

# The Role of Episodic Accretion in Low-Mass Star Formation

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Very Low Mass Stars and Brown Dwarfs  
October 14, 2011

Offner & McKee, 2011

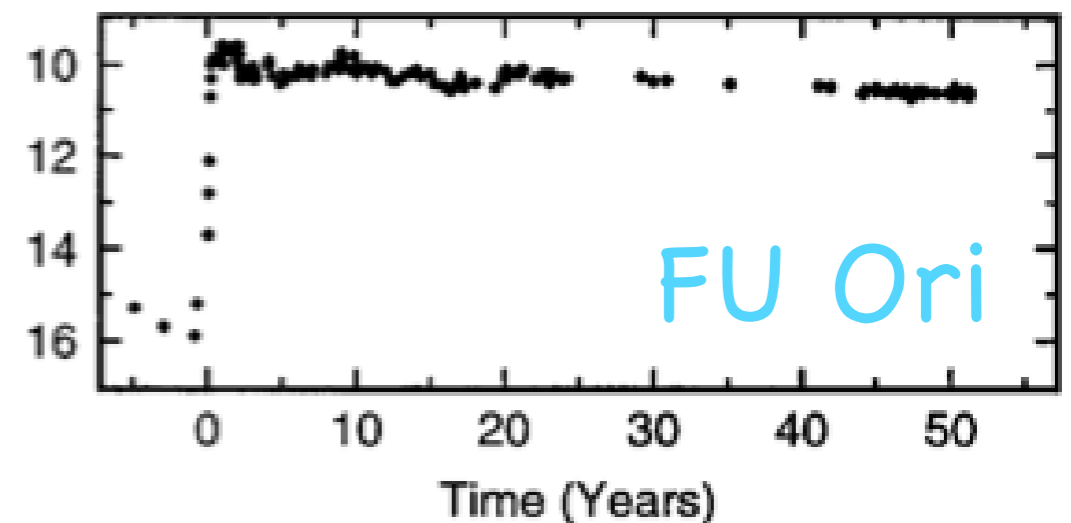
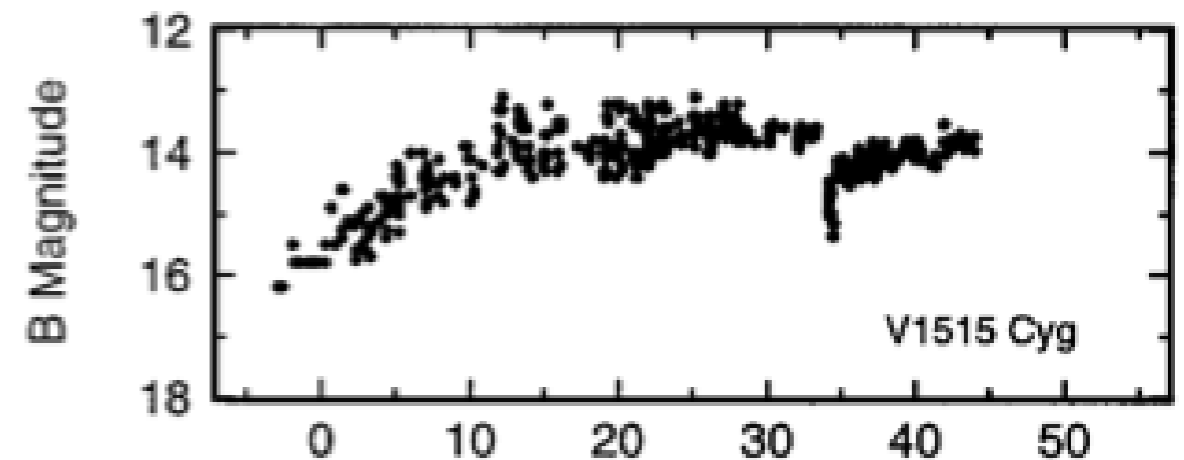
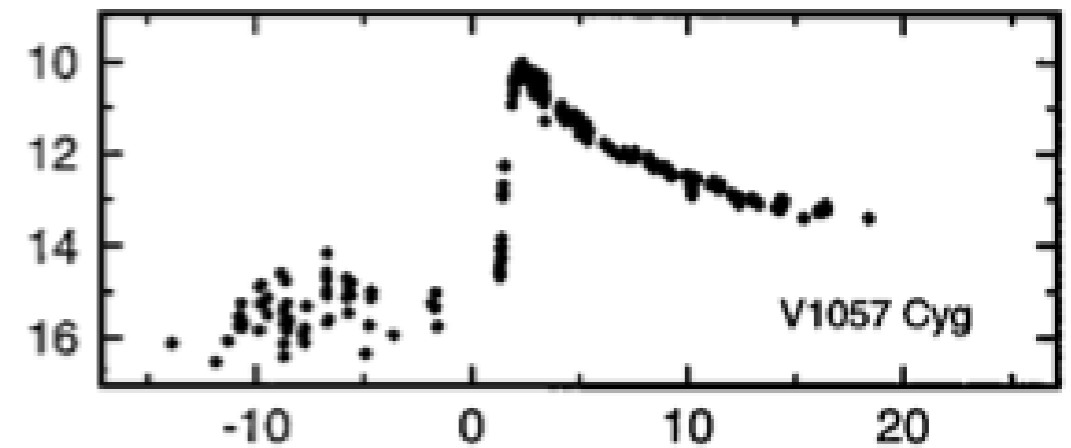
Hosokawa, Offner & Krumholz, 2011



# Definition

Kenyon & Hartmann 96

- $\geq 4$  orders of magnitude in B magnitude ( $100 \times L^*$ )
- Absorption lines in optical spectra
- IR Excess (Class I/II protostars)
- Reflection Nebulae
- $\Delta t = 10s$  years



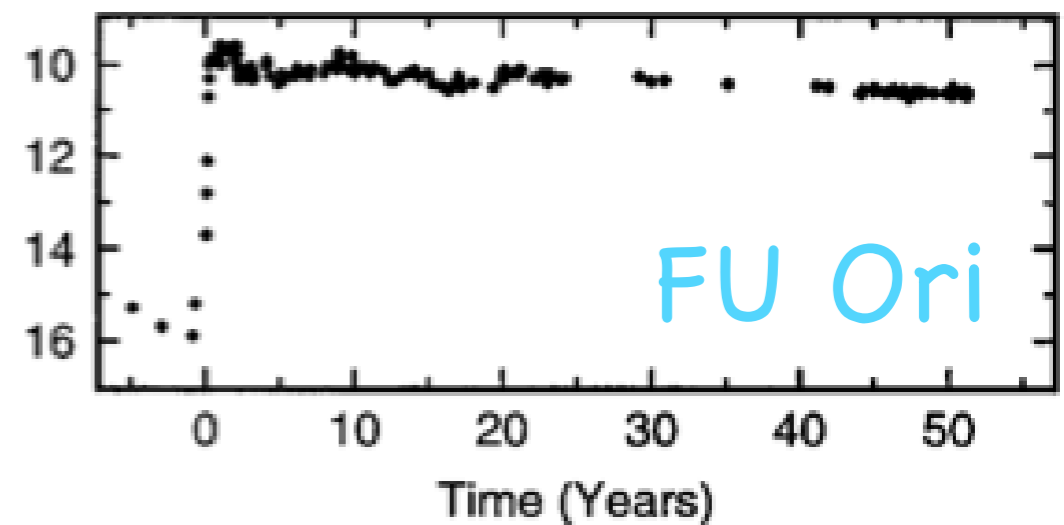
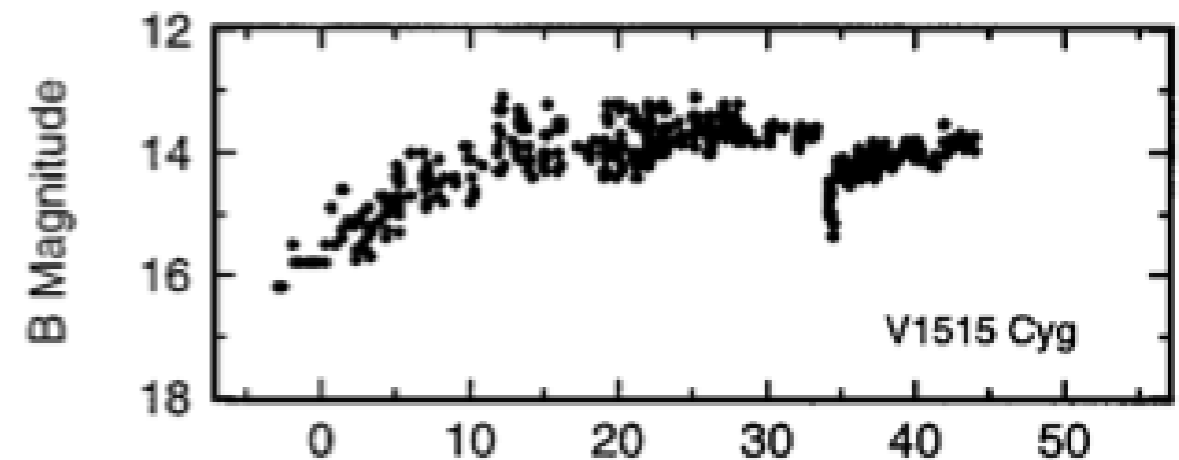
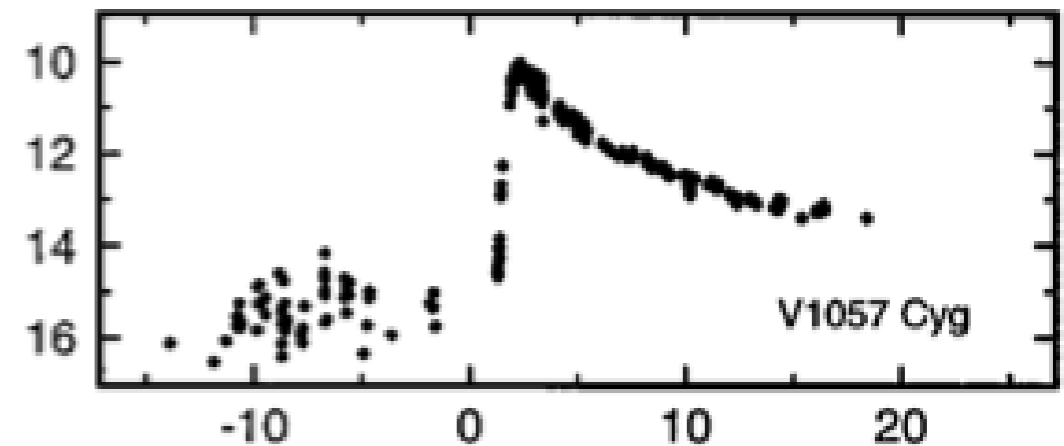


# Definition

Kenyon & Hartmann 96

☉  $\Delta L = 20-220 L_{\text{sun}}$

$$L_{\text{acc}} = f_{\text{acc}} \left( \frac{G m \dot{m}}{r_*} \right)$$





# Burst Origin

Offner et al. 2009, 2010

- Thermal Instability  
(Bell & Lin 94)
- Binary Interactions  
(Reipurth & Clarke 01,  
Bonnell & Bastian 92)
- Gravitational  
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(Vorobyov & Basu 2005+,  
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- MRI + GI  
(Armitage ea 2001, Zhu  
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100 AU



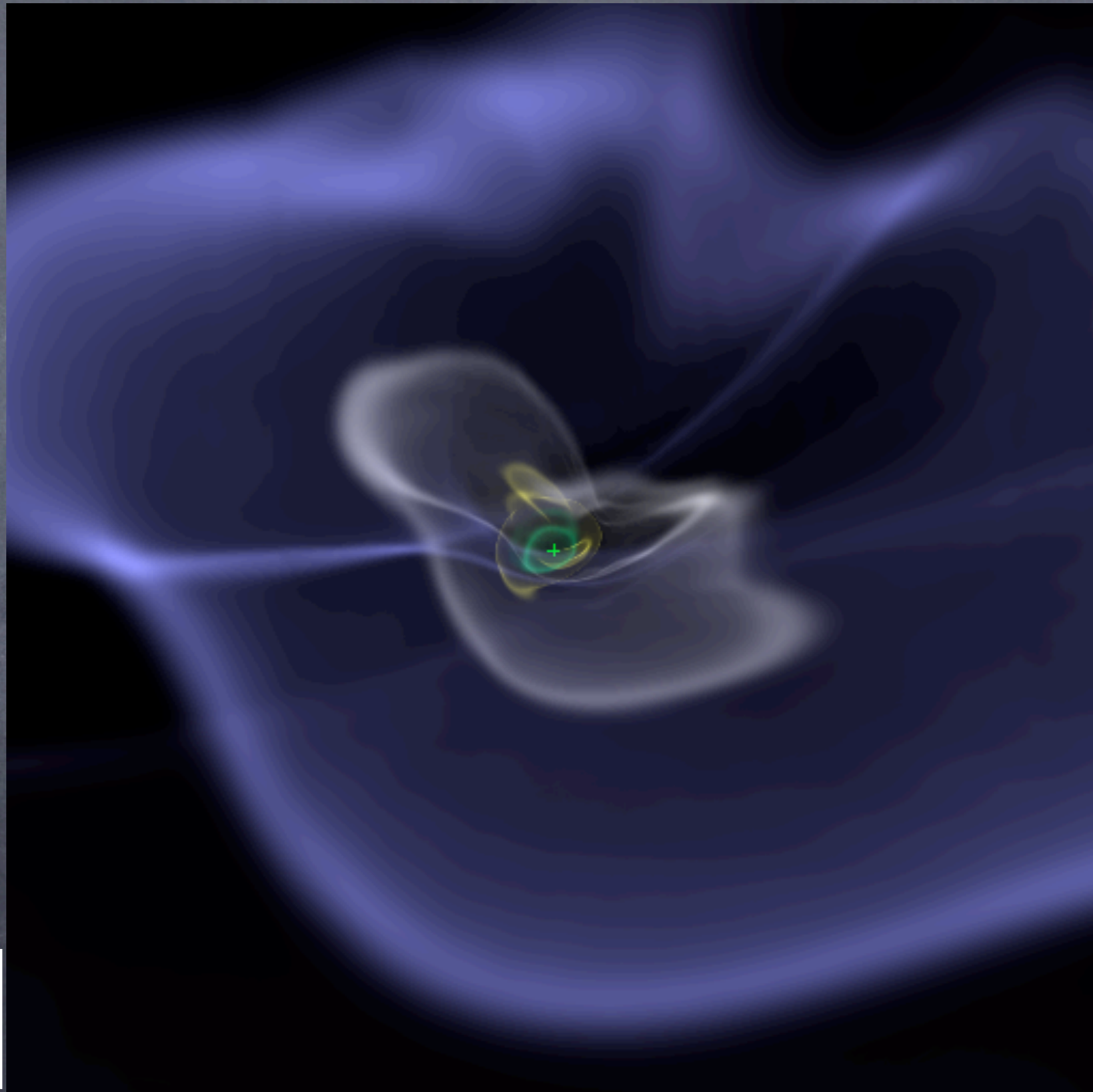


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# Estimations: Fraction of Mass Accreted

- $N_p = \#$  of bursting sources = 20  
(observed in last 70 years)
- $\dot{N}^* =$  Star Formation Rate = 0.016 \*/yr
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1/4 of Mass



# Estimations: Fraction of Lifetime

- $\langle t_f \rangle$  = Mean protostellar lifetime = 0.1-1 Myr  
(Evans et al. 2009:  $\langle t_f \rangle = 0.44$  Myr for Class 0 +  
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$$\frac{\Delta t_{\text{high}}}{\langle t_f \rangle} = \frac{1200 \text{ yr}}{10^5 - 10^6 \text{ yr}} \simeq 0.01 - 0.001$$



Can Episodic Accretion  
Solve Open Problems in  
Star formation ??



# (Embarrassing) Problem # 1: Luminosity Problem (I)

- Protostars are dimmer than star formation models predict (Kenyon et al. 1990)
- $\langle L \rangle_{\text{obs}} \cong 2 L_{\text{sun}}$  for Class 0, I (Enoch et al. 2009)
- Considering only accretion:

$$\langle L_{\text{acc}} \rangle = f_{\text{acc}} \left( \frac{Gm\dot{m}}{r} \right)$$



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$$\begin{aligned} \langle L_{\text{acc}} \rangle &= f_{\text{acc}} \left( \frac{Gm\dot{m}}{r} \right) \\ &\simeq \frac{0.75 \times G \times 0.25M_{\odot} \times 2.5 \times 10^{-6}M_{\odot}/\text{yr}}{2.5R_{\odot}} = 5.9L_{\odot} \end{aligned}$$



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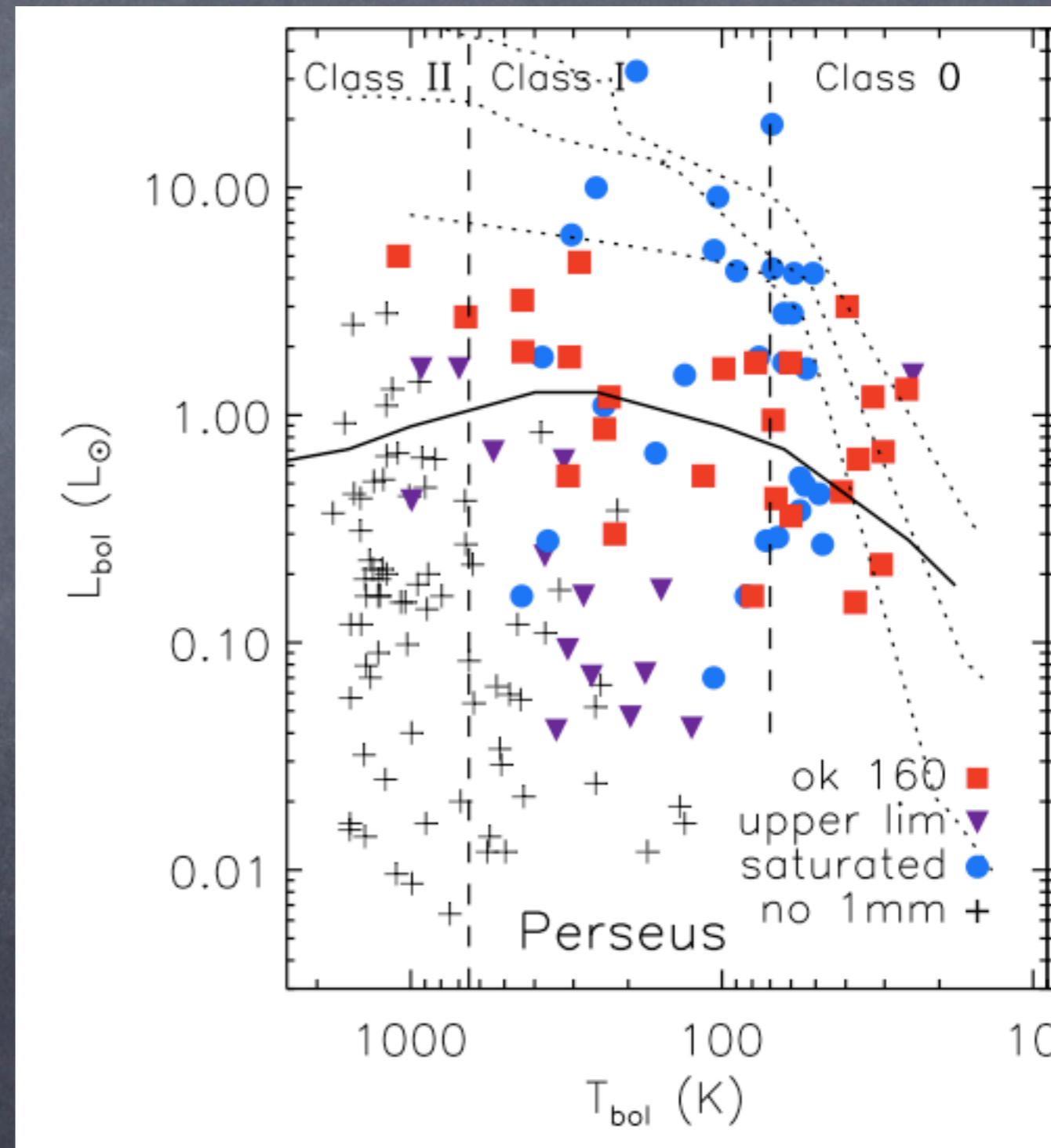
→  $\langle L \rangle_{\text{obs}} \cong 5.3 L_{\text{sun}}$  with extinction correction  
(Evans et al. 2009)



# (Embarrassing) Problem # 1: Luminosity Problem (II)

Enoch et al. 2009

- Luminosities range over 3 orders of magnitude
- There are a large number of low-luminosity protostars





# Protostellar Mass Function (PMF)

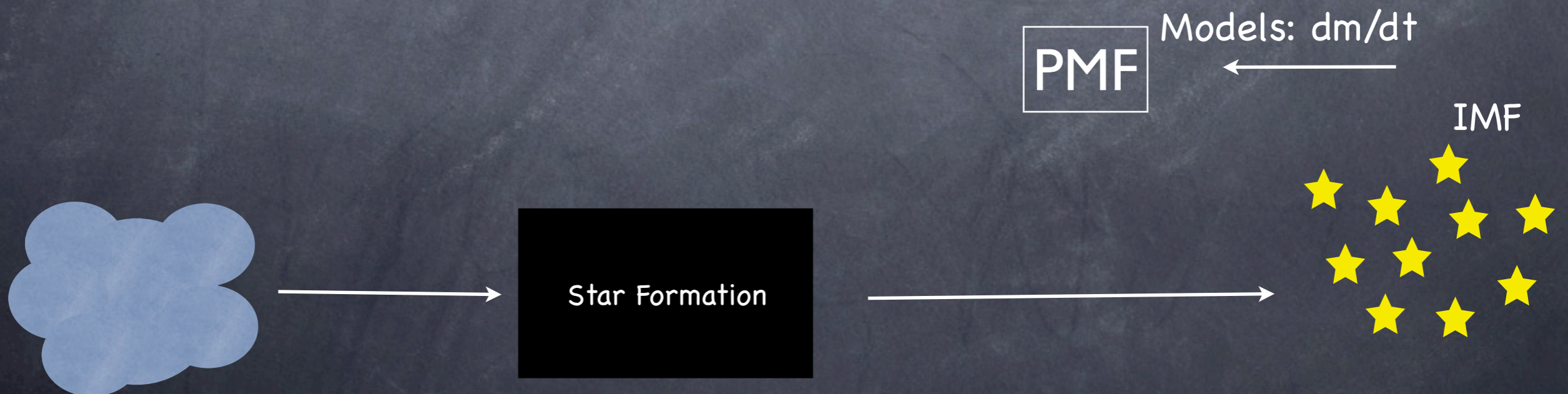
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- ...but the initial mass function of stars (final protostellar masses) is well constrained.





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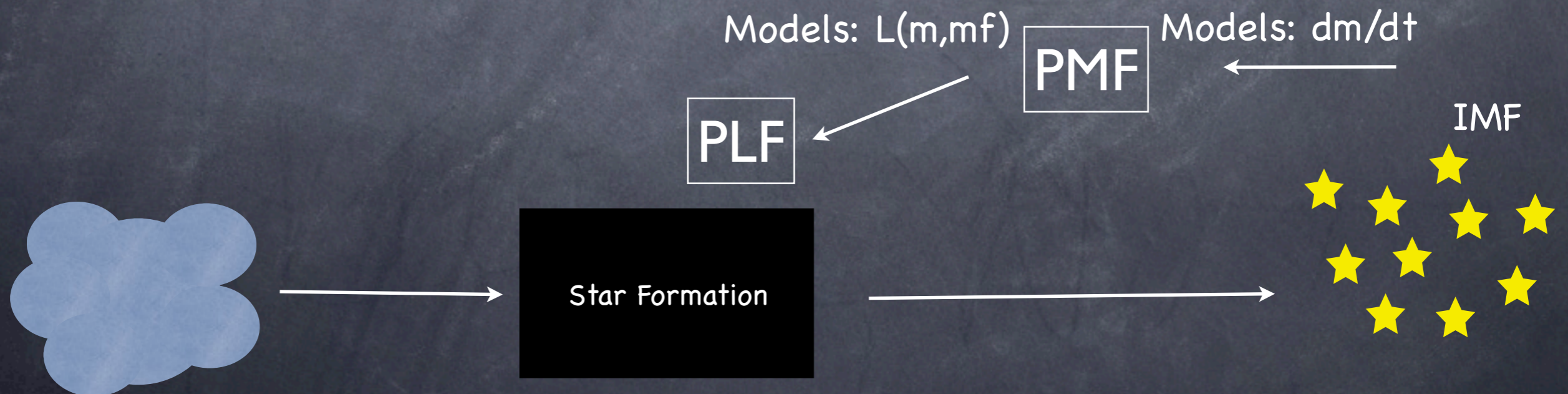
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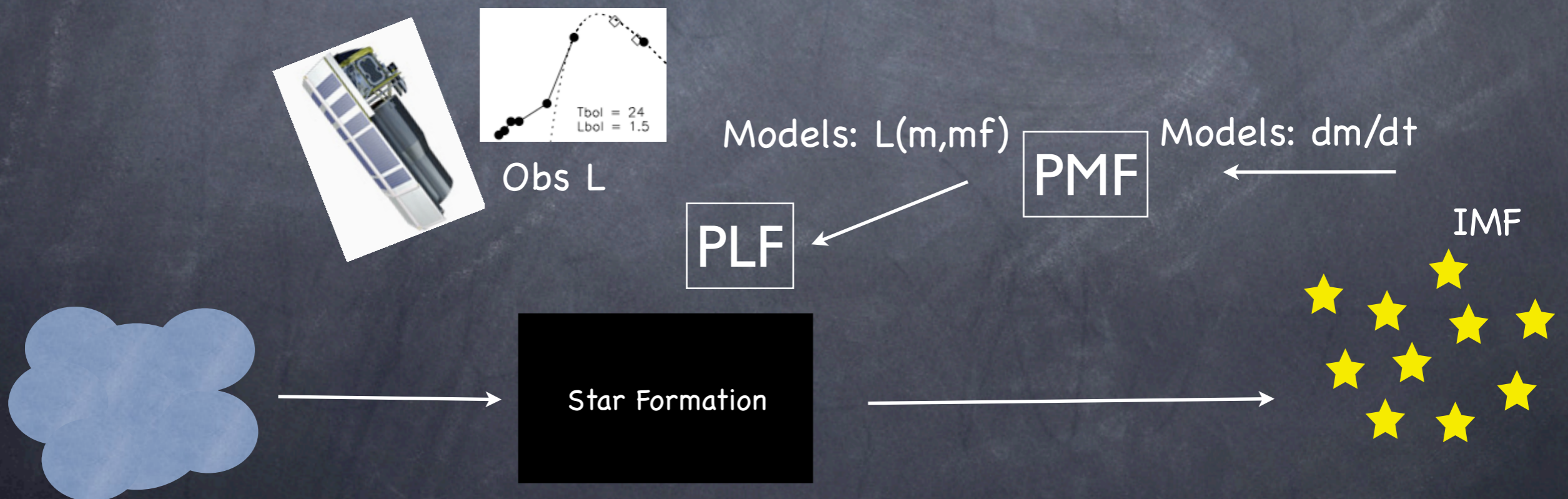
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# Ingredients

- IMF with upper mass cutoff,  $m_u$ :  $\psi_c$  (Chabrier 2005)
- Accretion rate as a function of the instantaneous mass,  $m$ , and final mass,  $m_f$ :  $dm/dt (m, m_f)$
- Formation time as a function of stellar mass:  $t_f (m_f)$
- Fraction of mass accreted in bursts,  $f_{epi}$
- Fraction of accretion energy radiated away,  $f_{acc}$

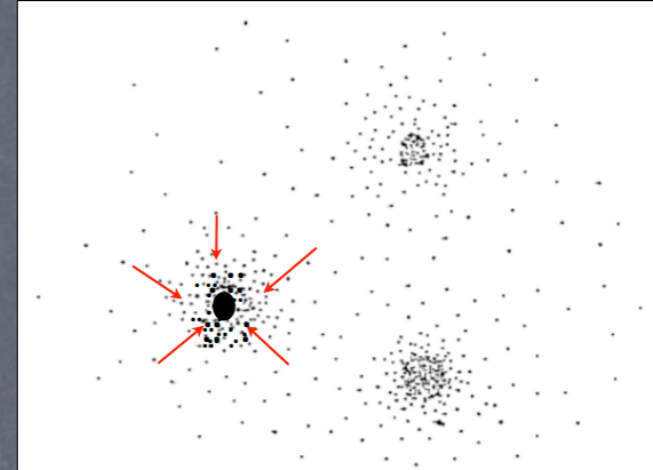


# Star Formation Models

Isothermal Sphere (IS, Shu 1977):

$$\dot{m} = \dot{m}_S \simeq c_s^3/G$$

$$t_f = m_f/\dot{m}_S$$





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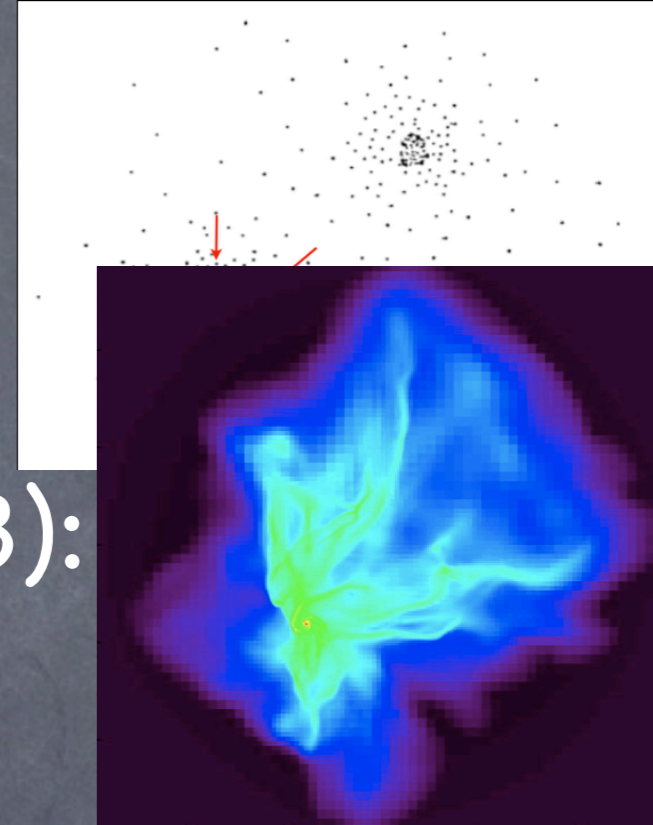
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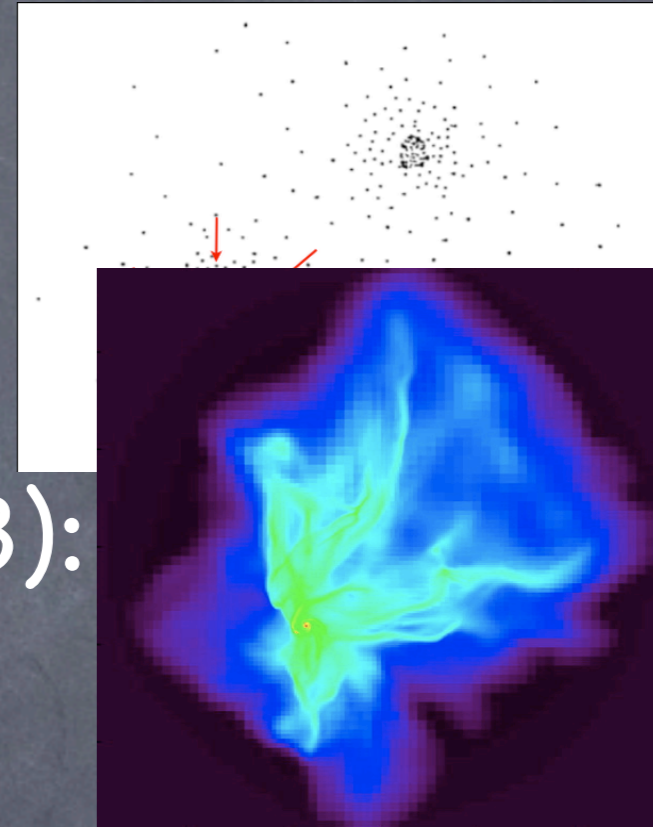
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Two-Component TC (2CTC, McKee & Tan 2003):

$$\dot{m} = (\dot{m}_S^2 + \dot{m}_{TC}^2(m/m_f)^{1/2}m_f^{3/2})^{1/2} \quad t_f = \frac{2m_f}{\dot{m}_S \left[ 1 + \sqrt{1 + (\dot{m}_{TC}/\dot{m}_S)^2 m_f^{3/2}} \right]}$$



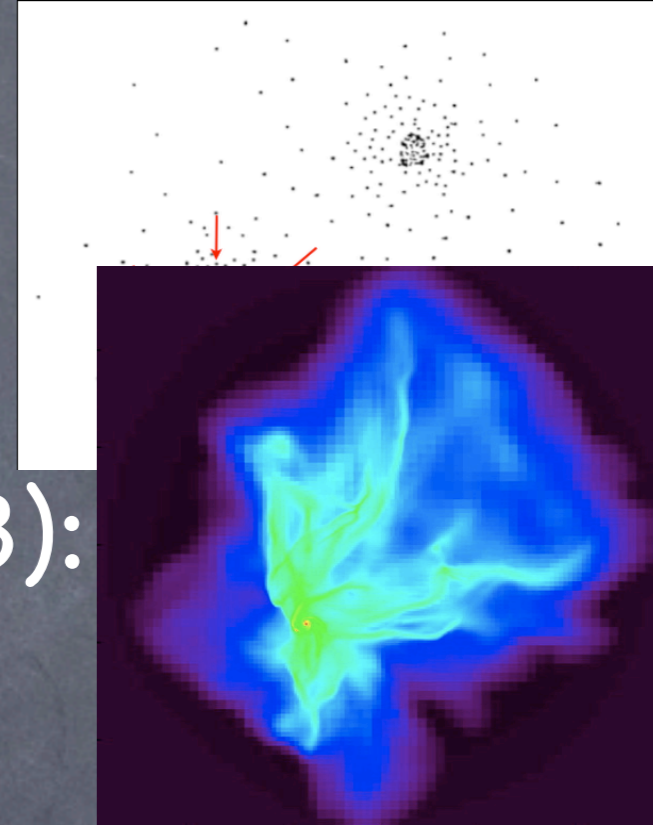


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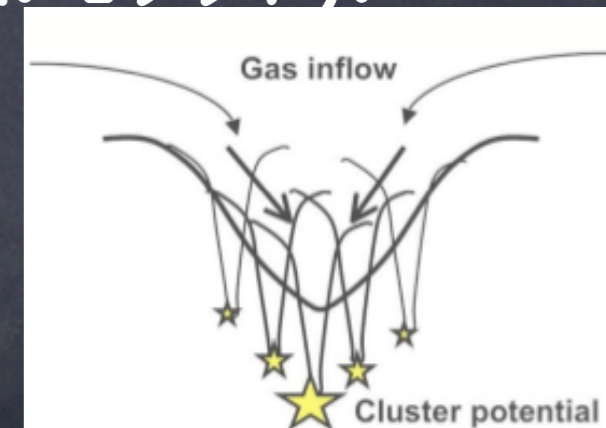
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Competitive Accretion (CA, Bonnell et al. 1997):

$$\dot{m} = \dot{m}_{CA} (m/m_f)^{2/3} m_f$$

$$t_f = t_{ff} \propto \sqrt{\rho}$$

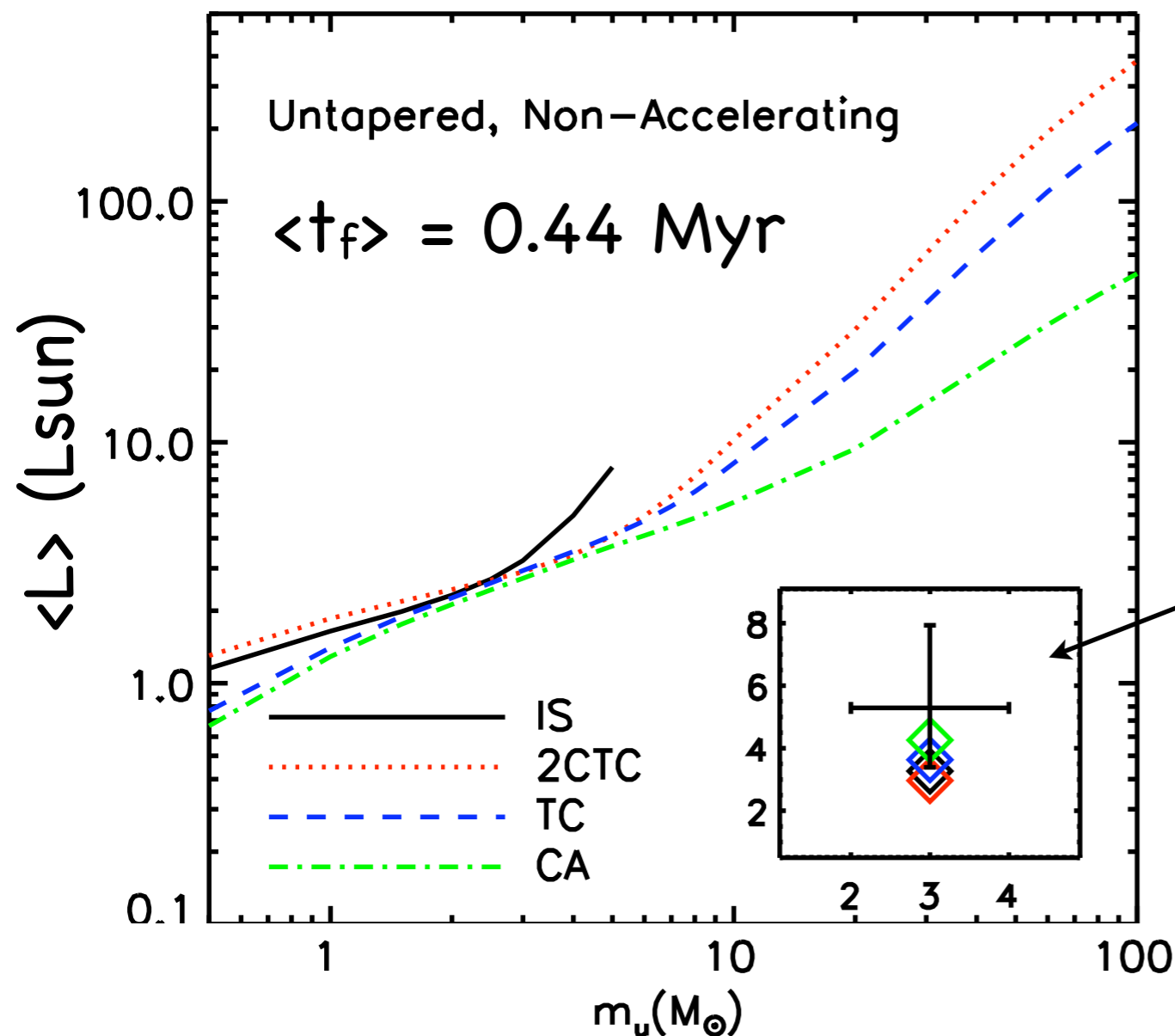




# Mean Protostellar Luminosity

Mean Luminosity:

$$\langle L \rangle_p = \int_{m_l}^{m_u} d \ln m_f \int_0^{m_f} d \ln m L(m, m_f) \psi_{p2}$$



$m_u$  = highest mass star forming in the cluster

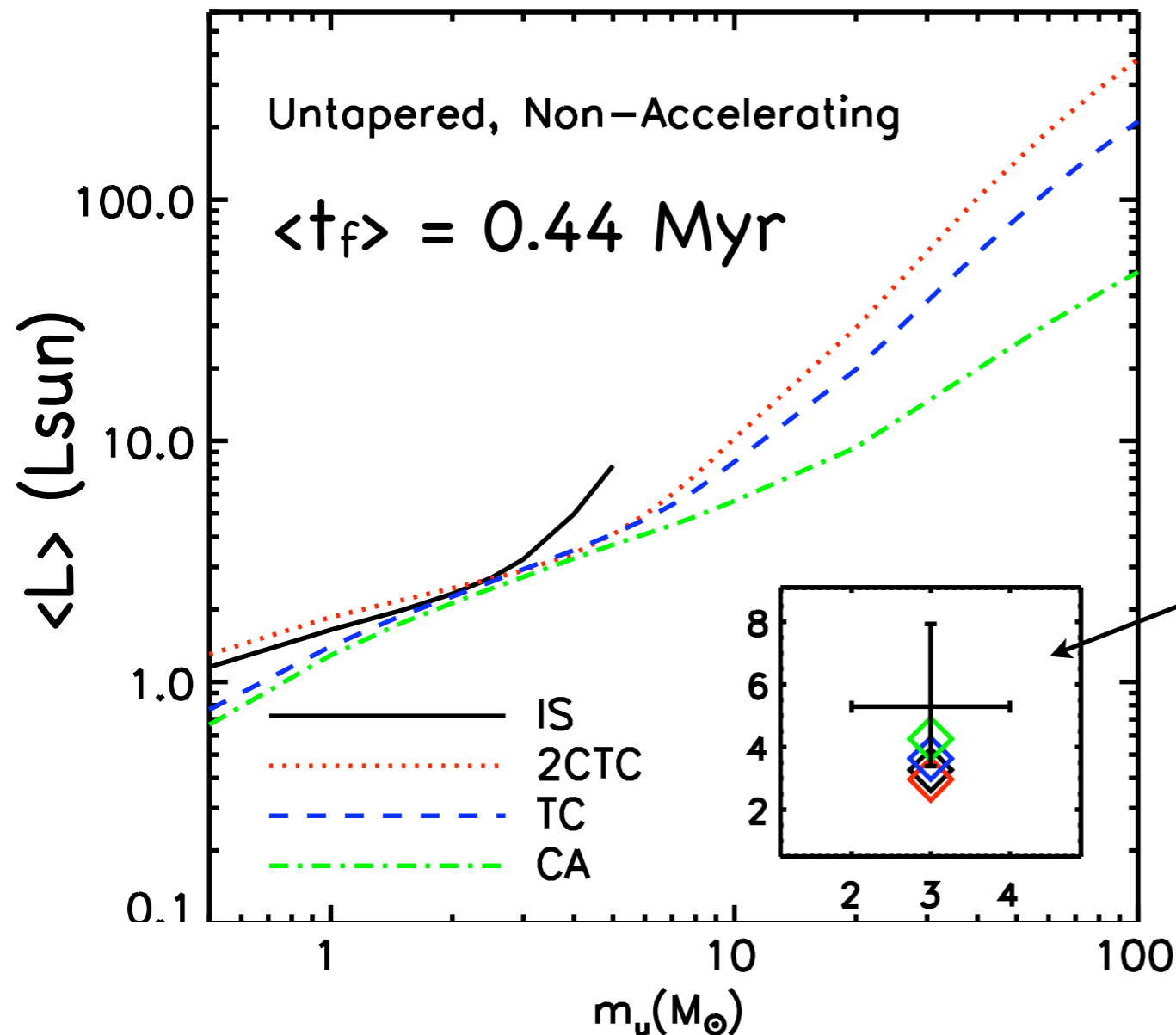
Evans et al. 09



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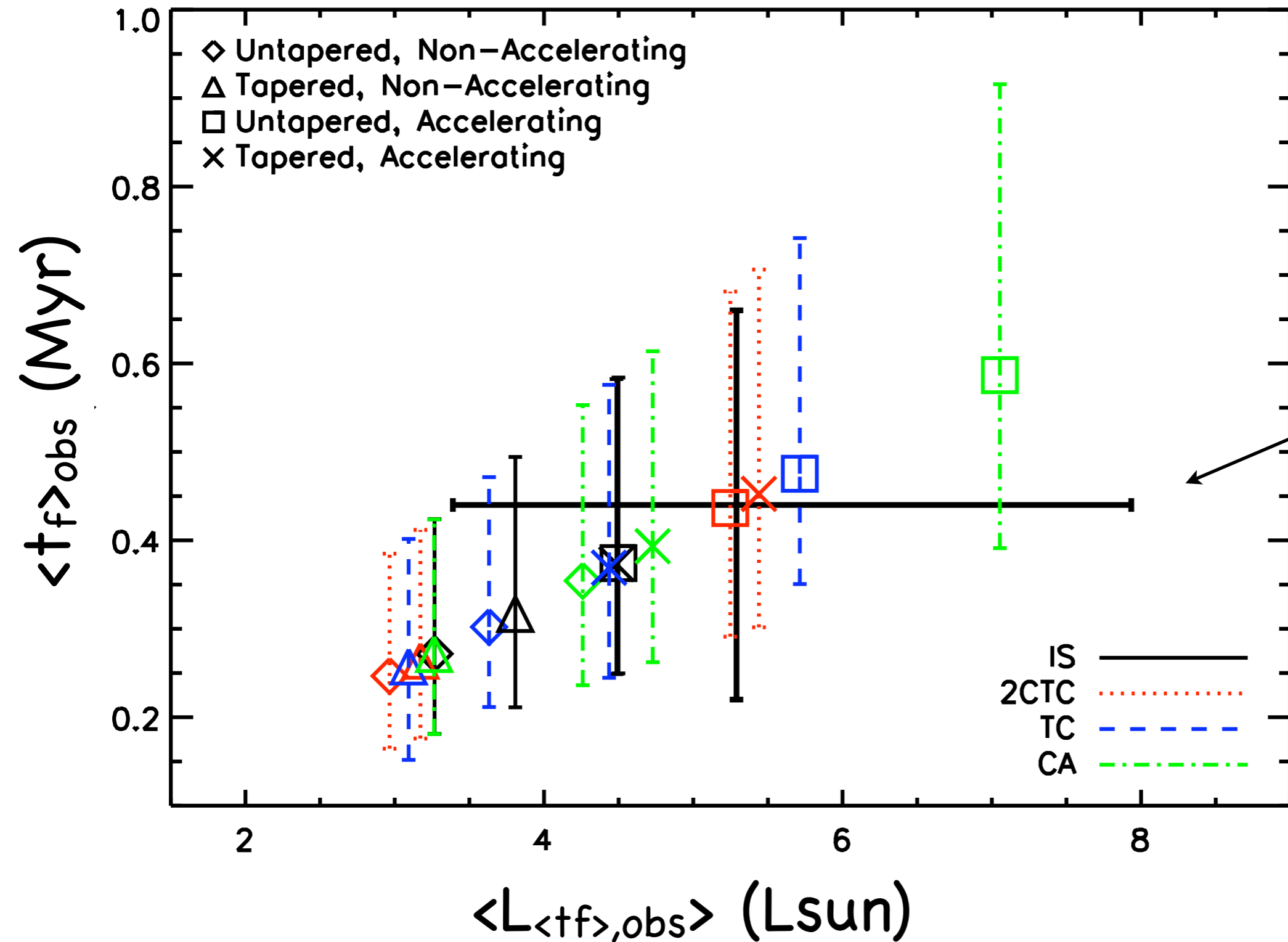
$m_u$  = highest mass star forming in the cluster

Evans et al. 09

Models are too low!



# $\langle t_f \rangle$ vs $\langle L \rangle$



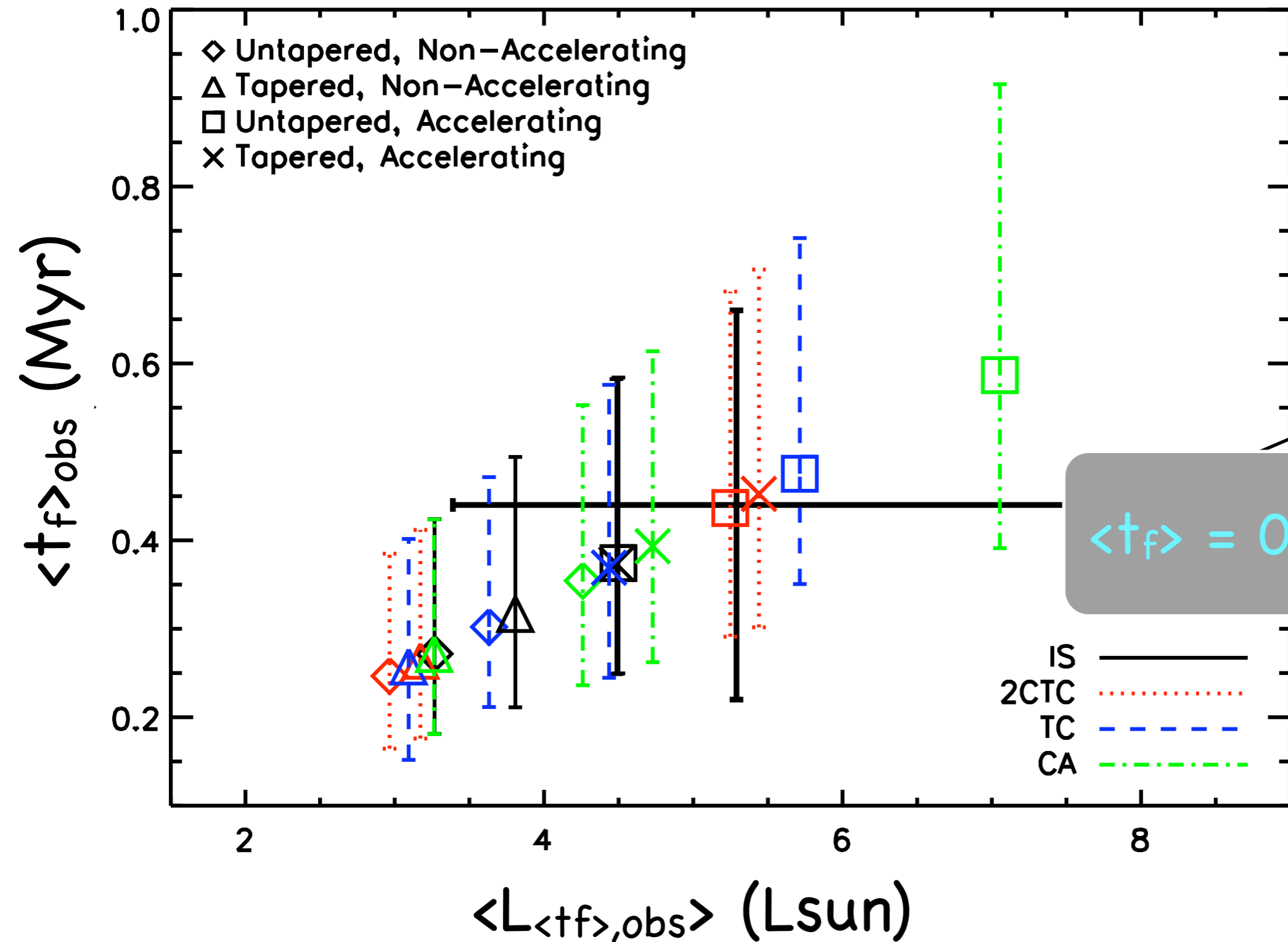
Disk lifetime  
=  $2 \pm 1$  Myr

Evans et al. 09

Offner & McKee  
2011



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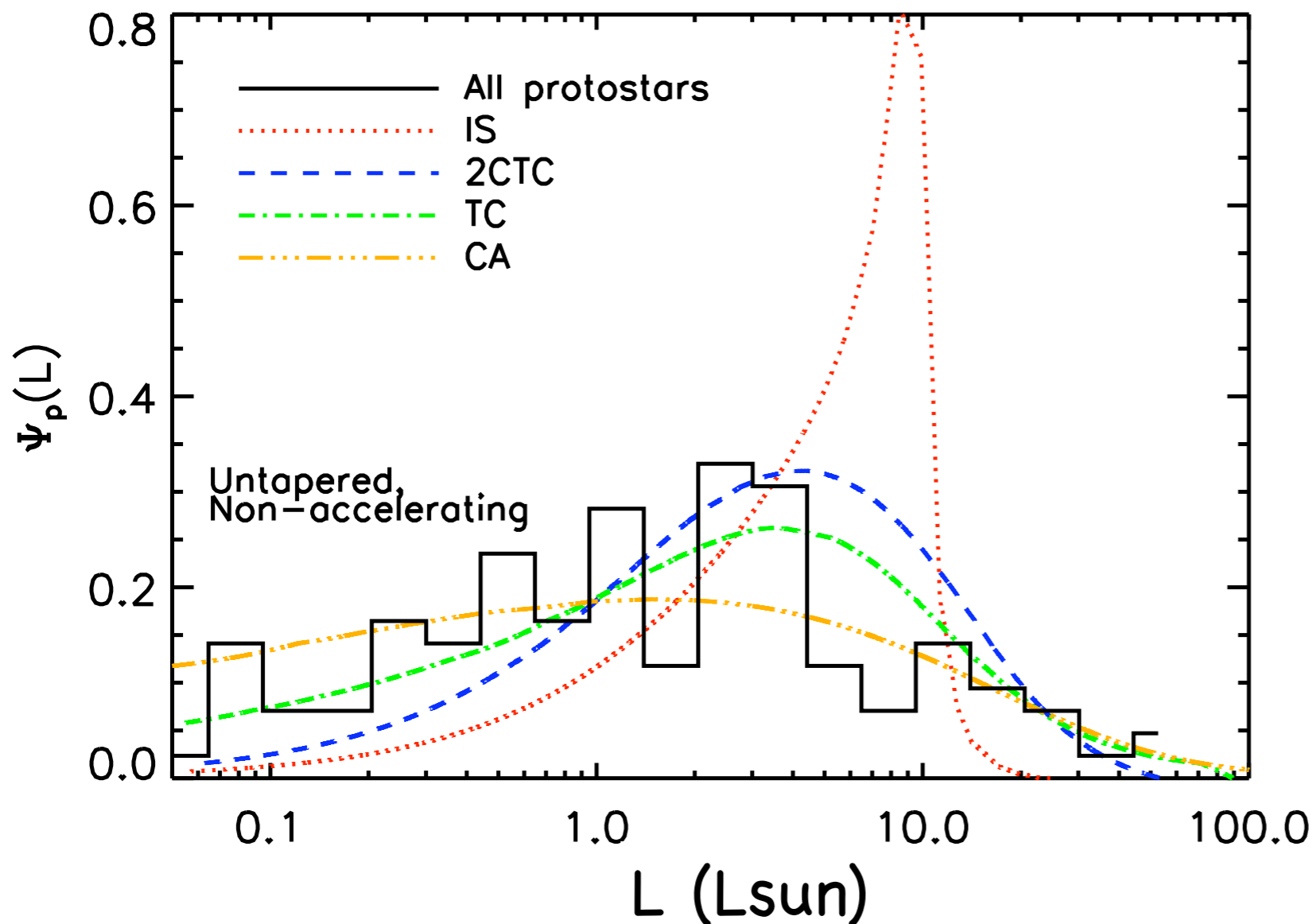
Evans et al. 09

$\langle t_f \rangle = 0.3 \pm 0.1$  Myr



# PLF Shapes

$$\Psi_p(L) = \int_{m_{f,l}}^{m_u} d \ln m_f \frac{\psi_{p2}[m(L, m_f), m_f]}{\left| \frac{\partial \ln L}{\partial \ln m} \right|}$$



Models tend to peak towards higher luminosity with scaling using  $\langle L \rangle$

Broad shapes of CA, TC show best agreement



# Verdict on Episodic Accretion

- Assuming some radiative inefficiency,  $f_{\text{acc}}=0.75$ , and some episodic accretion,  $f_{\text{epi}}=0.25$ , there is **no** luminosity problem (I)
- If  $f_{\text{epi}}=0.25$ , models suggest  $\langle t_f \rangle = 0.3 \pm 0.1$  Myr
- Episodic accretion is not needed to broaden the distribution -- if  $\dot{m}$  depends on  $m$ ,  $m_f$  there is **no** luminosity problem (II)
- Models with constant star formation time (CA, TC) agree better than models with constant accretion rates (IS)



Can Episodic Accretion  
Solve Open Problems in  
Star formation ??

Problem # 2:  
Stellar Ages



# How old are young stars?

For example:

D'Antona & Mazzitelli  
(1994)

Baraffe et al. (1998)

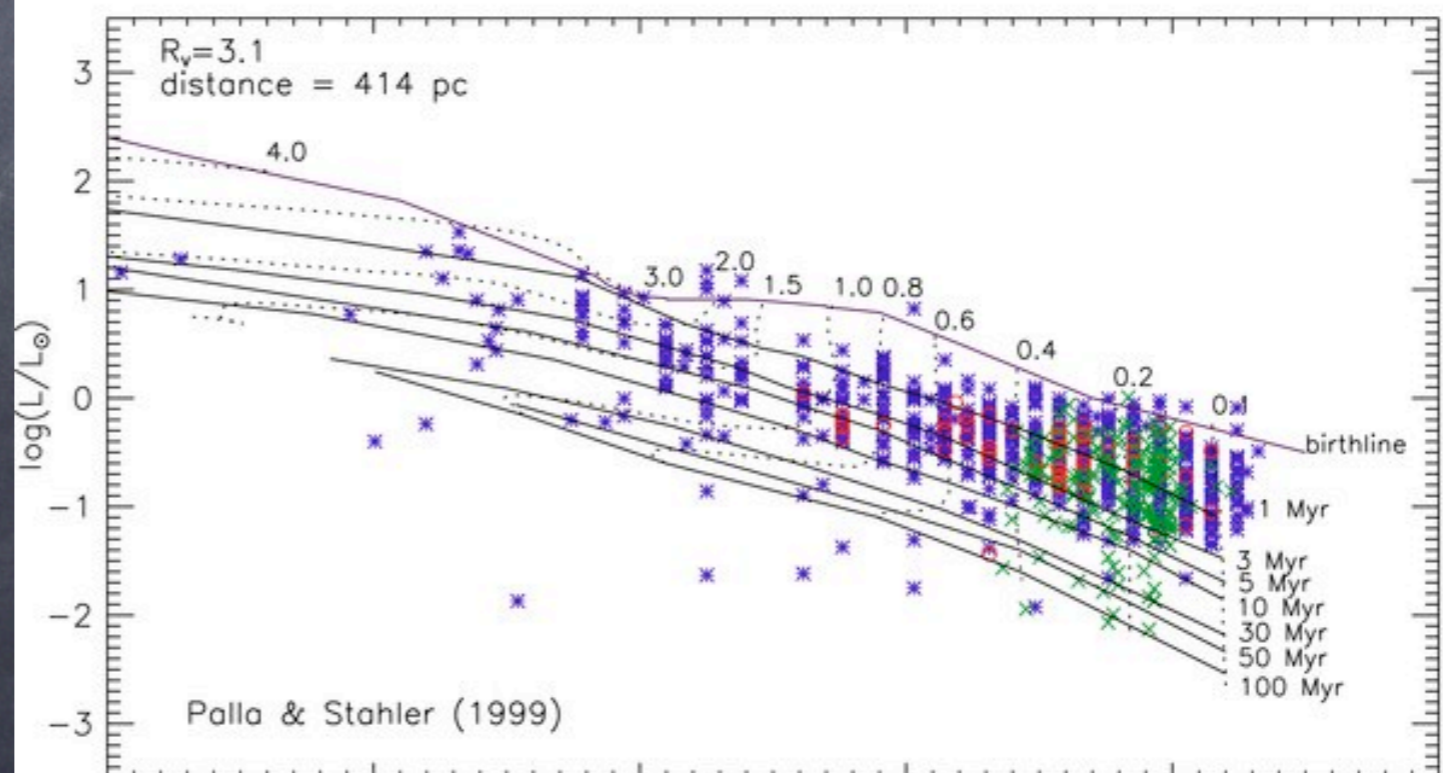
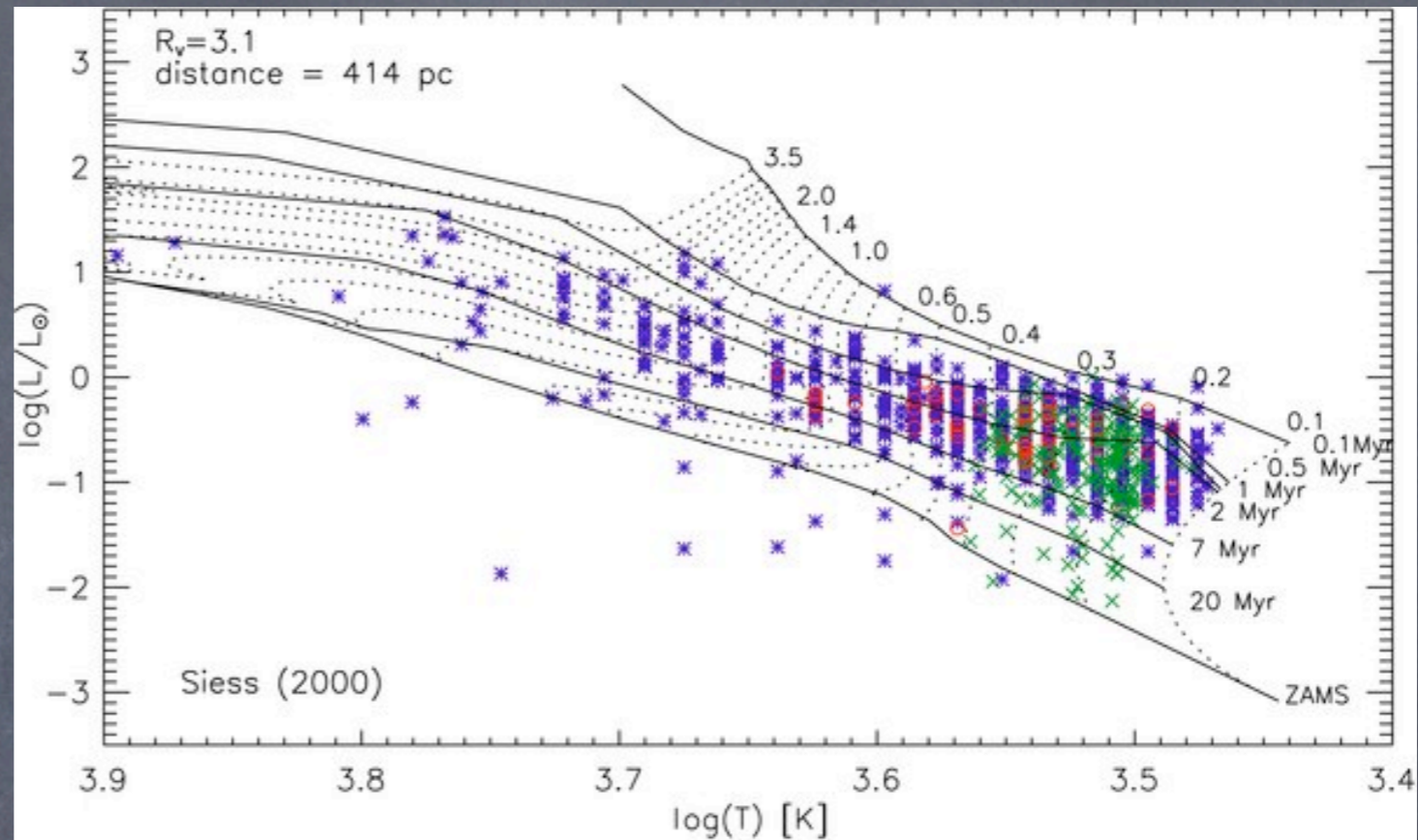
Siess et al. (2000)

Palla & Stahler (1999,  
2000)

Hartmann (2001, 2003)

## ONC

(Da Rio et al. 2009)





# Initial Models

## Accretion Histories

Episodic

Constant

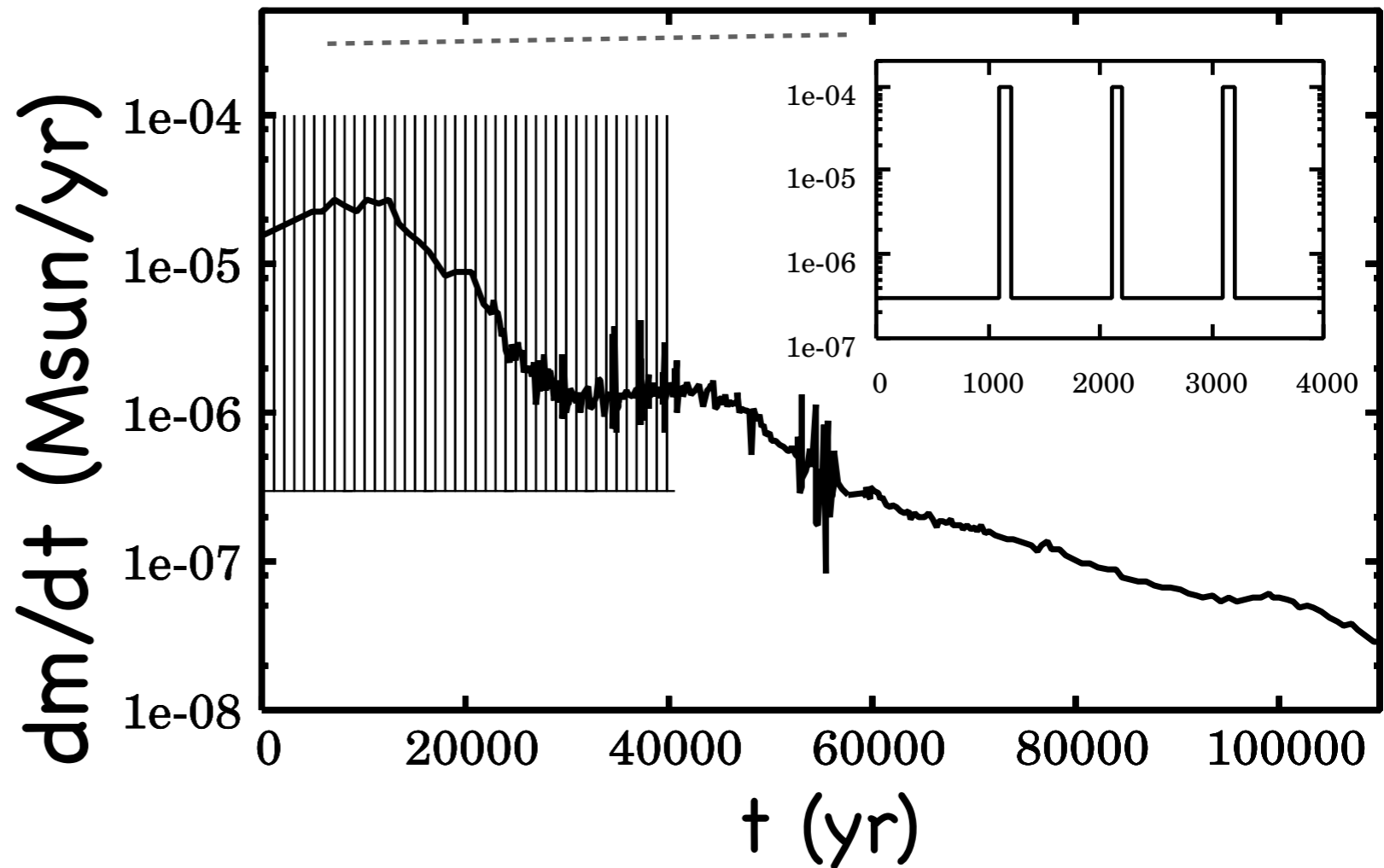
Declining (Offner 09)

Masses:

0.05–0.9  $M_{\text{sun}}$

Boundary Condition

Hot or Cold





# Model Definition

Hot ( $\alpha \geq 0.2$ )

vs.

Cold ( $\alpha < 0.2$ )

“Spherical”

Accretion directly hits and covers most of stellar surface (may arrive in a disk)

“Thin Disk”

Accretion covers small fraction of the stellar surface

“Thermally Efficient”

Some heat carried into stellar interior

“Thermally Inefficient”

Material settles softly and stellar photosphere radiates freely (most energy lost)

Shock jump boundary conditions

Photospheric boundary conditions

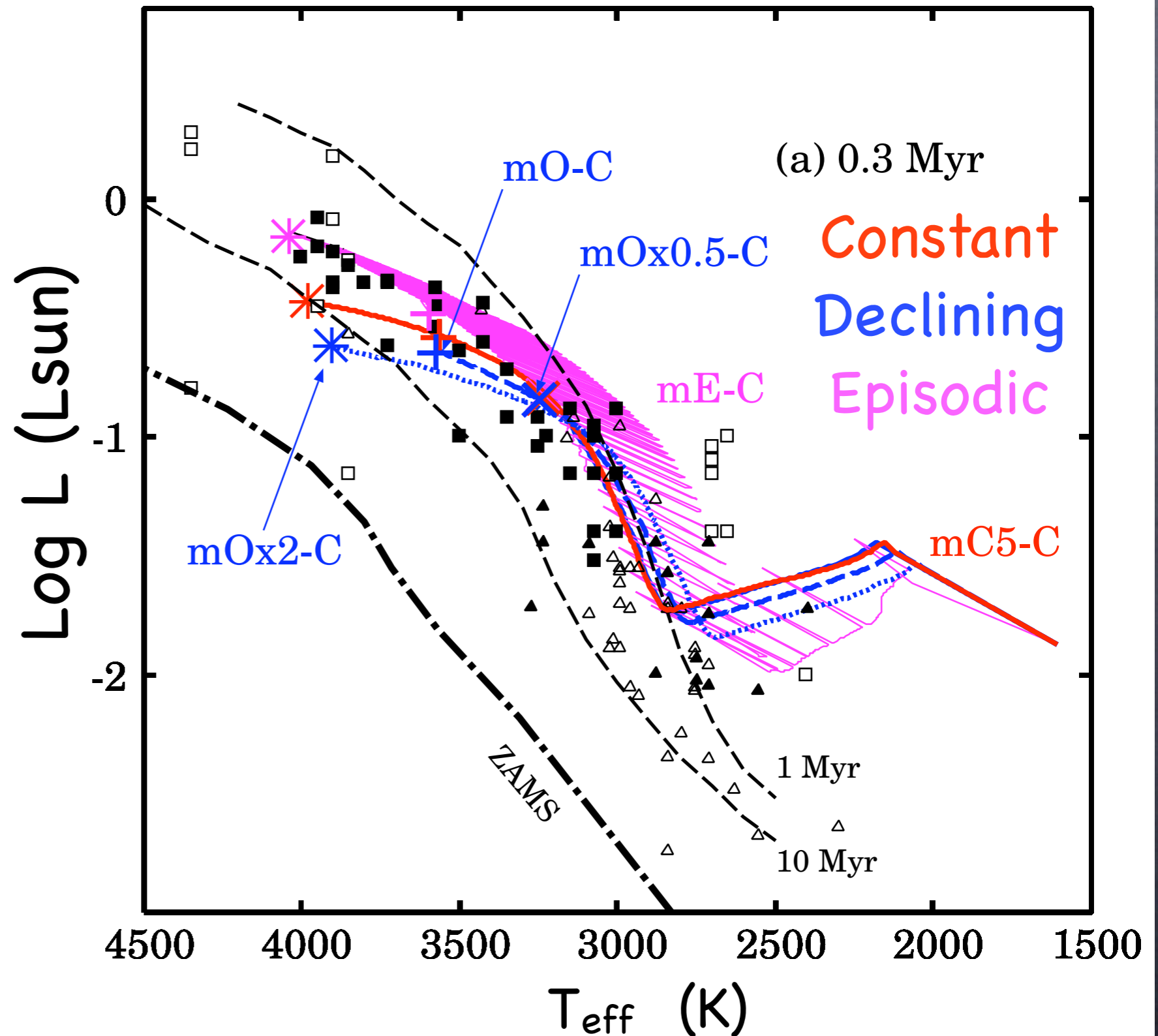


# Accretion History

HOK2011

Cold,  
same initial  
conditions,  
different  
accretion  
histories

x 0.23 Msun  
+ 0.45 Msun  
\* 0.90 Msun



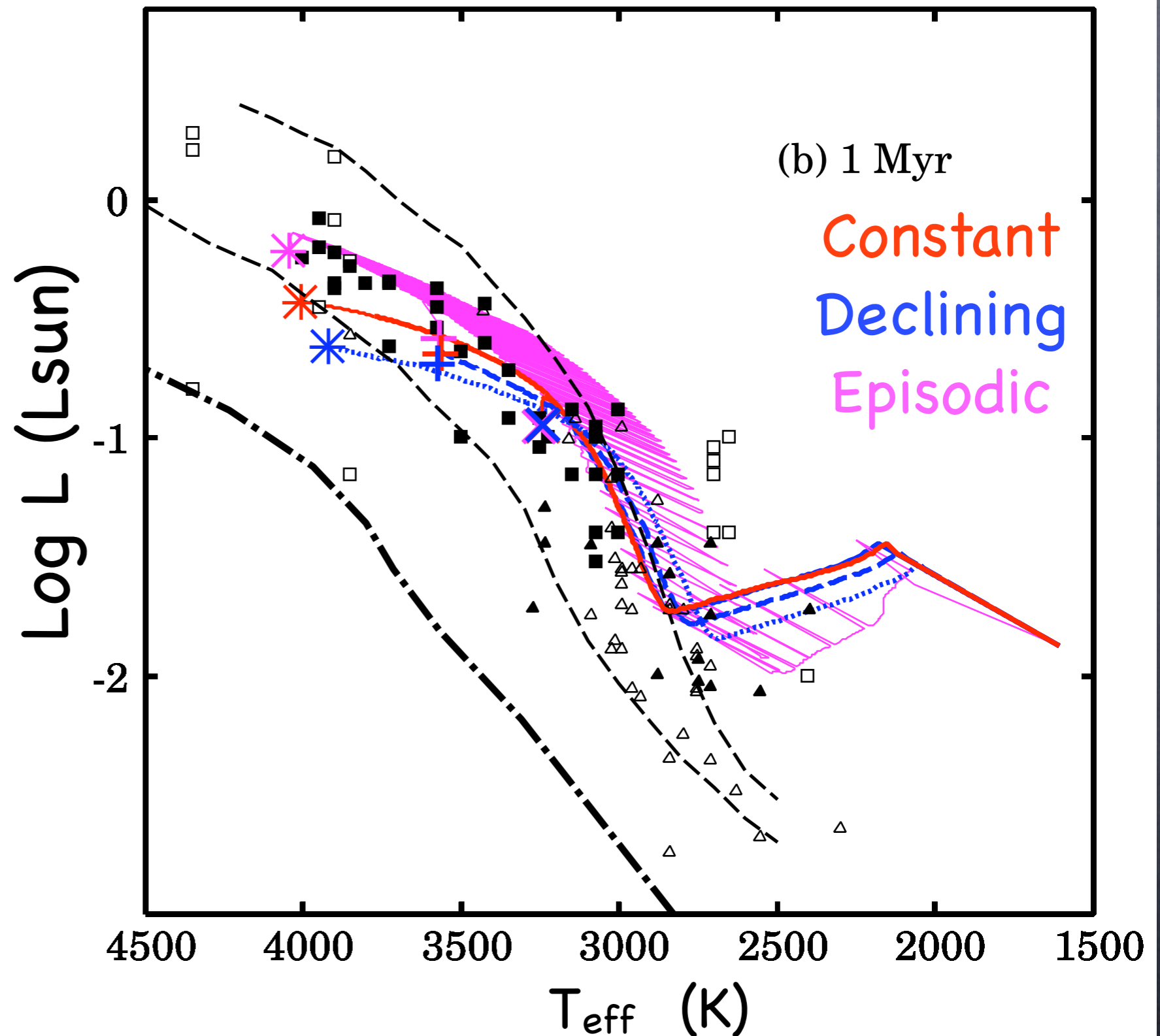


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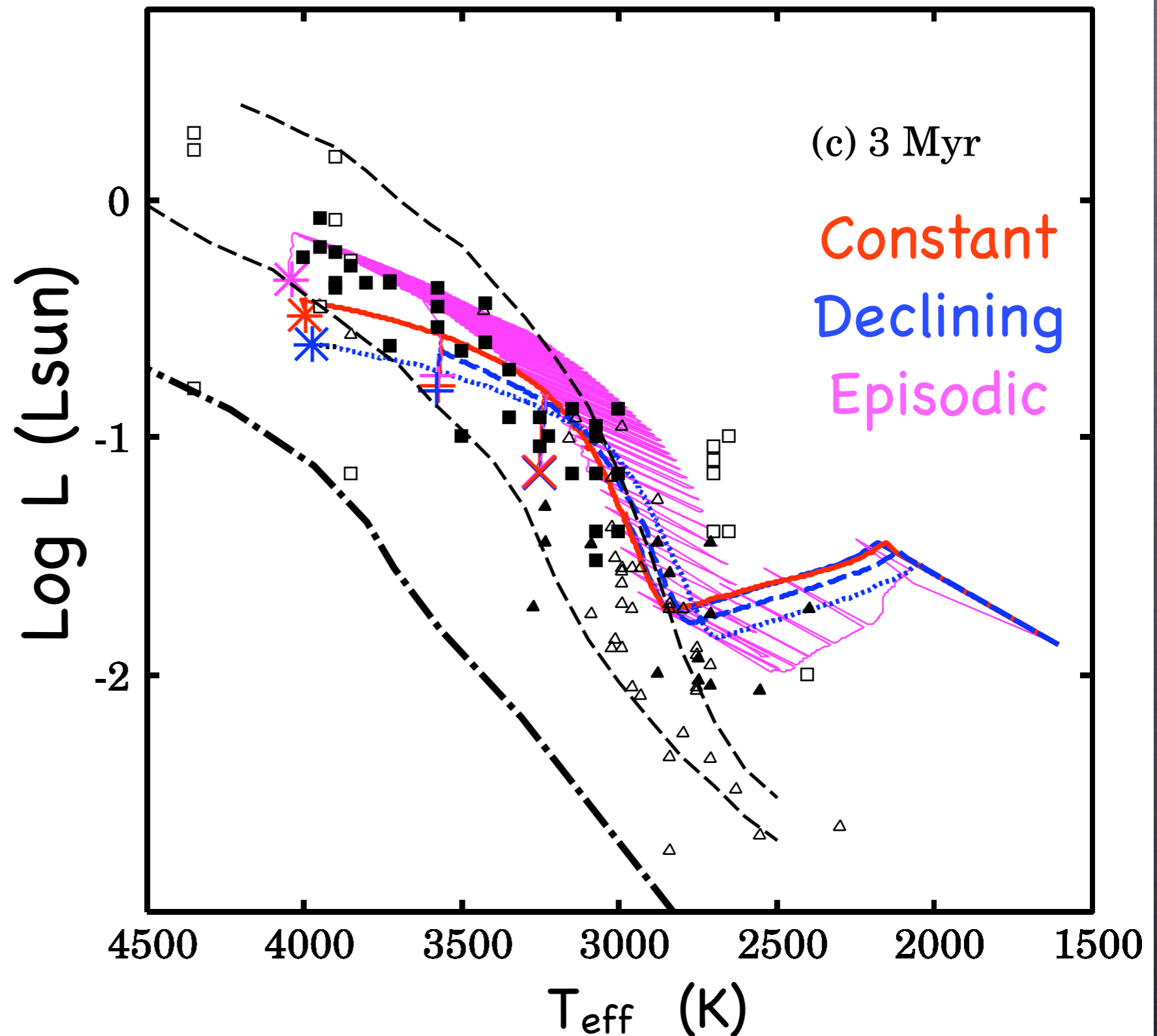


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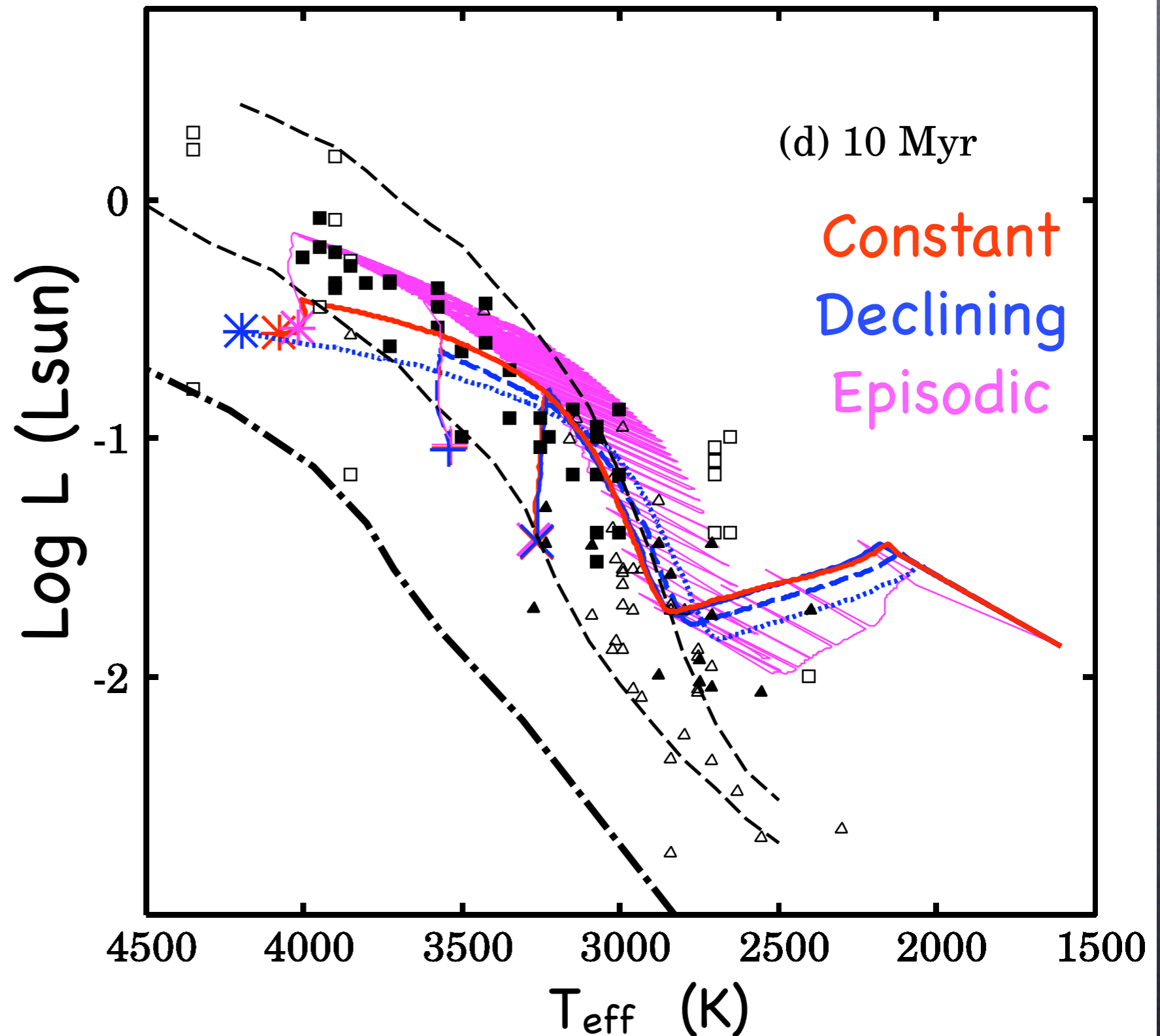


# Accretion History

HOK2011

Cold,  
same initial  
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accretion  
histories

0.23 and 0.45  
Msun show no /  
little  
dependence on  
accretion



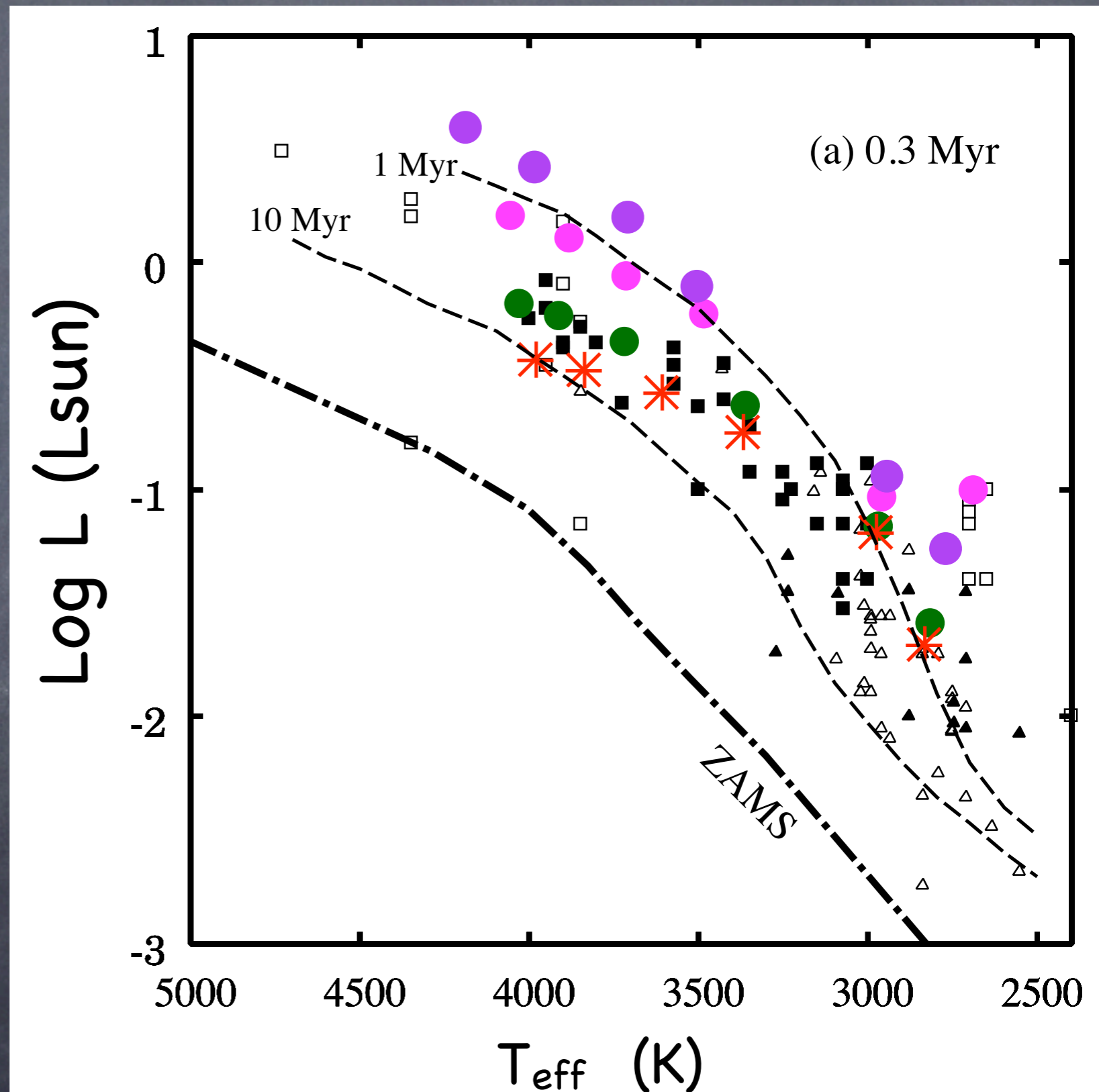


# Model Assumption

HOK2011

Same accretion  
history,  
different model

Hot ( $R=3.7$ )  
Hot/Cold ( $M=0.03$ )  
Cold ( $R=3.7$ )  
Cold ( $R=1.5$ )



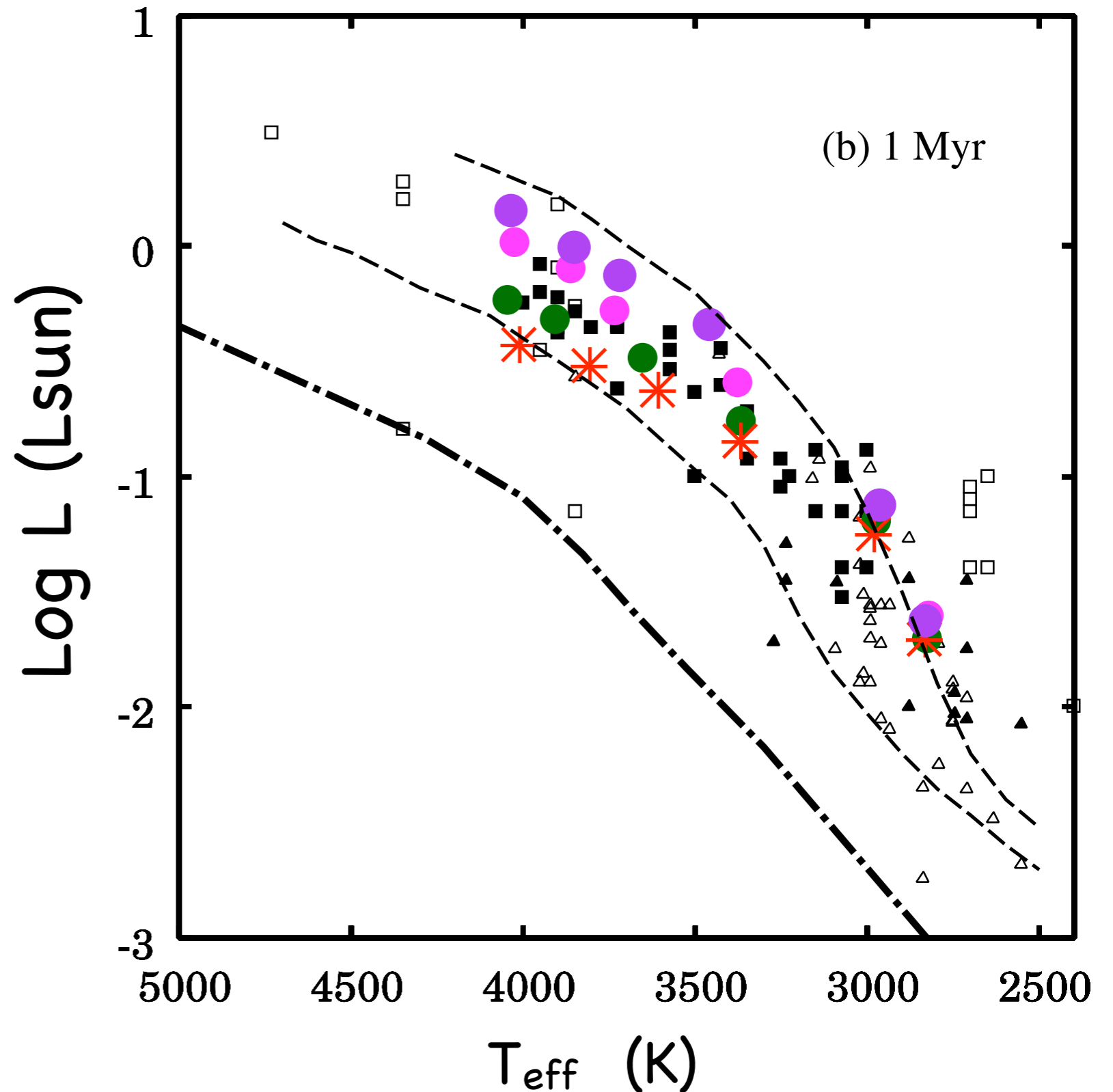


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HOK2011

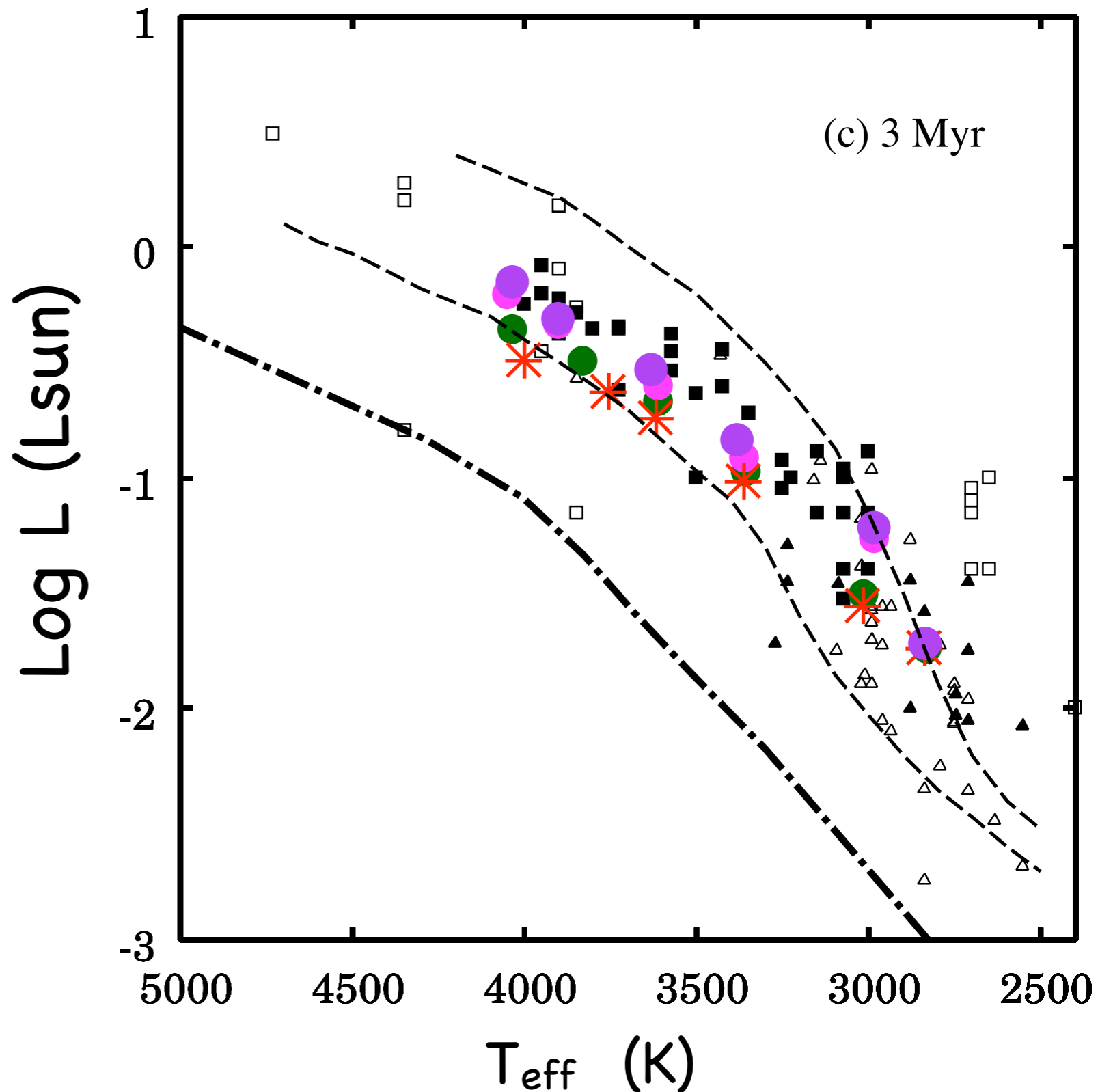
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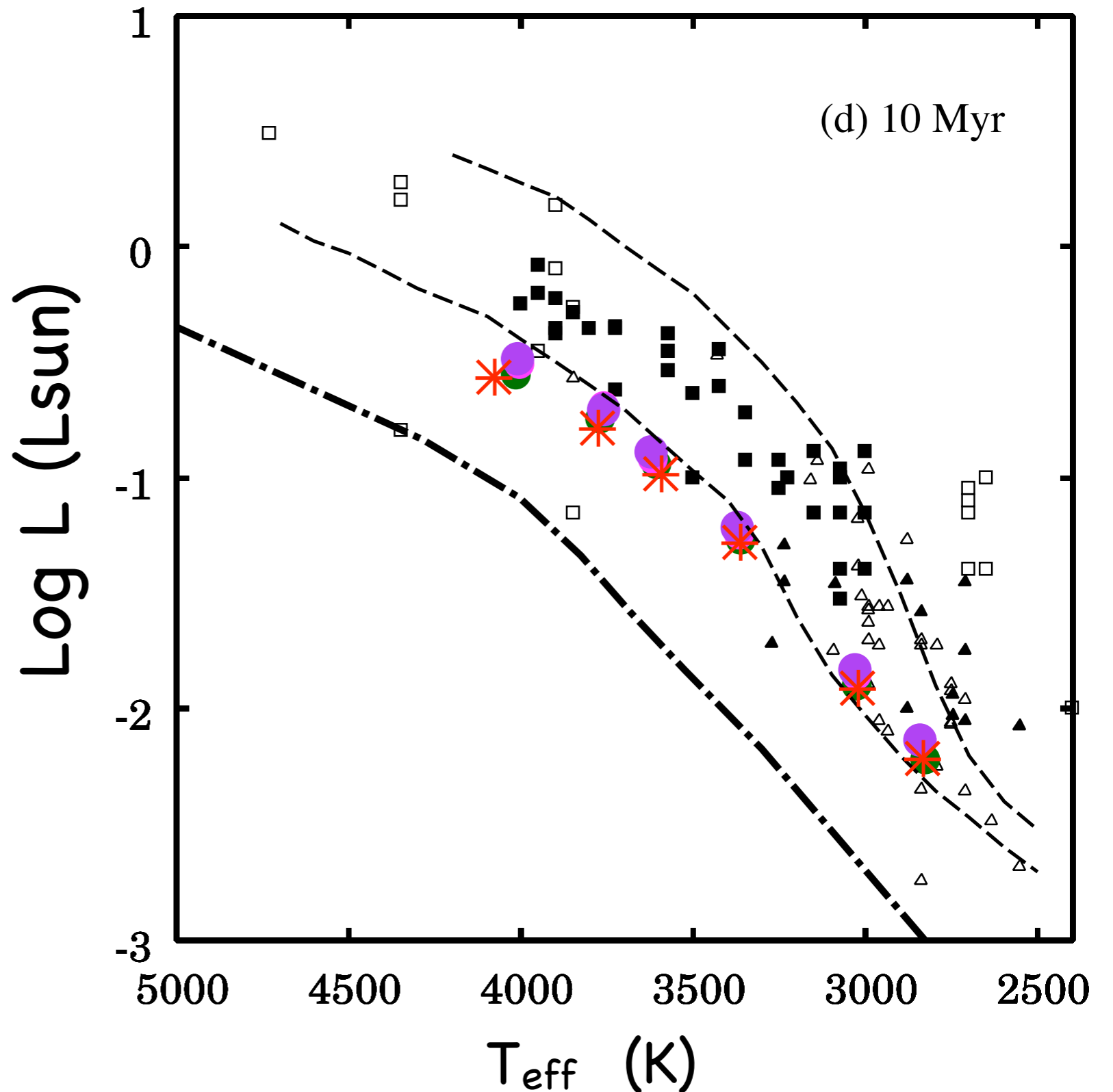


# Model Assumption

HOK2011

Same accretion  
history,  
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Need age  
spreads or hot  
and cold  
accretion with  
different initial  
conditions



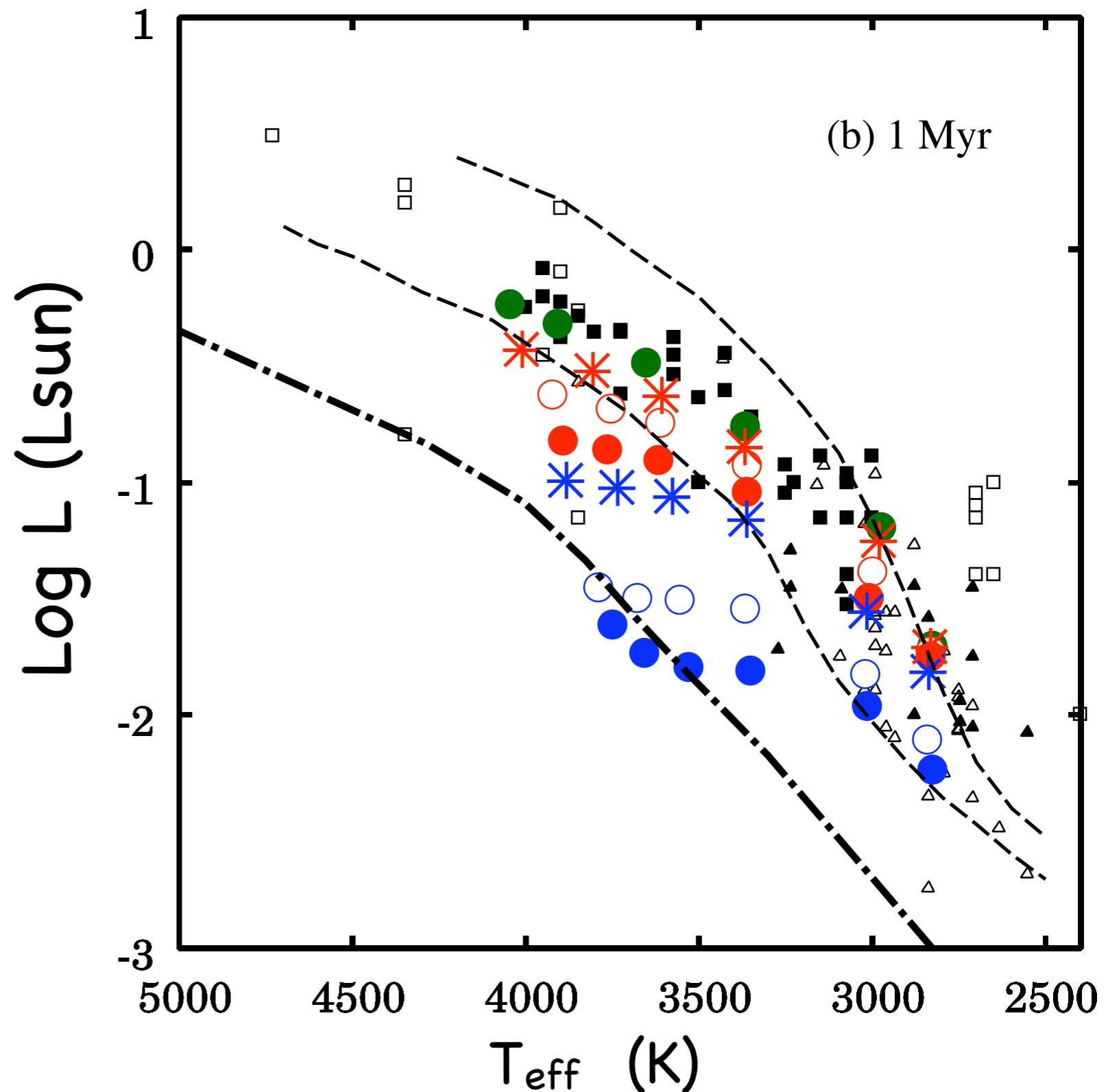


# Initial Conditions

HOK2011

Same accretion  
history, Cold,  
different initial  
radii

- Cold ( $R=3.7$ )
- \* Cold ( $R=1.5$ )
- Cold ( $R=1.0$ )
- Cold ( $R=0.65$ )
- \* Cold ( $R=0.3$ )
- Cold ( $R=0.25$ )
- Cold ( $R=0.2$ )





# Verdict on Episodic Accretion

- Initial conditions and model assumptions influence evolution more than accretion
- Accretion history mainly affects higher mass stars ( $>0.9 M_{\text{sun}}$ ) otherwise differences disappear in  $\sim 2$  Myr
- Stellar age spreads are likely real (unless initial conditions know about final mass)



# Conclusions

- Episodic accretion likely accounts for **25%** of the stellar mass, but ....
- **Not required** to explain distribution of protostellar luminosities
- It is **not useful** for explaining stellar age spreads