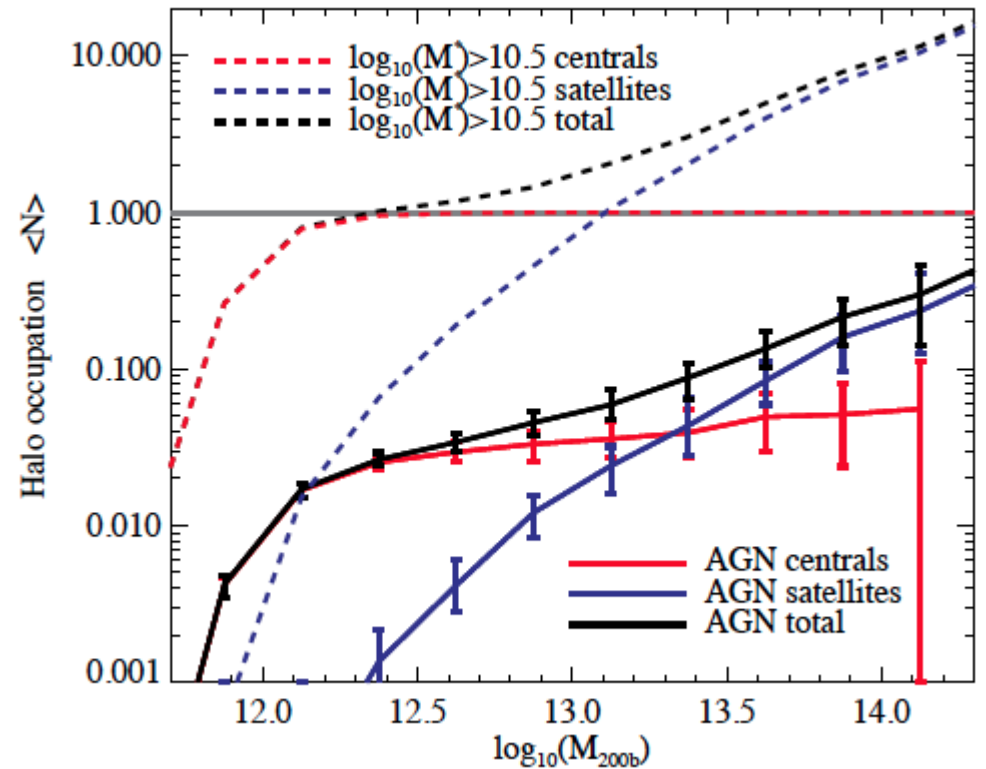
- The limit on  $\alpha_s < 1$  means that the number of (satellite) AGNs/Halo ***grows slower than  $M_h$*** .
  - ★ The HOD of satellite **galaxies** show  $\alpha \sim 1$ , i.e., number/halo  $\propto M_h$  (e.g. Zehavi et al. 2010).
  - ★ **AGN fraction** (non-center) **decreases with  $M_h$** .
  - ★ Long-suggested anti-correlation of emission-line AGN fraction and cluster richness (e.g. Gisler 1978; Dressler et al. 1985).
  - ★ Consistent with: AGN fraction anti-correlates with the velocity dispersion of clusters/groups ( Popesso & Biviano 2006).
  - ★ X-ray AGN fraction is smaller in clusters ( $M_h > 10^{14} M_{\text{sol}}$ ) than the field at low  $z$ . Higher at high  $z$  ( $z > \sim 1.5$ ), this trend reverses (Martini+13).



# Trend Verified in direct counts/Weak lensing-based HOD studies



Allevato+12, direct count  
 Satellite HOD slope  $\alpha_s < 0.63$



Leauthaud+2014, A. Coil's Talk

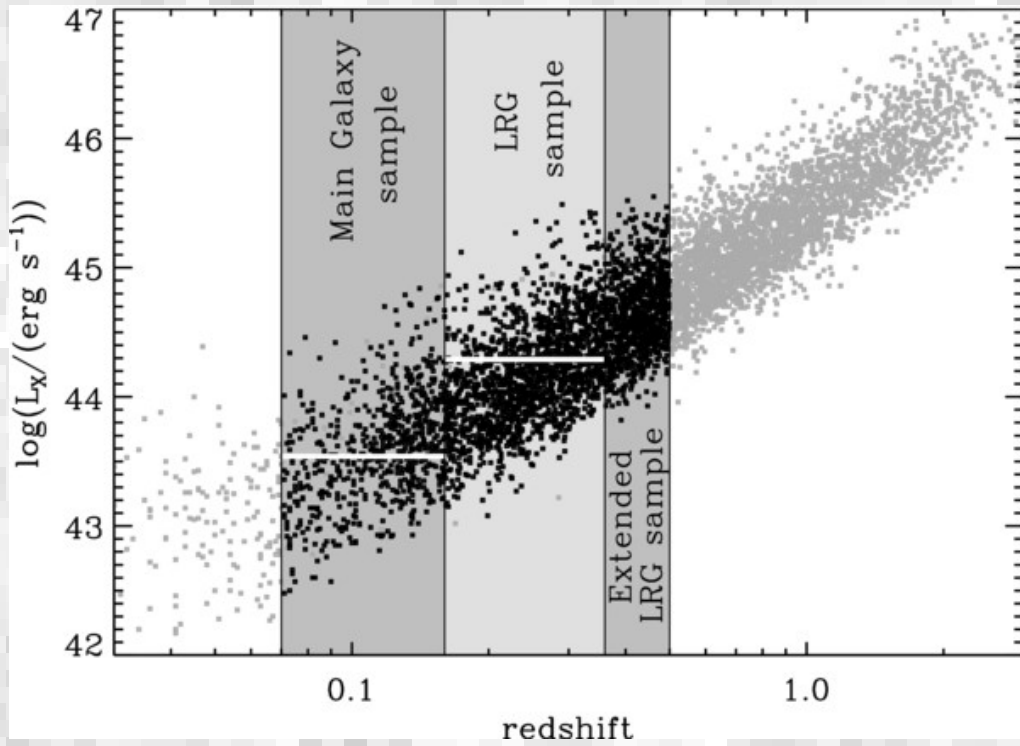
# Implications -cont'd

- Possible mechanisms:

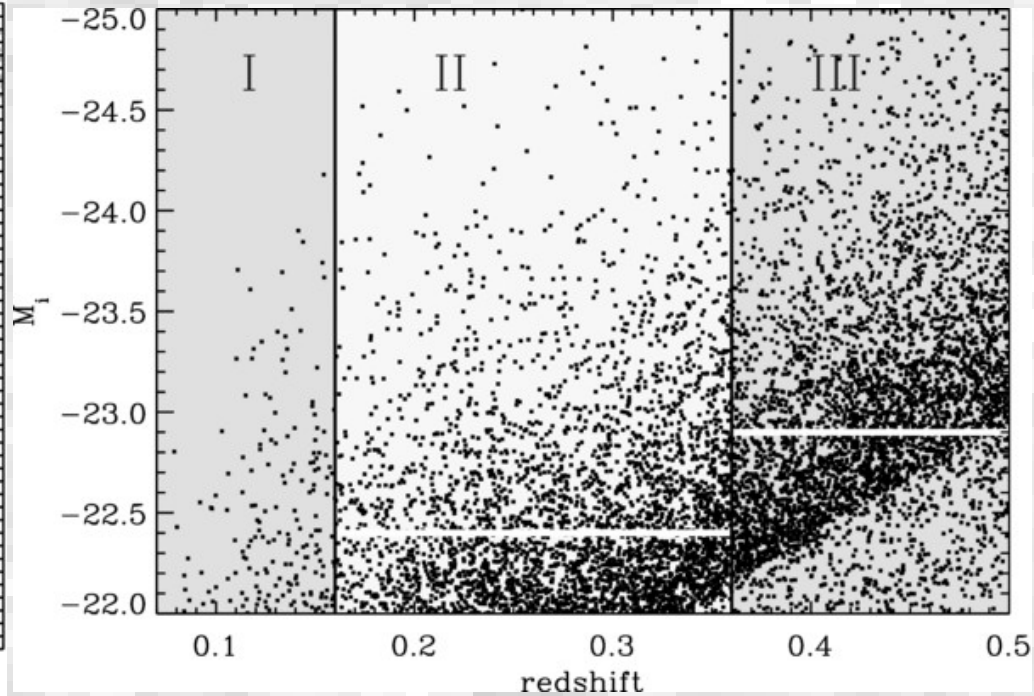
- ★ Merging efficiency low in high velocity encounters (Makino & Hut 1997).
- ★ Would AGN triggering by major merger/minor merger of **sub-halos** inside larger host halos explain the HOD behavior (Altamirano's talk)?
- ★ Ram pressure stripping/thermalevaporation of cold gas in galaxies in Intracluster/intragroup medium (Gunn & Gott 1972; Cowie & Songaila 1977).



# Extended sample



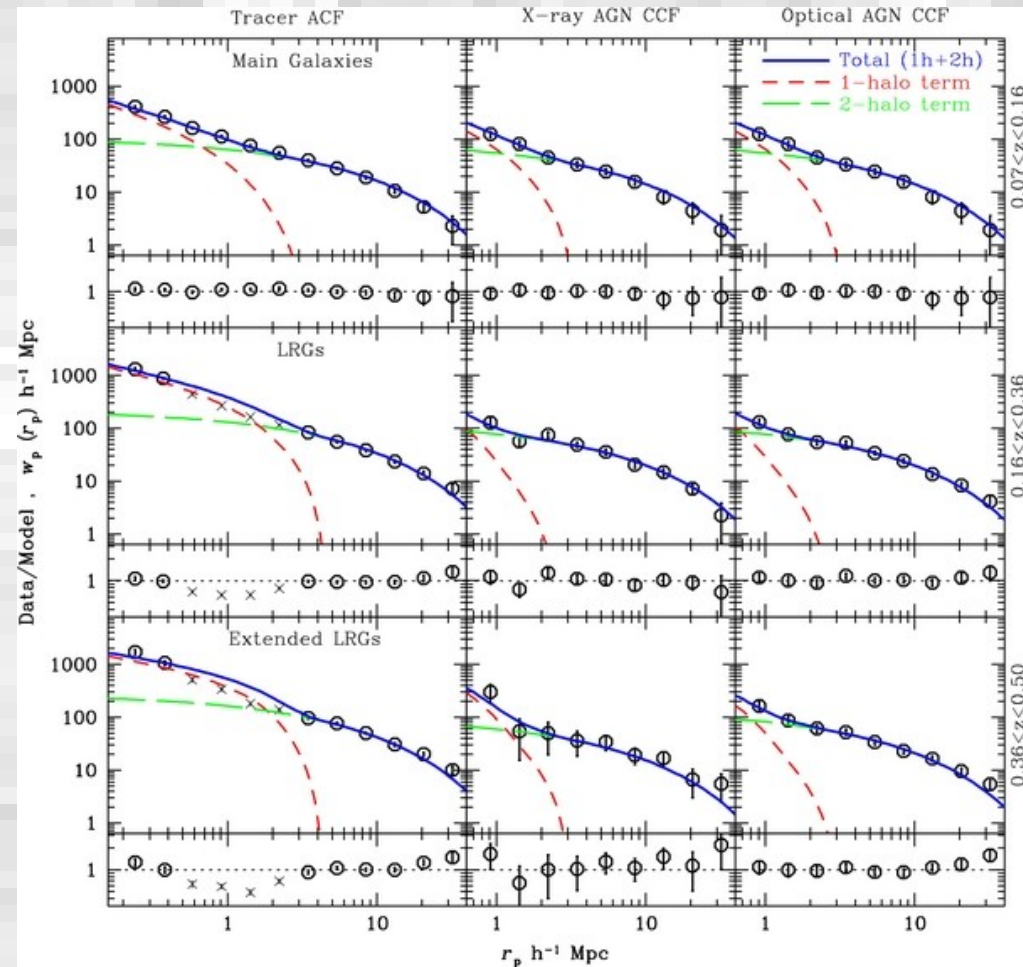
RASS-AGNs extended



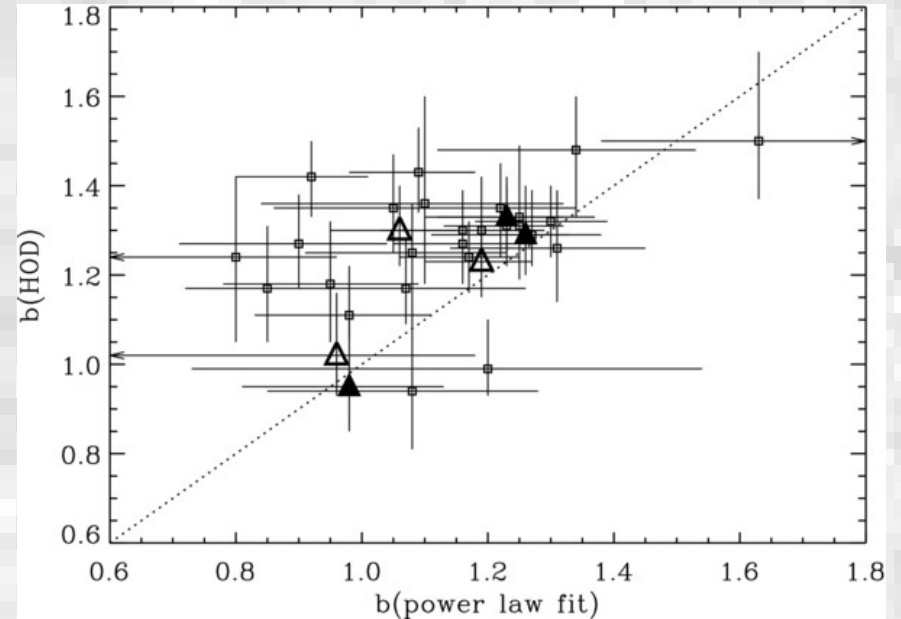
Schneider et al. 2010, Optically-selected Broad-line AGN sample

Paper III: Krumpe, TM, Coil Aceves 2012

# HOD approach may be simply used for more accurate determination of linear bias parameters



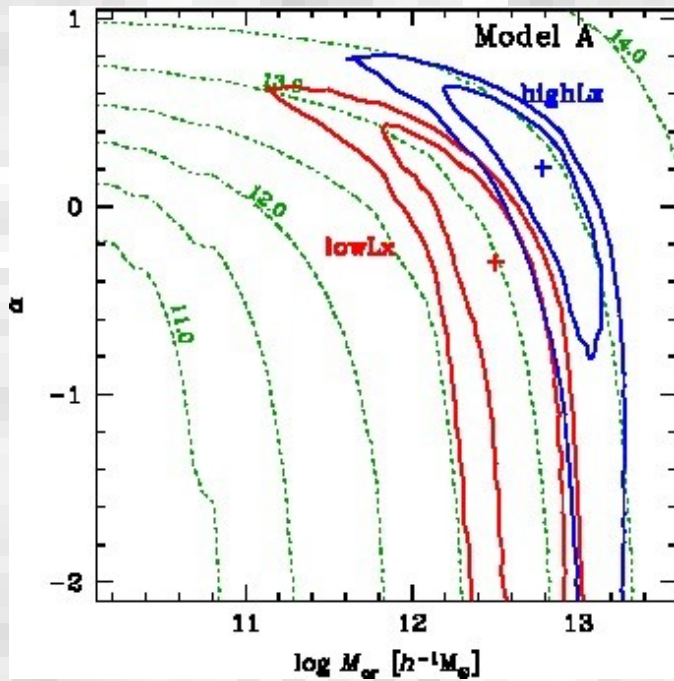
Figs: Krumpel, TM et al. (2012)



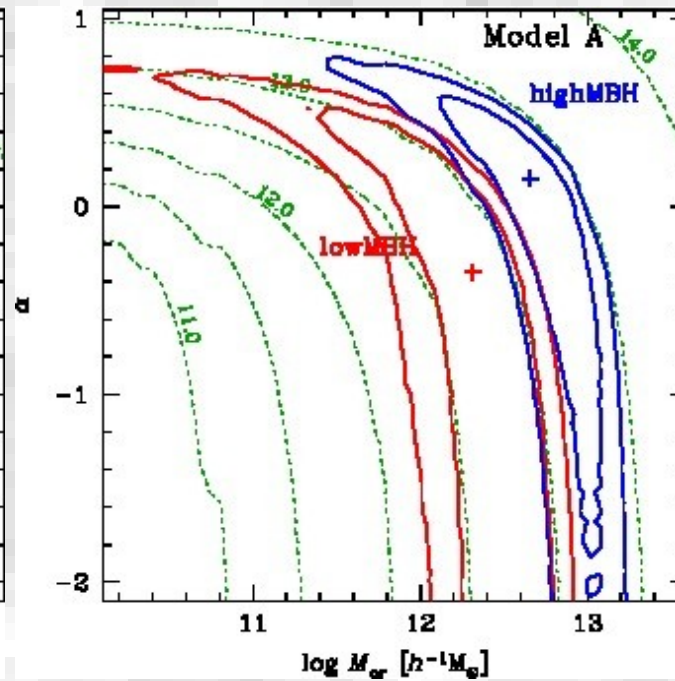
- More accurate determination of  $b_{\text{lin}}$  than power-law fits.
- Fitting 2-halo term only to  $r_p > 1.5 h^{-1} \text{Mpc}$  (Allevalo et al. 2011, 2012)
- Fitting 1 and 2-halo terms with a simple parameterized HOD model to obtain constraints on  $b$  and  $\log \langle Mh \rangle$  (Krumpel, TM et al. 2012, 2014).

# Highlight differences between $L_x$ , $M_{BH}$ , & $L/L_{edd}$ divided samples

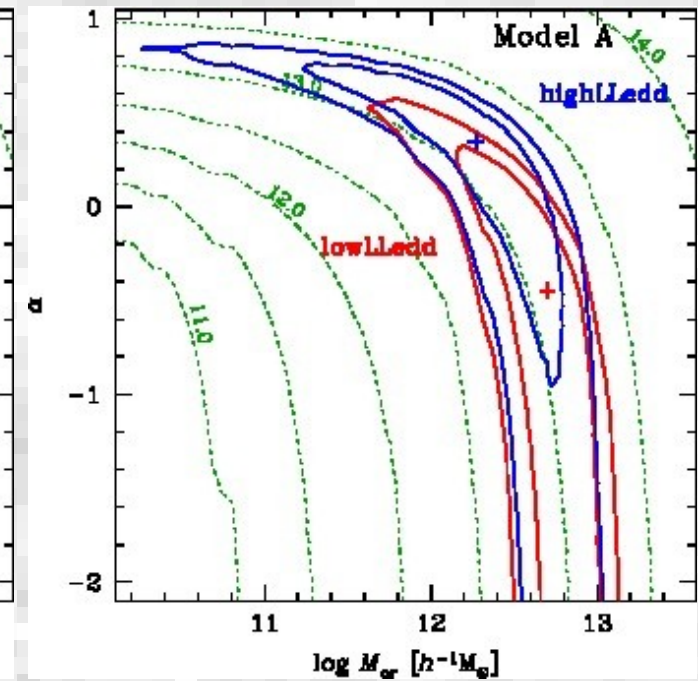
High vs low  $L_x$



High vs low  $M_{BH}$



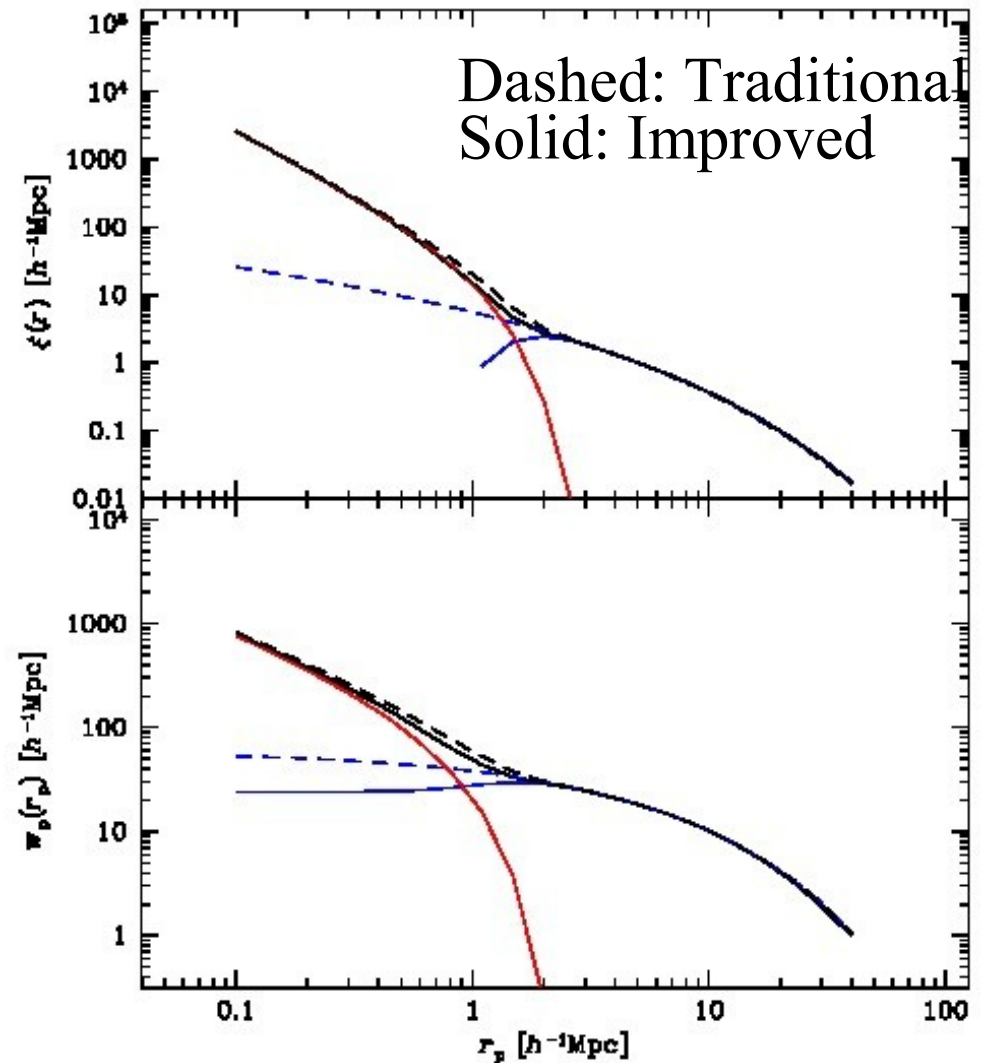
High vs low  $L/L_{edd}$



Comparing biases only use data at 2-h terms  
This approach takes advantage of data at all scales.

# Two-halo term improvements

- Instead of simple linear PS, use non-linear PS, scale-dependent bias, and exclusion of pairs that should be counted in the 2-halo term (Zheng+'04; Tinker+'05; van den Bosch+'13)



# Limitations

- Good sampling at 2-halo term ( $r_p > \sim 1$  Mpc)
  - Good constraint on only one parameter: linear bias
- Poor sampling at 1-halo term ( $r_p < \sim 1$  Mpc)
  - Poor constraint on the distribution of  $N(M_h)$
  - CCF approach helps
- Degeneracy in the interpretation of the 1-halo term.
  - Central vs satellite pair or satellite-satellite pair?
- Do satellite AGNs follow DM profile?
  - The same problem with galaxy HOD studies, especially comparing blue vs red galaxy HODs.

# Direct counts within resolved groups/clusters?

- QSO counts within rich clusters of galaxies (Martini et al. 2009;2013)
- DMHs with  $M_h > \sim 13 h^{-1} M_\odot$  can be cataloged as groups/clusters (e.g. X-ray selected).
  - Direct counts of AGNs in these groups/clusters are possible.
  - Combine with the CFs involving AGNs that do not belong to these groups/clusters give constraints on the minimum halo mass occupied by these HODs -> Alleinato+12, **(Talk by A. Finoguenov)**
- SDSS QSOs in clusters ( $M_h > \sim 14 h^{-1} M_\odot$ )  
**(Talk by M. Nguyen)**



# Conclusions

- The HOD analysis is a strong tool to interpret correlation functions of galaxies/AGNs to scale over linear to non-linear scales.
- From HOD analysis, we can obtain not only a single “typical” host DMH mass but also constraints on how AGNs distribute among DMHs as a function of mass.
- Applying the HOD analysis to  $z \sim 0.3$  SDSS LRG vs RASS AGNs, we find that solutions where AGN fraction among satellite galaxies decrease with Halo mass.
- The interpretation of the HOD analysis is limited by poor sampling at small scales (especially of AGNs) and model degeneracies.
- If we have good catalog of resolved clusters/groups, direct count of AGNs in these clusters/groups can give robust HOD measures.