

Fundamental Parameters of Stellar (Photospheric) Physics

Jason Aufdenberg (ERAU)

What's to Come....

90 Years of stellar angular diameters

Diameters + Distances \rightarrow Radii

Quick intro to temperature structure of the Sun

Quick introduction to limb darkening

How an interferometer sees a star

Limb darkening observed on 23 stars

Giants, geometry, and limb darkening

Convection, 3D models, and limb darkening

Warm supergiants and limb darkening

Rapid Rotators: observations and models

Michelson and Pease (1921): Angular Size of Betelgeuse

Astrophysical Journal 53, 249-259

MEASUREMENT OF THE DIAMETER OF α ORIONIS WITH THE INTERFEROMETER¹

BY A. A. MICHELSON AND F. G. PEASE

ABSTRACT

Twenty-foot interferometer for measuring minute angles.—Since pencils of rays at least 10 feet apart must be used to measure the diameters of even the largest stars, and because the interferometer results obtained with the 100-inch reflector were so encouraging, the construction of a 20-foot interferometer was undertaken. A very rigid beam made of structural steel was mounted on the end of the Cassegrain cage, and four 6-inch mirrors were mounted on it so as to reduce the separation of the pencils to 45 inches and enable them to be brought to accurate coincidence by the telescope. The methods of making the fine adjustments necessary are described, including the use of two thin wedges of glass to vary continuously the equivalent air-path of one pencil. Sharp fringes were obtained with this instrument in August, 1920.

Diameter of α Orionis.—Although the interferometer was not yet provided with means for continuously altering the distance between the pencils used, some observations were made on this star, which was known to be very large. On December 13, 1920, with very good seeing, no fringes could be found when the separation of the pencils was 121 inches, although tests on other stars showed the instrument to be in perfect adjustment. This separation for minimum visibility gives the angular diameter as $0''.047$ within 10 per cent, assuming the disk of the star uniformly luminous. Hence, taking the parallax as $0''.018$, the linear diameter comes out 240×10^6 miles.

Interferometer method of determining the distribution of luminosity on a stellar disk.—The variation of intensity of the interference fringes with the separation of the two pencils depends not only on the angular diameter of the disk but also on the distribution of luminosity. The theory is developed for the case in which $I = I_0 (R^2 - r^2)^n$, and formulae are given for determining n from observations.

Table of values of $\int_0^1 (1-x^2)^{n+\frac{1}{2}} \cos kx dx$, for n equal to 0, $\frac{1}{2}$, 1, and 2, and for k up to 600° , is given.

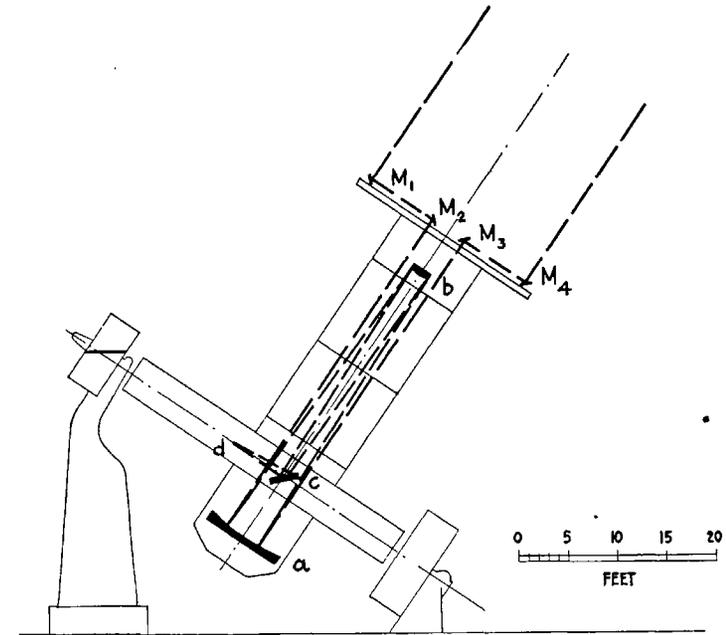
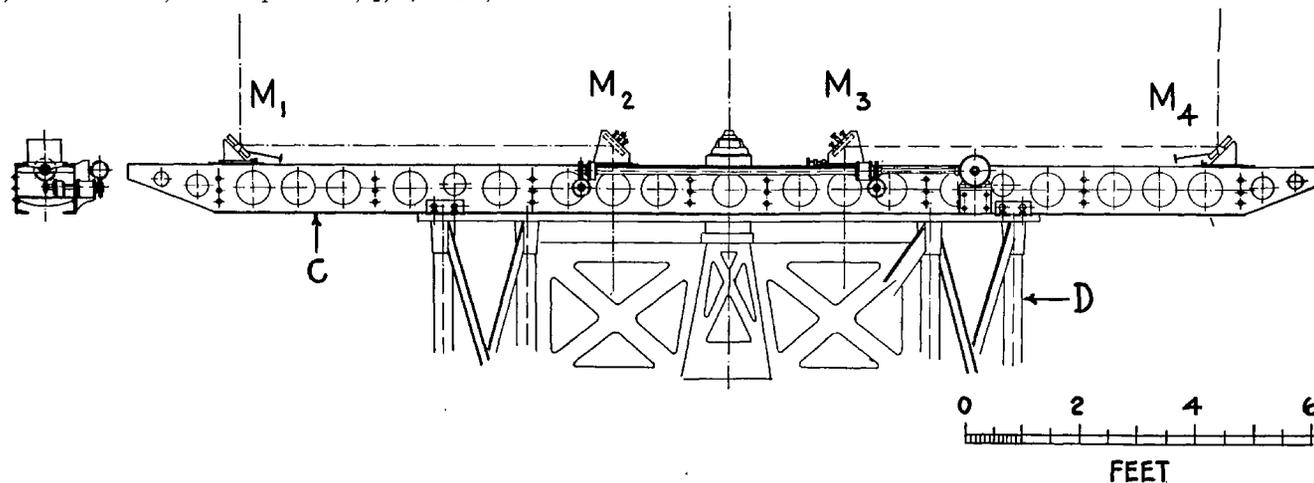


FIG. 1.—Diagram of optical path of interferometer pencils. M_1, M_2, M_3, M_4 , mirrors; a , 100-inch paraboloid; b , convex mirror; c , coudé flat; d , focus.



**Interferometric Fringes from
Creekside Observatory, Daytona Beach, Florida, USA
 α Lyrae 29 September 2011**



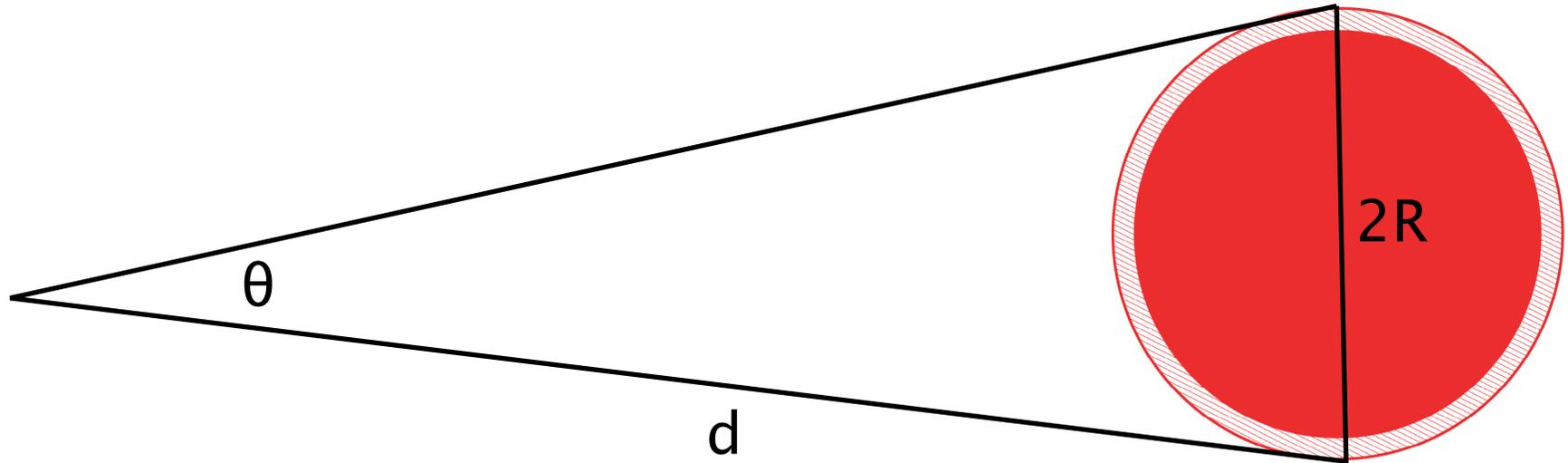
Wavelength: R-band (~600 nm)

Apertures: 12.1 cm, Baseline: 37.5 cm

Scale = 0.08 arcseconds/pixel

0.05 sec exposures, 5 frames per second movie

Radius from Angular Size and Distance



$$R = \frac{\theta d}{2}$$

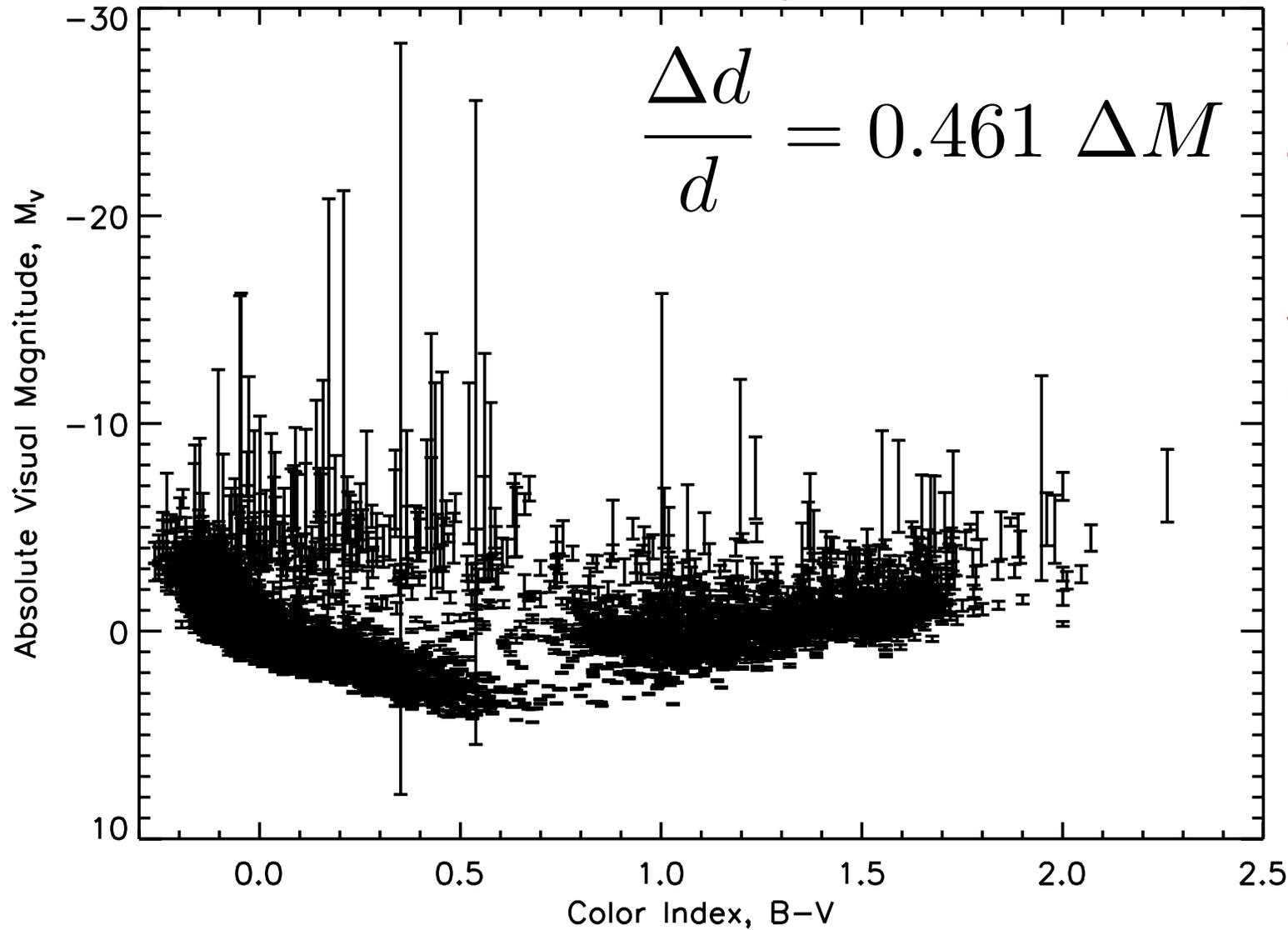
$$\theta \ll 1 \text{ radian}$$

Parallax error > 1% for 4811 of the brightest ($V < 6$) stars

All Stars $V < 6$; 1000% > parallax error > 1%

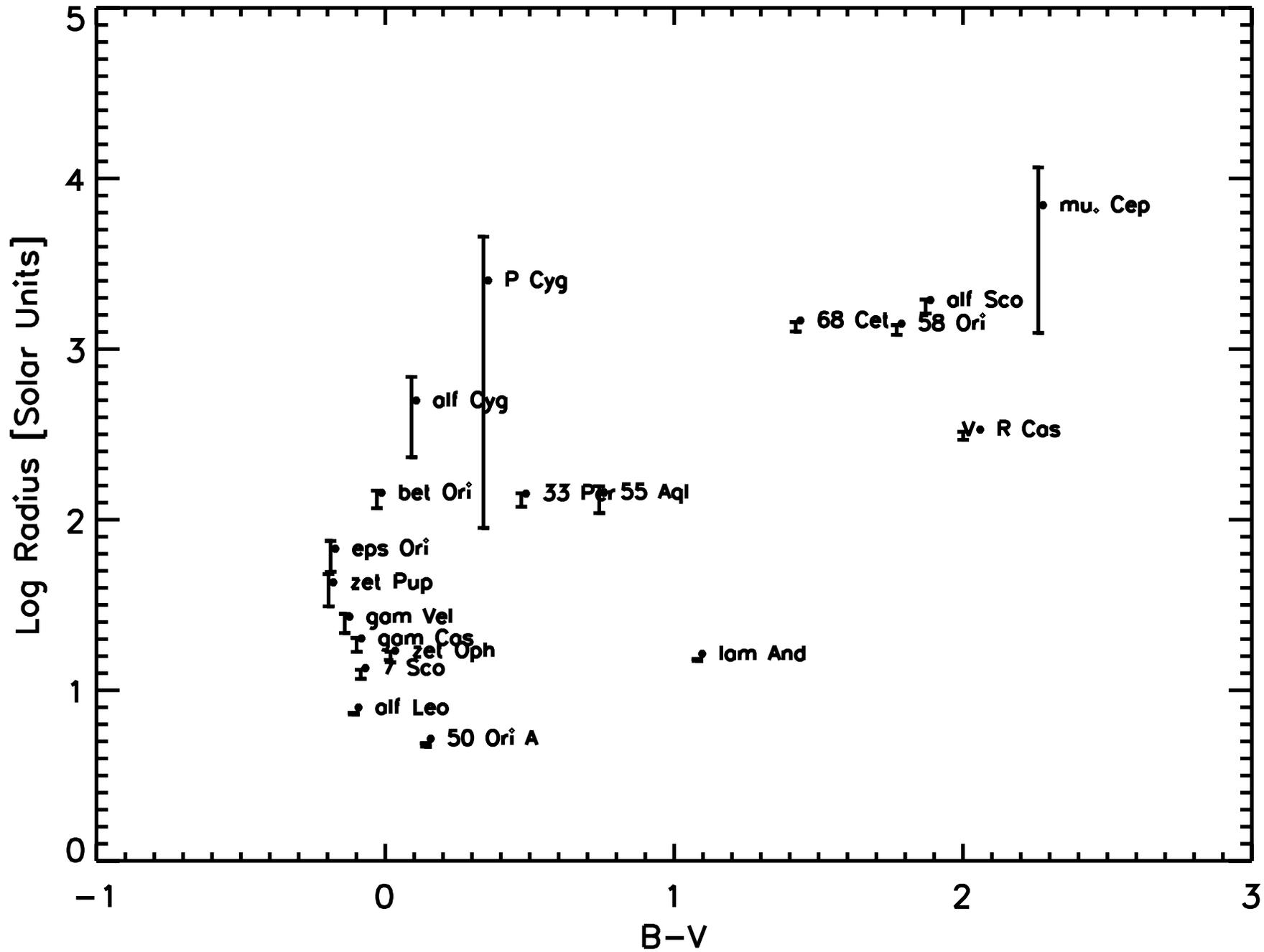
$$\frac{\Delta d}{d} = 0.461 \Delta M$$

- Seven stars ($V < 6$) have $\pi < 0.05$ mas:
HR 8154 (O8e)
32 Eri A (G8 III),
V399 Car (A9Ia),
 θ Mus (WC+...),
HR 5223 (B2IIne),
HR 5680 (O8IIIp).



"Famous" stars have radius precision limited by parallax

Radii bibs > 500



Effective Temperature from Angular Size and Flux

$$T_{\text{eff}} = \left[\frac{4\mathcal{F}_0}{\sigma\theta_{\text{LD}}^2} \right]^{1/4}$$

Angular Diameter (corrected for limb darkening)

Bolometric Flux (corrected for extinction)

follows from:

$$4\pi d^2 \mathcal{F}_0 = L = 4\pi R^2 \sigma T_{\text{eff}}^4$$

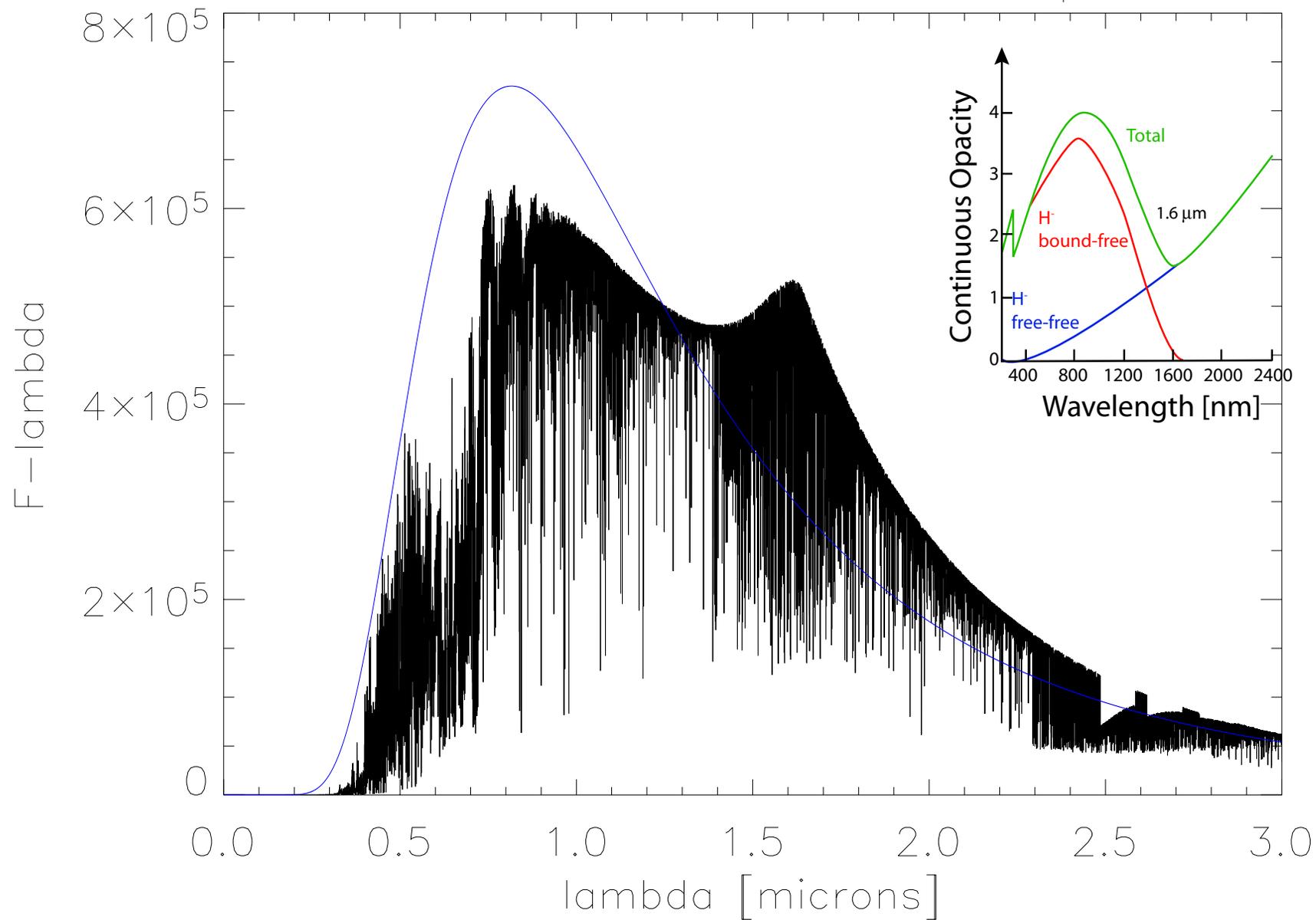
distance luminosity radius

$$\mathcal{F}_0 = \frac{R^2}{d^2} \sigma T_{\text{eff}}^4$$
$$\mathcal{F}_0 = \frac{\theta^2}{4} \sigma T_{\text{eff}}^4$$

Effective Temperature radiates same integrated flux as the star

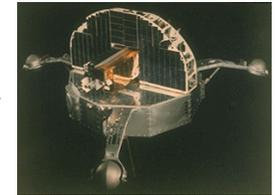
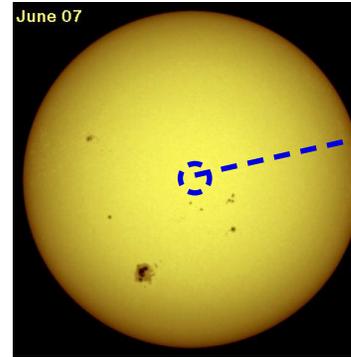
Effective temperature of black body radiates same integrated flux

3550 K BB vs. Model Atmosphere

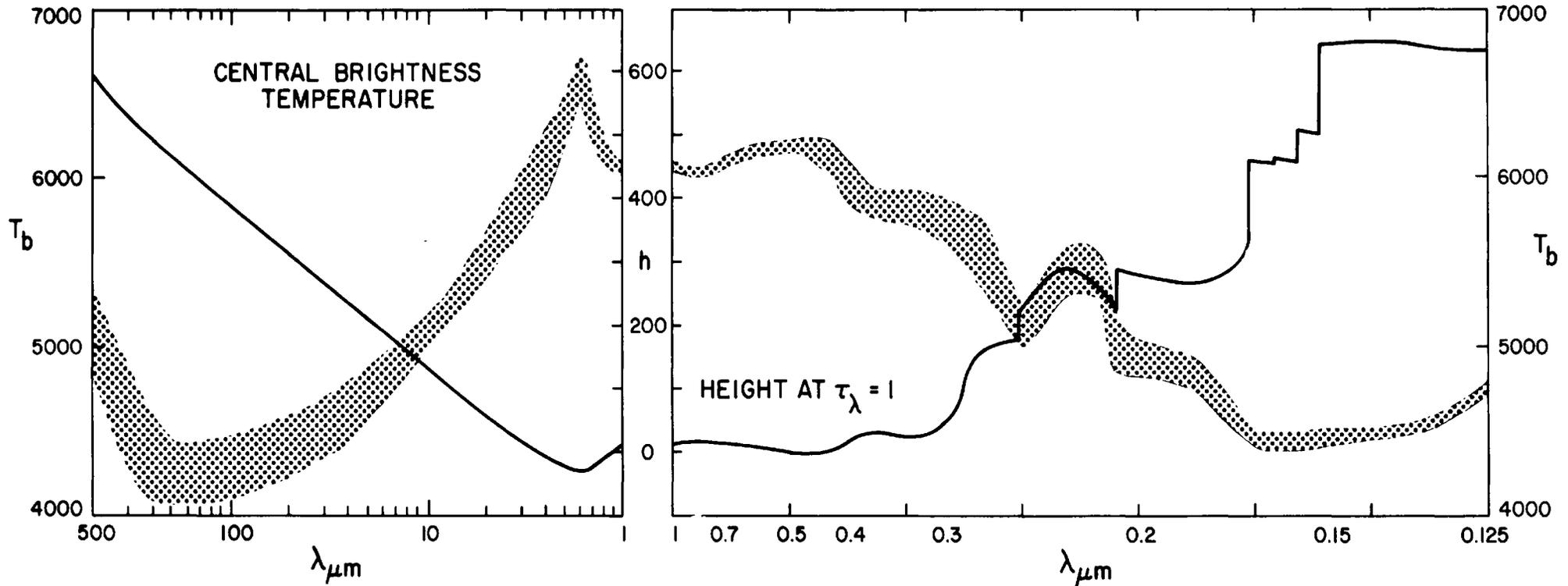


Reconstructing Temperature Structure: Spatially Resolved Absolute Intensities

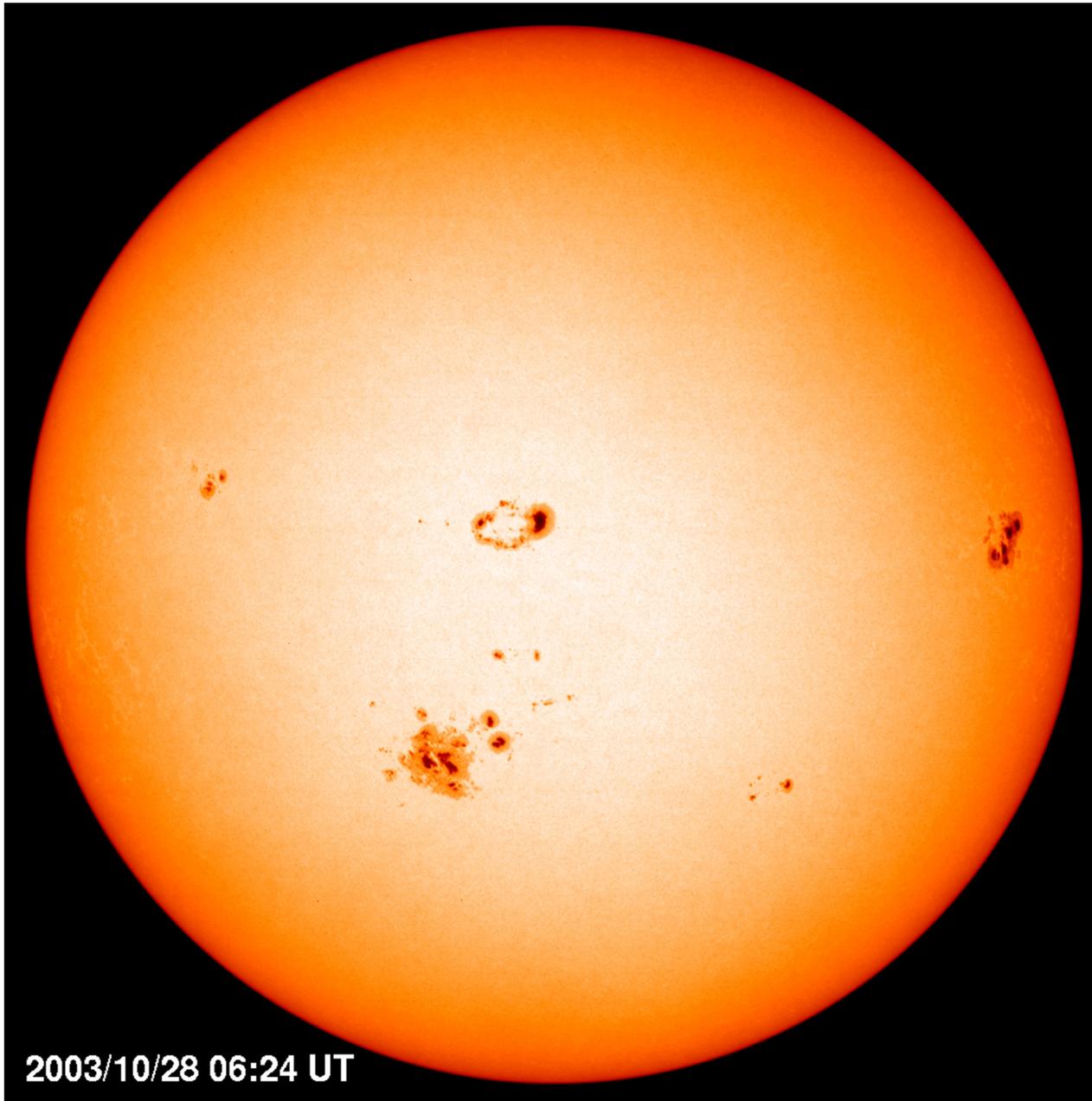
$$T_b^{\text{center}} = \frac{14388}{\lambda \ln [(11909/\lambda^5 I_\lambda) + 1]}$$



Orbiting Solar Observatory 6



Limb Darkening Reveals Temperature Structure



2003/10/28 06:24 UT

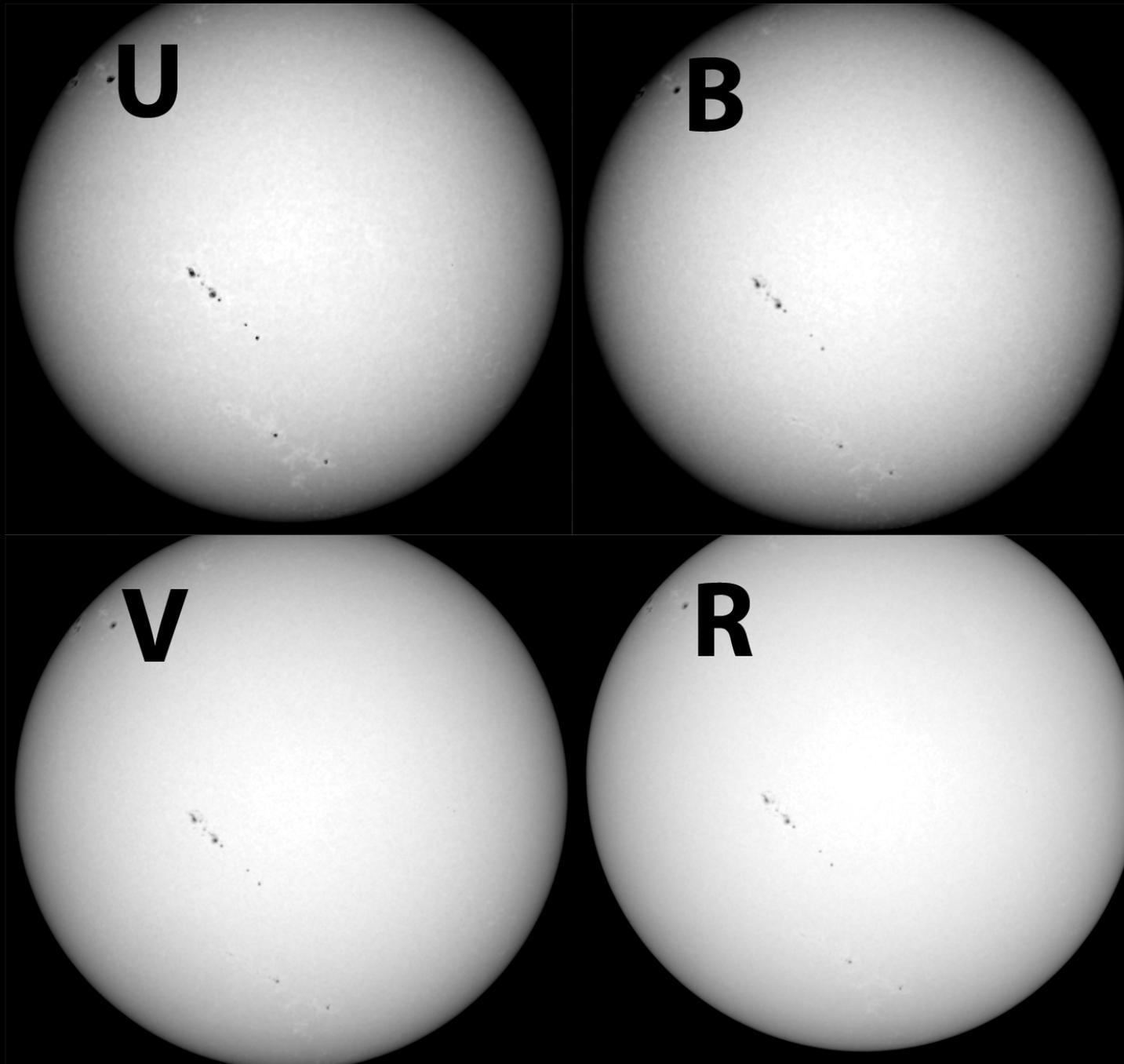
Solar and Heliospheric Observatory (SOHO), Michelson Doppler Imager (MDI)
Very narrow band Ni 6768 Å (sohowww.nascom.nasa.gov)

(a) Deeper, hotter layers are visible near the disk center

(b) Shallower, cooler layers are visible near the disk limb

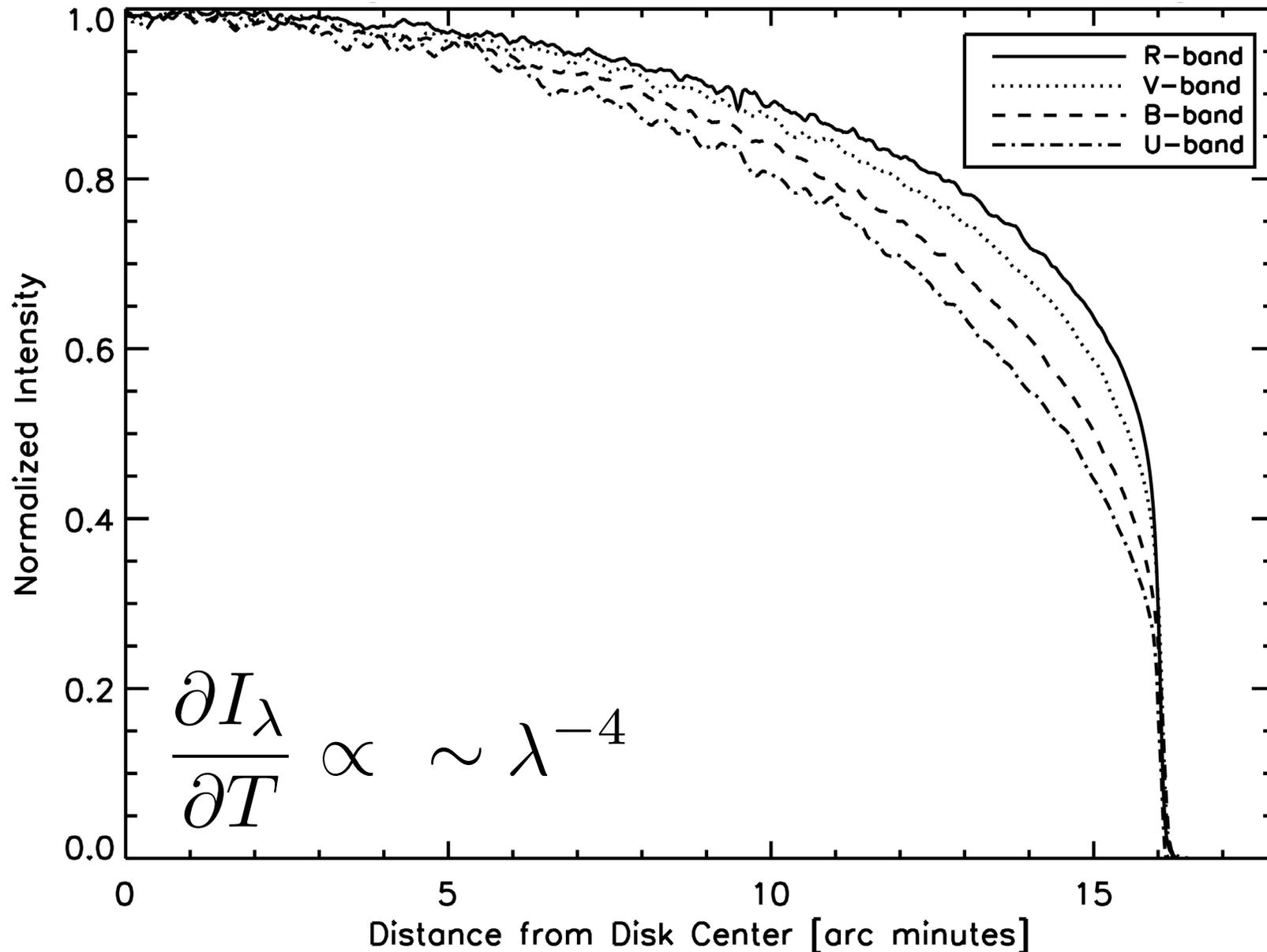
isothermal atmospheres do not exhibit limb darkening

Limb Darkening Depends on Wavelength



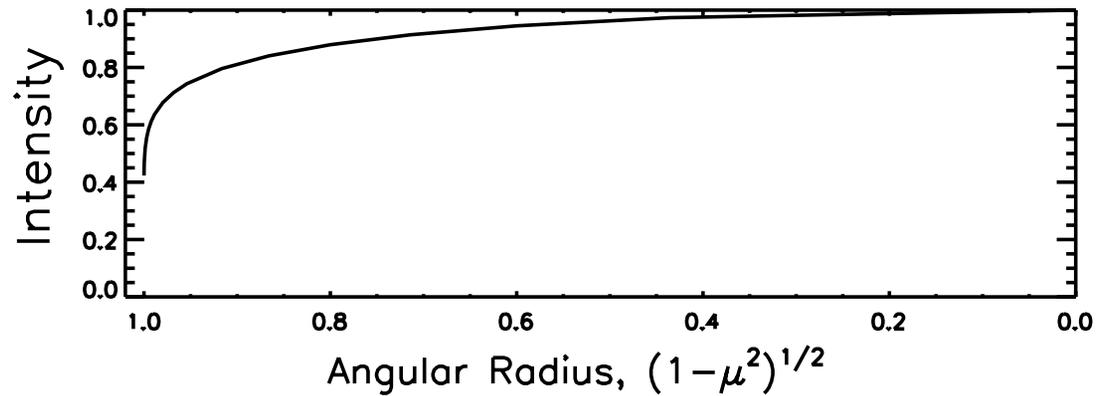
Credit: undergraduate students Edward Muller and Keily Grubaugh

Limb Darkening Depends on Wavelength

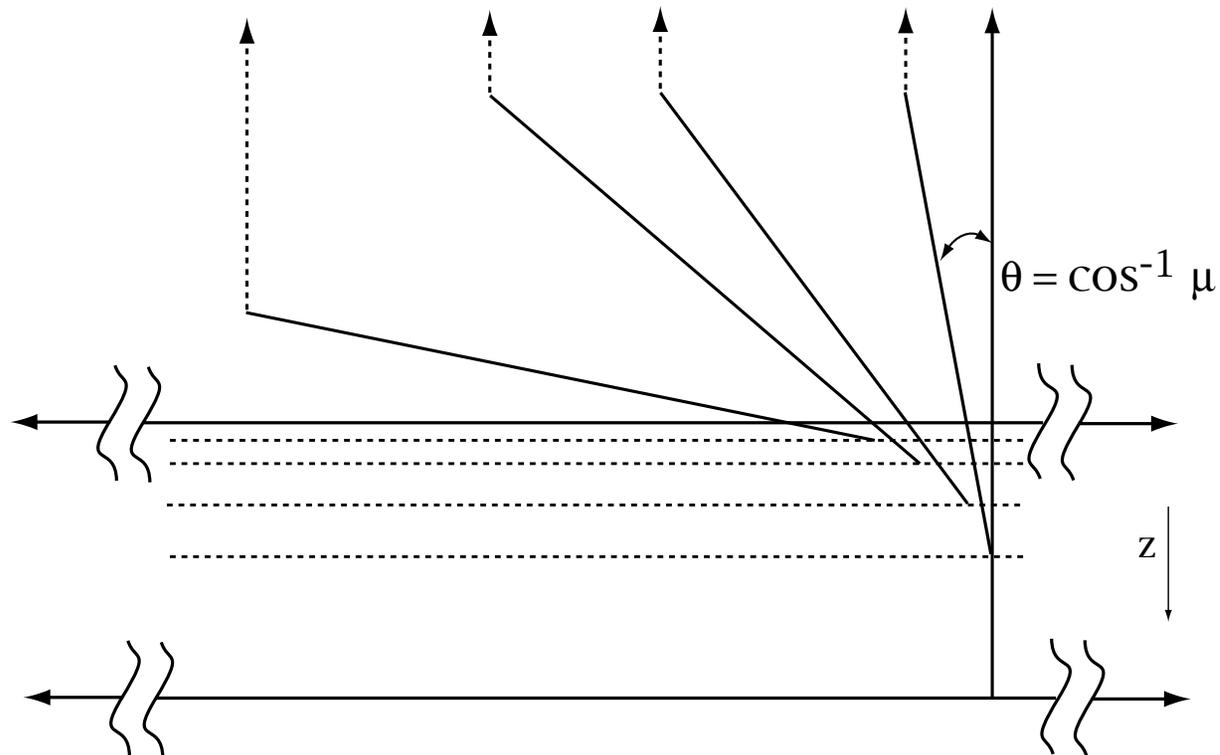


Credit: undergraduate students Edward Muller and Keily Grubaugh

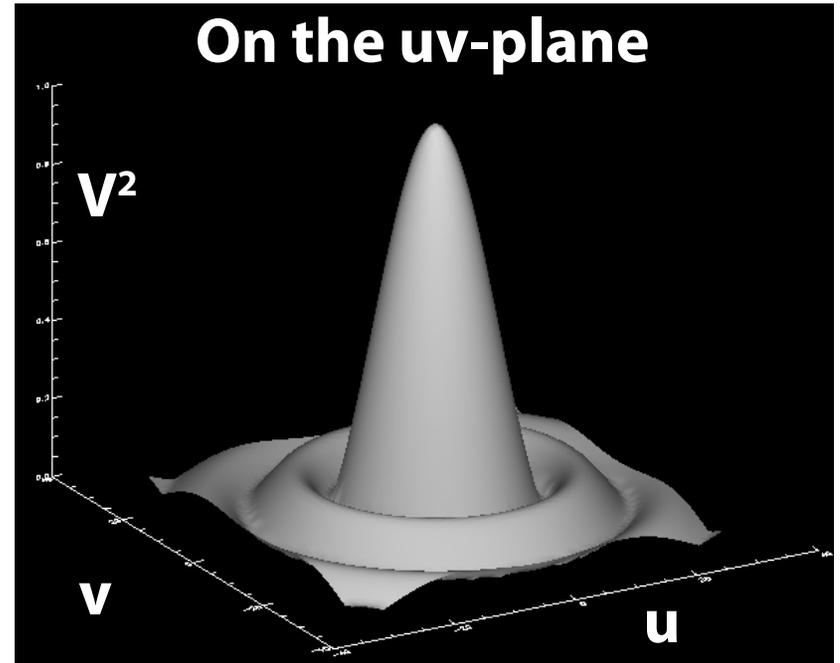
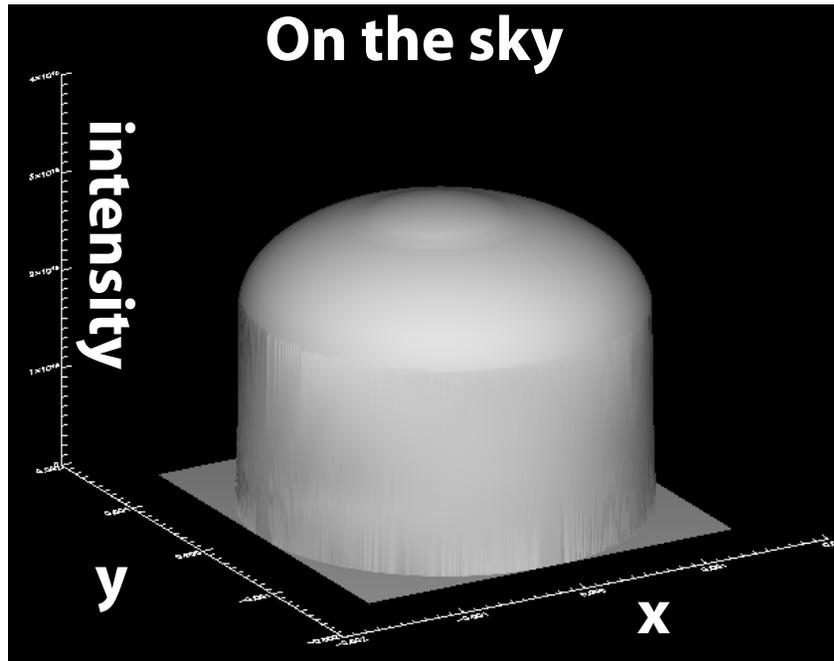
Stellar Limb Darkening: Geometry of a plane-parallel atmosphere



0.1% of
stellar
radius



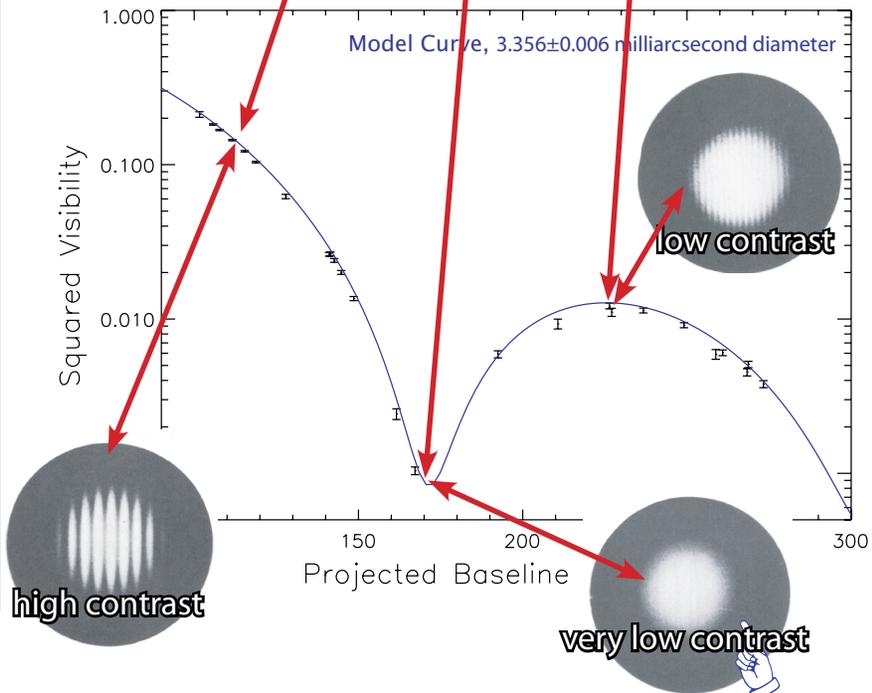
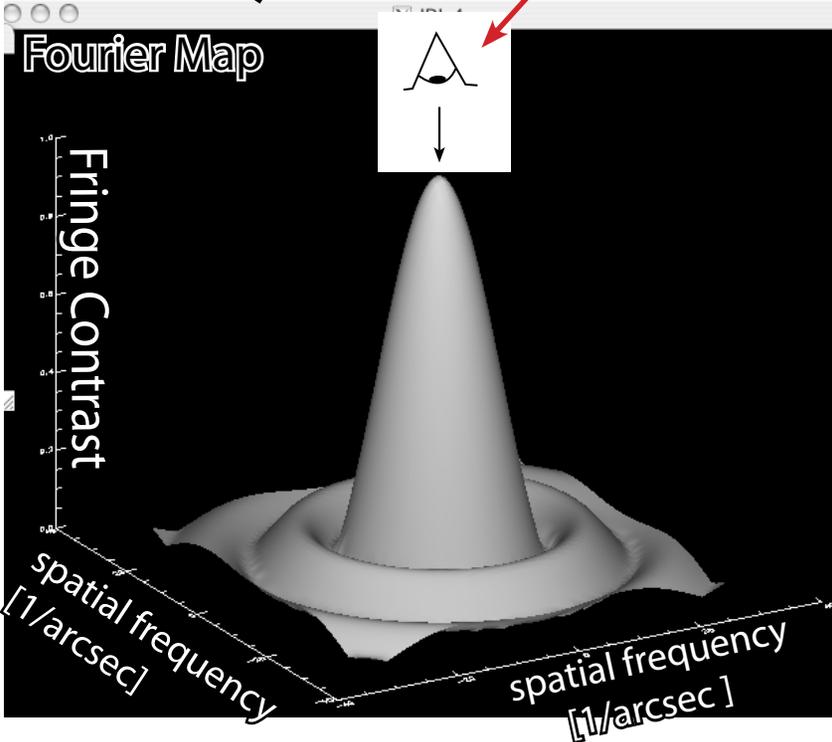
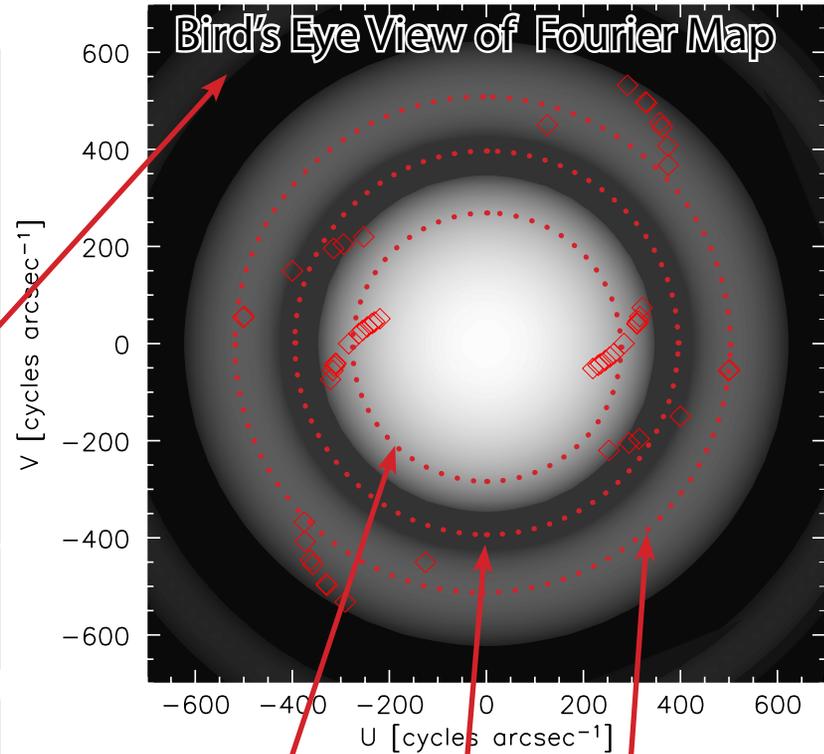
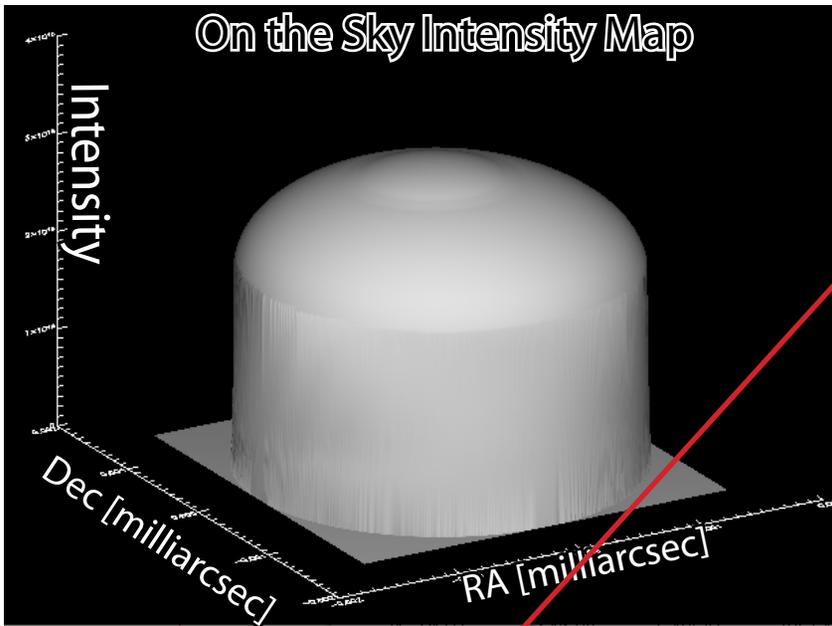
Angular Size from Interferometry



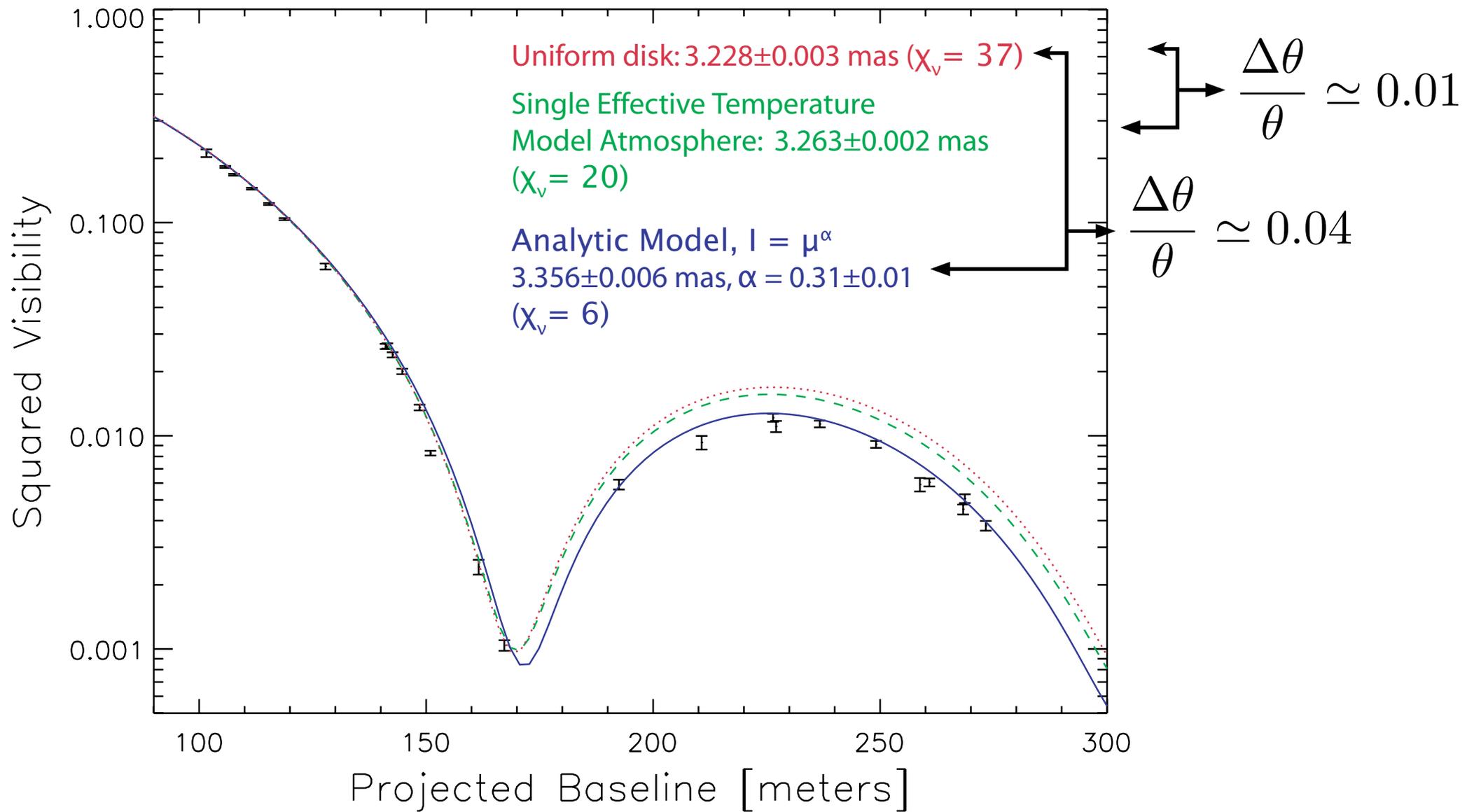
$$V_{\lambda}^2(u, v) = \left[\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} S_{\lambda} I_{\lambda}(x, y) e^{i2\pi(ux+vy)} dx dy \right]^2$$

$$V^2(B, \lambda, \theta) = \left(\frac{2J_1(\pi\theta B/\lambda)}{\pi\theta B/\lambda} \right)^2 \quad (B/\lambda)^2 = u^2 + v^2$$

How Does an Interferometer See a Single Star?



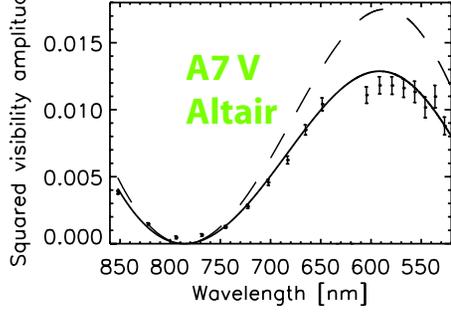
Corrections to Uniform-Disk Diameters



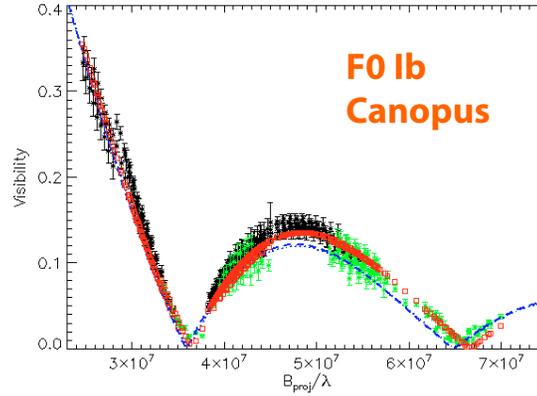
Vega (α Lyr), K-Band, CHARA/FLUOR (Aufdenberg et al. 2006, ApJ, 645, 664)

Exemplary second-lobe measurements from interferometry

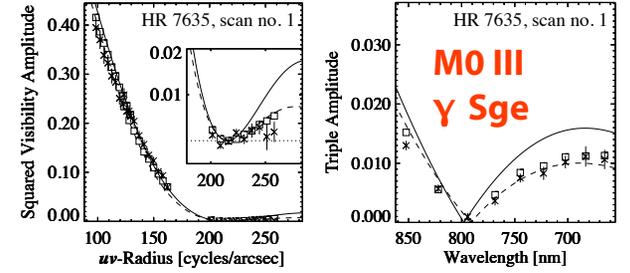
Ohishi et al. (2004)



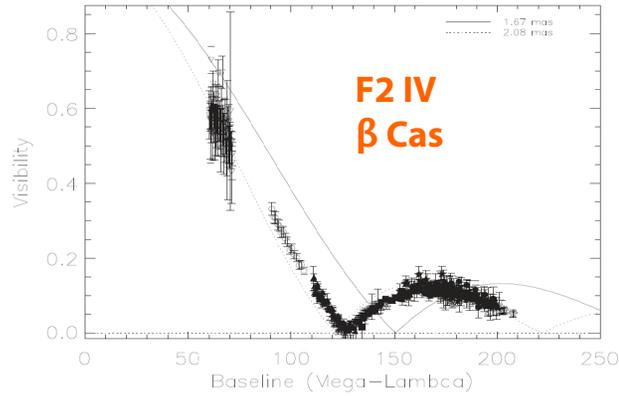
Domiciano de Souza et al. (2008)



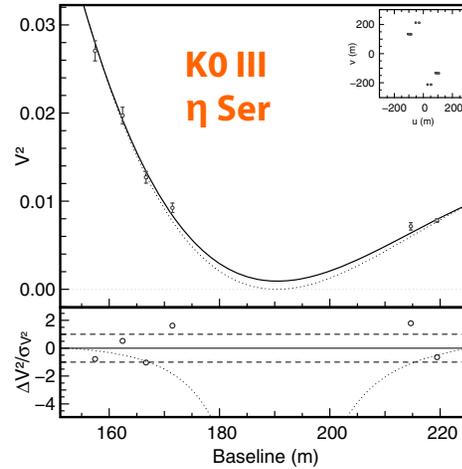
Wittkowski et al. (2001)



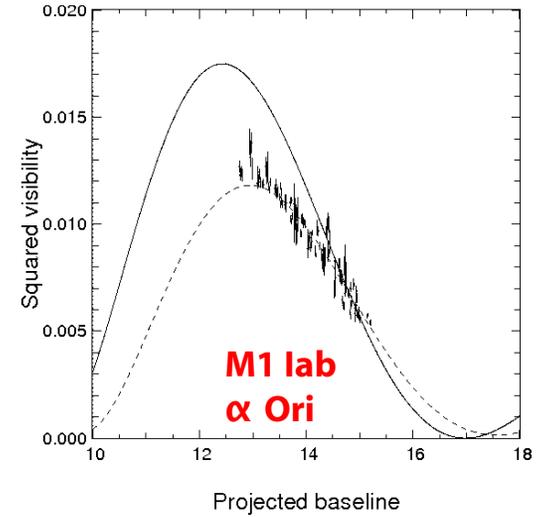
Che et al. (2011)



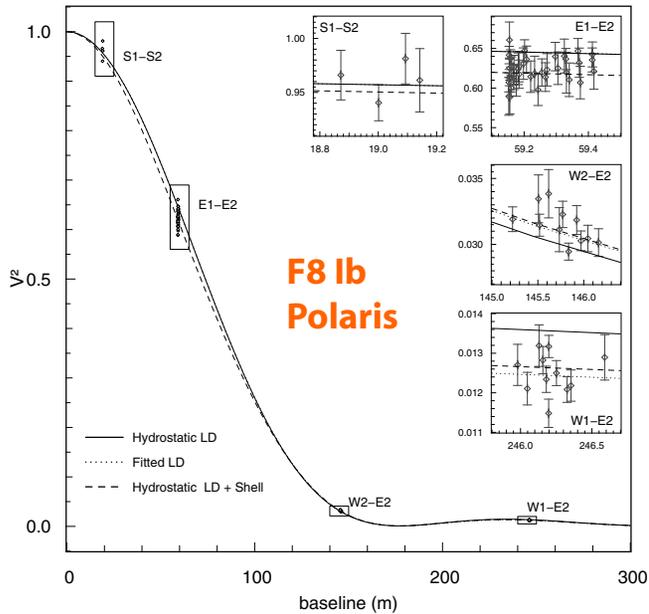
Mérand et al. (2010)



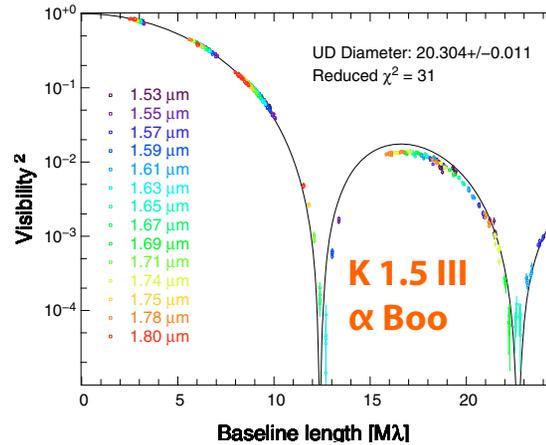
Xaubois et al. (2010)



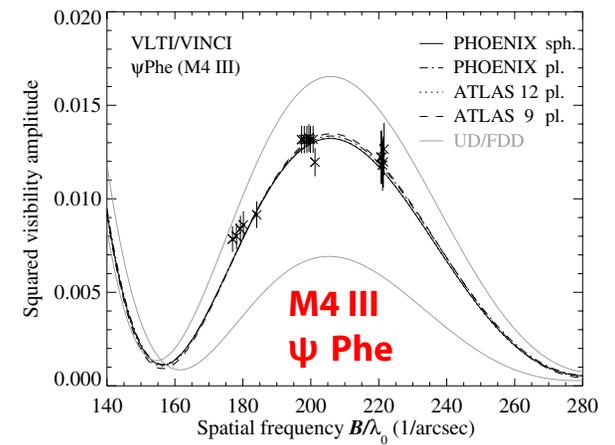
Mérand et al. (2006)



Lacour et al. (2008)

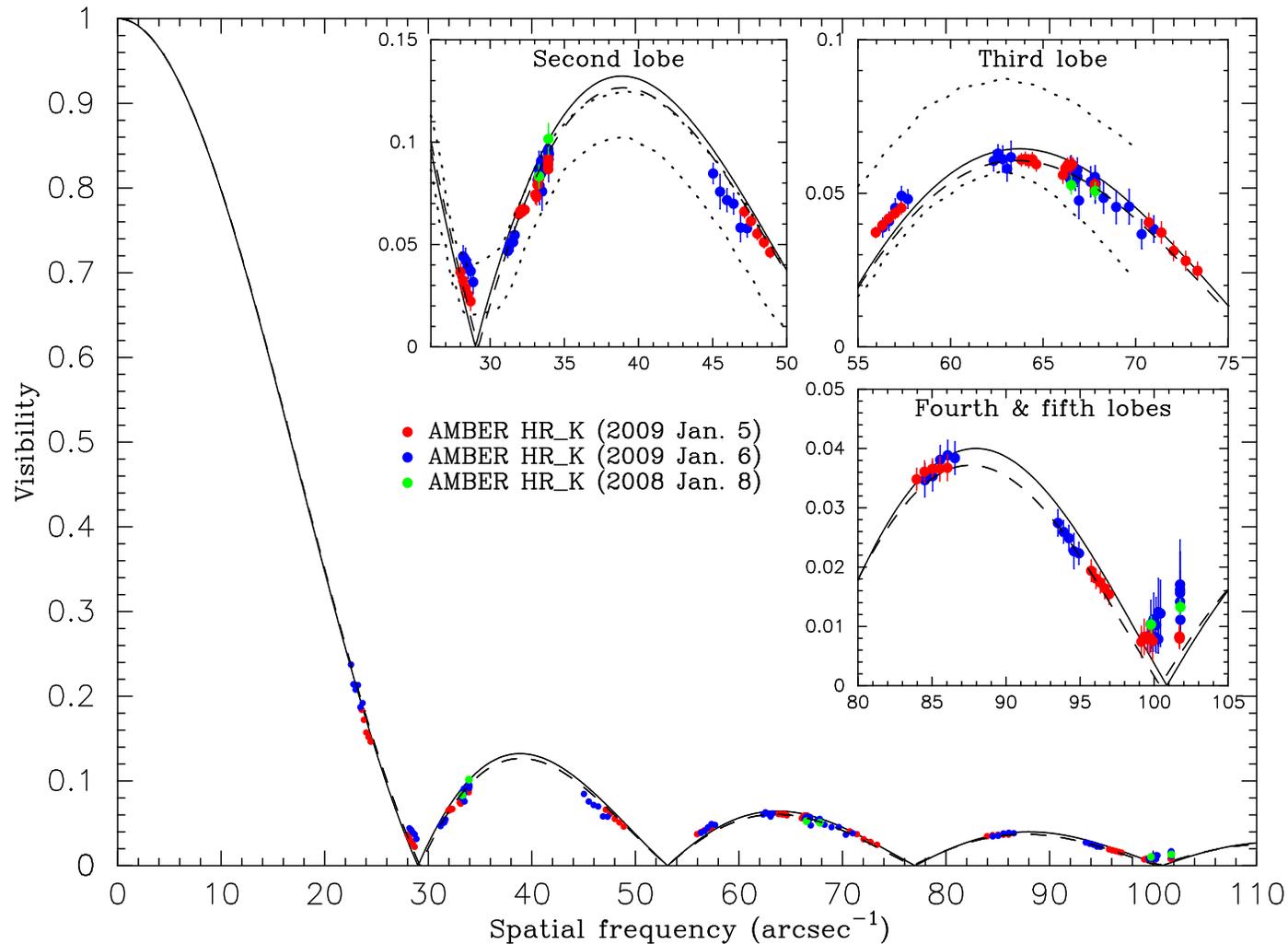


Wittkowski et al. (2004)



Imaging the dynamical atmosphere of the red supergiant Betelgeuse in the CO first overtone lines with VLT/AMBER \star

K. Ohnaka¹, G. Weigelt¹, F. Millour^{1,2}, K.-H. Hofmann¹, T. Driebe^{1,3}, D. Schertl¹, A. Chelli⁴, F. Massi⁵, R. Petrov², and Ph. Stee²



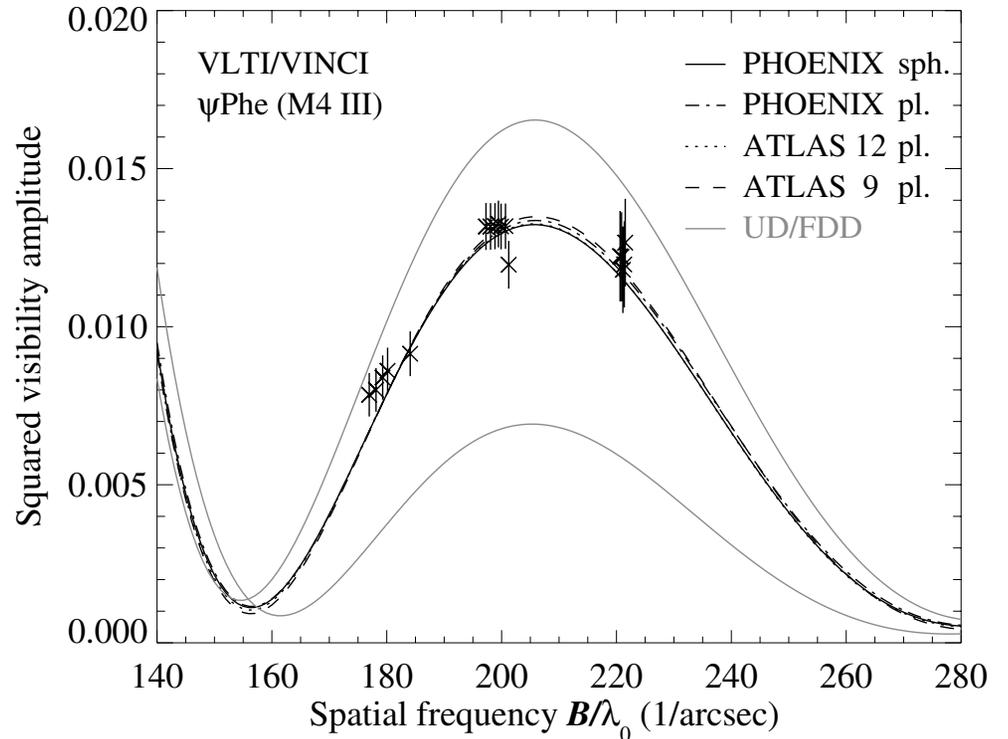
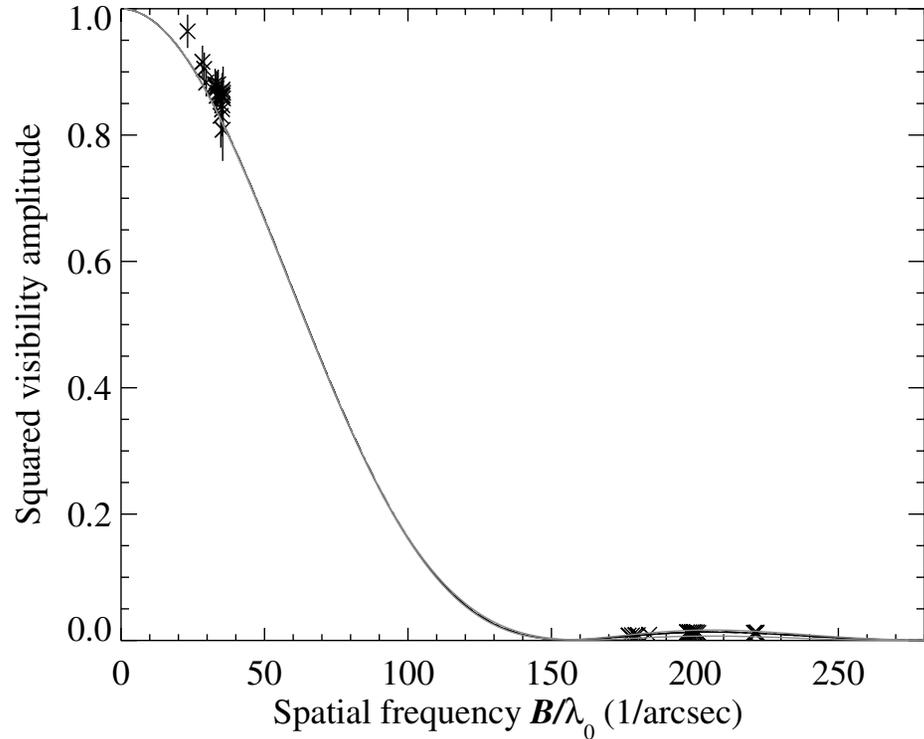
Ohnaka et al. (2011) *A&A*, 520, 163 [More on CO in α Ori @ 11:30!]

Second-lobe measurements from interferometry to date

M5 II	α Her	(Perrin et al. 2004)
M4.5 III	BY Boo	(Wittkowski et al. 2001)
M4 III	V416 Lac	(Wittkowski et al. 2001)
M4 III	ψ Phe	(Wittkowski et al. 2001; Wittkowski et al. 2004 (VLTI))
M1.5 III	α Cet	(Wittkowski et al. 2006) (VLTI)
M1Iab	α Ori	(Burns et al. 1997; Perrin et al. 2004; Xauboys et al. 2010, Ohnaka et al. 2011 (VLTI))
M0 III	γ Sge	(Wittkowski et al. 2001; Wittkowski et al. 2006 (VLTI))
K3 II	γ Aql	(Nordgen et al. 1999)
K2 III	α Ari	(Hajian et al. 1998)
K2 III	11 Lac	(Baines et al. 2010)
K1.5 III	α Boo	(Quirrenbach et al. 1996, Lacour et al. 2008)
K1 V	α Cen B	(Bigot et al. 2006) (VLTI)
K1 IV	γ Cep	(Baines et al. 2009)
K0 III	α Cas	(Hajian et al. 1998)
K0 III	η Ser	(Mérand et al. 2010)
F8 Ib	α UMi	(Mérand et al. 2006)
F5 Ib	α Per	(Mérand et al. 2007)
F5 IV-V	α CMi	(Aufdenberg et al. 2005)
F2 IV	β Cas	(Che et al. 2011)
F0 Ib	α Car	(Domiciano de Souza et al. 2008) (VLTI)
A7 V	α Aql	(Ohishi et al. 2004; Monnier et al. 2007)
A1 V	α CMa	(Hanbury Brown et al. 1974)
A0 V	α Lyr	(Peterson et al. 2006; Aufdenberg et al. 2006)

Tests of stellar model atmospheres by optical interferometry

VLT/VINCI limb-darkening measurements of the M4 giant ψ Phe[★]

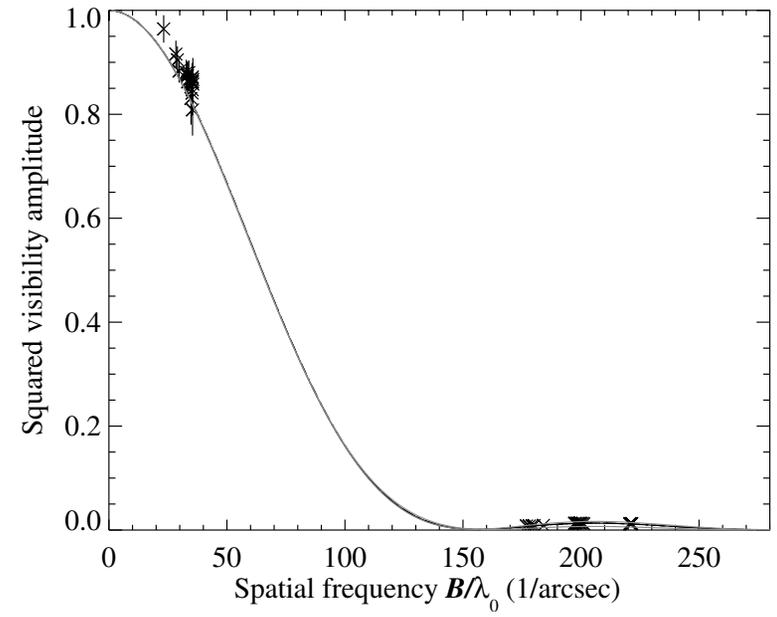


Wittkowski, Aufdenberg & Kervella (2004) A&A, 413, 711

Extracting a Diameter: Model Geometry Matters at the 1-2% level in K-band

T_{eff}	$\log g$	M	$C_{\text{Ross/LD}}$	θ_{LD}	χ^2_{ν}	θ_{Ross}
Spherical PHOENIX models:						
3550	0.7	1.3	0.9388	8.664	1.80	8.13
3500	0.7	1.3	0.9394	8.663	1.81	8.14
3600	0.7	1.3	0.9381	8.665	1.79	8.13
3550	0.5	1.3	0.9218	8.814	1.79	8.12
3550	1.0	1.3	0.9577	8.504	1.79	8.14
3550	0.7	1.0	0.9302	8.739	1.80	8.13
Plane-parallel PHOENIX model:						
3550	0.7	/	1	8.168	1.72	8.17
Plane-parallel ATLAS 12 model:						
3550	0.7	/	1	8.191	1.78	8.19
Plane-parallel ATLAS 9 models:						
3500	0.5	/	1	8.244	1.74	8.24
3500	1.0	/	1	8.243	1.73	8.24
3750	0.5	/	1	8.227	1.71	8.23
3750	1.0	/	1	8.228	1.71	8.23

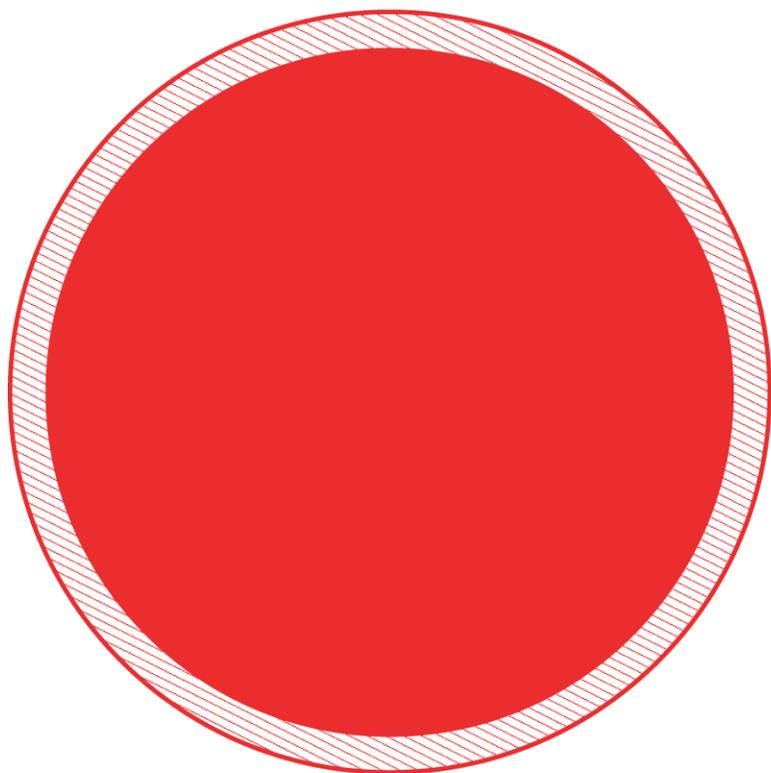
VLT/VINCI K-band



$$\frac{\Delta\theta}{\theta} \simeq 0.015$$

ψ Phe: Wittkowski, Aufdenberg & Kervella (2004) A&A, 413, 711

Spherical Atmospheres: same gravity, different mass



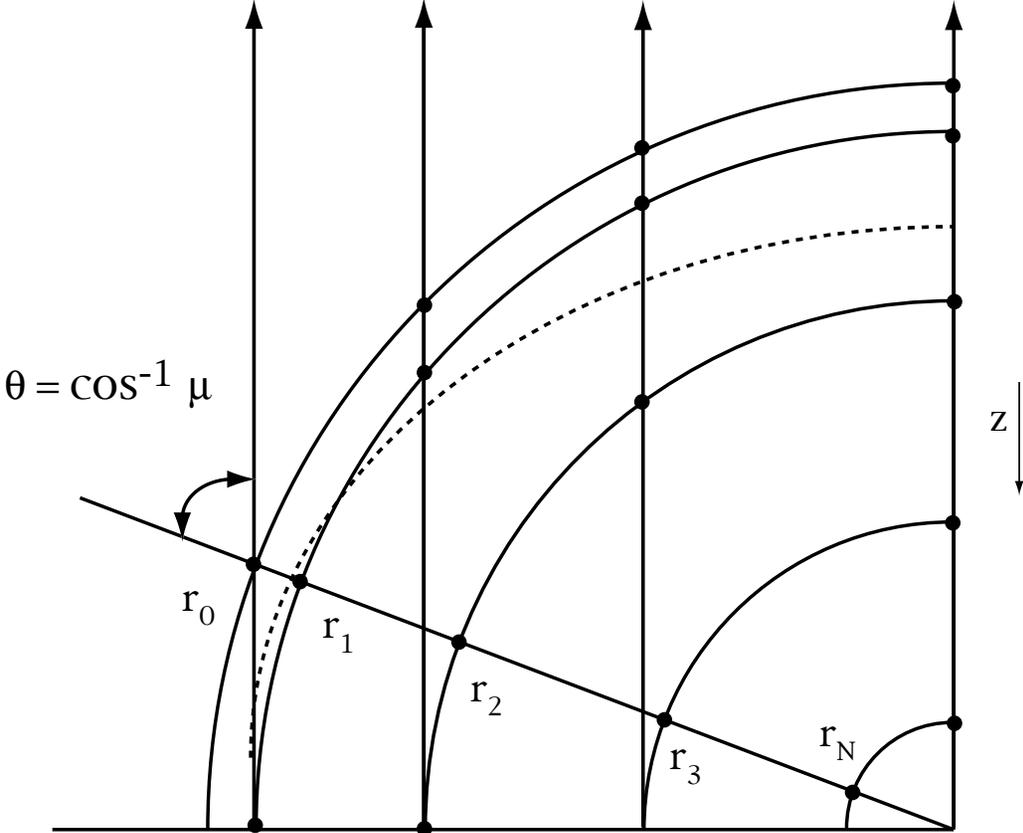
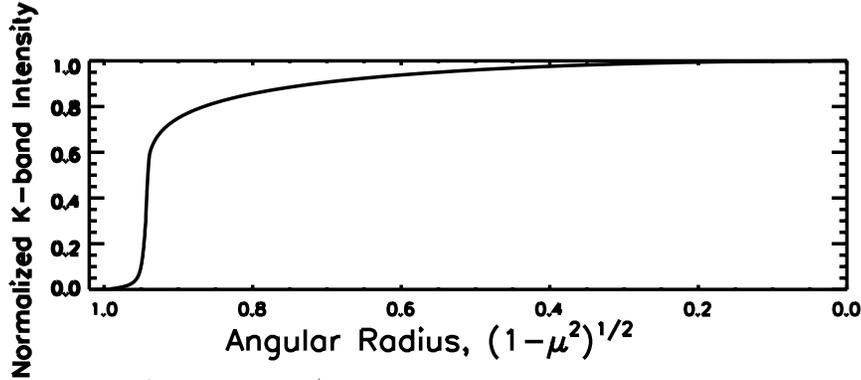
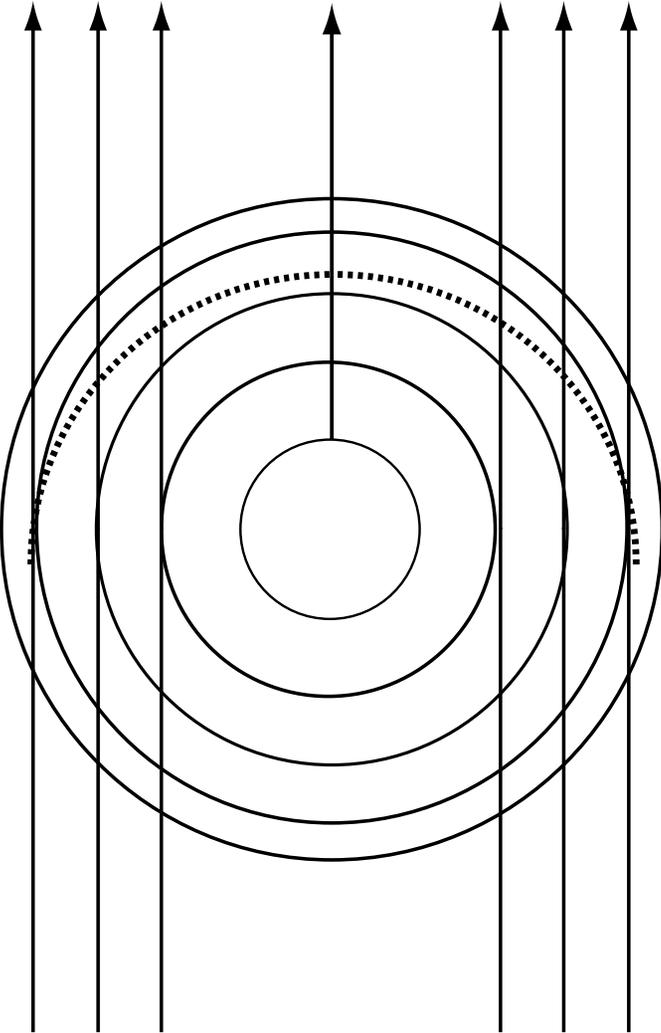
10 Msun



1 Msun

Two stars: same T_{eff} and $\log(g)$, different Mass

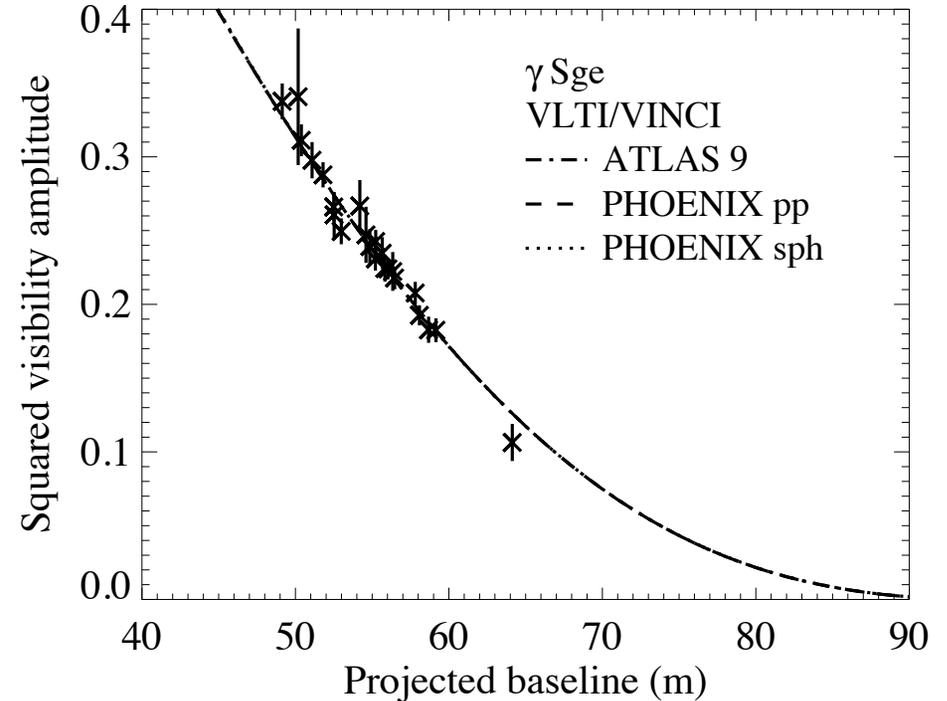
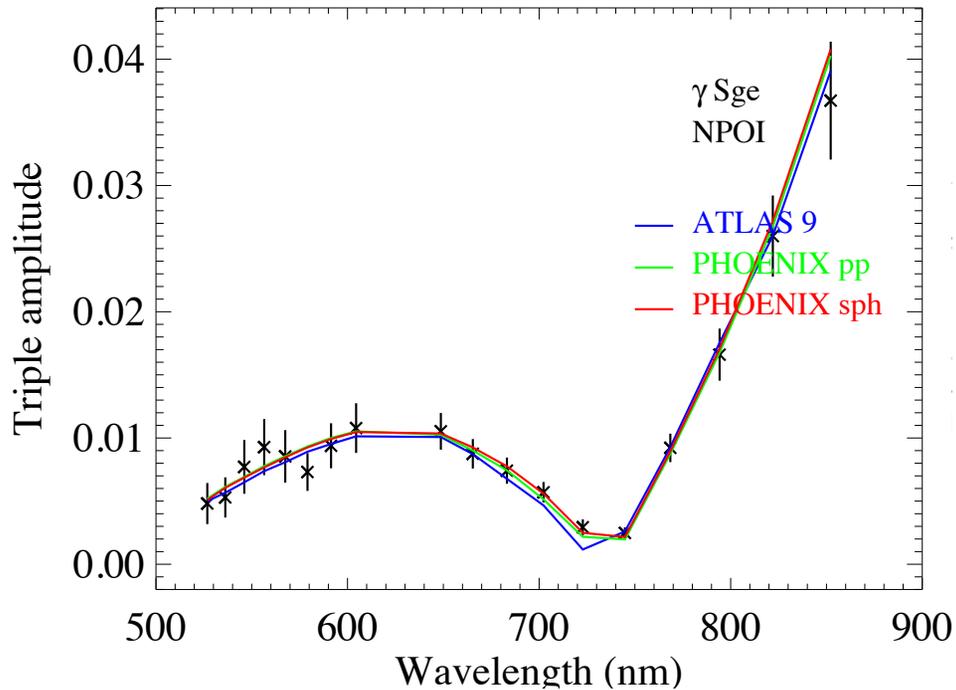
Spherical Geometry and Atmospheric Extension



Tests of stellar model atmospheres by optical interferometry

III. NPOI and VINCI interferometry of the M0 giant γ Sagittae covering $0.5\text{--}2.2\ \mu\text{m}^{\star,\star\star}$

M. Wittkowski¹, C. A. Hummel², J. P. Aufdenberg³, and V. Roccatagliata⁴



Spherical Model Yields Consistent Angular Diameter Across Optical/Near-IR for γ Sge (M0 III)

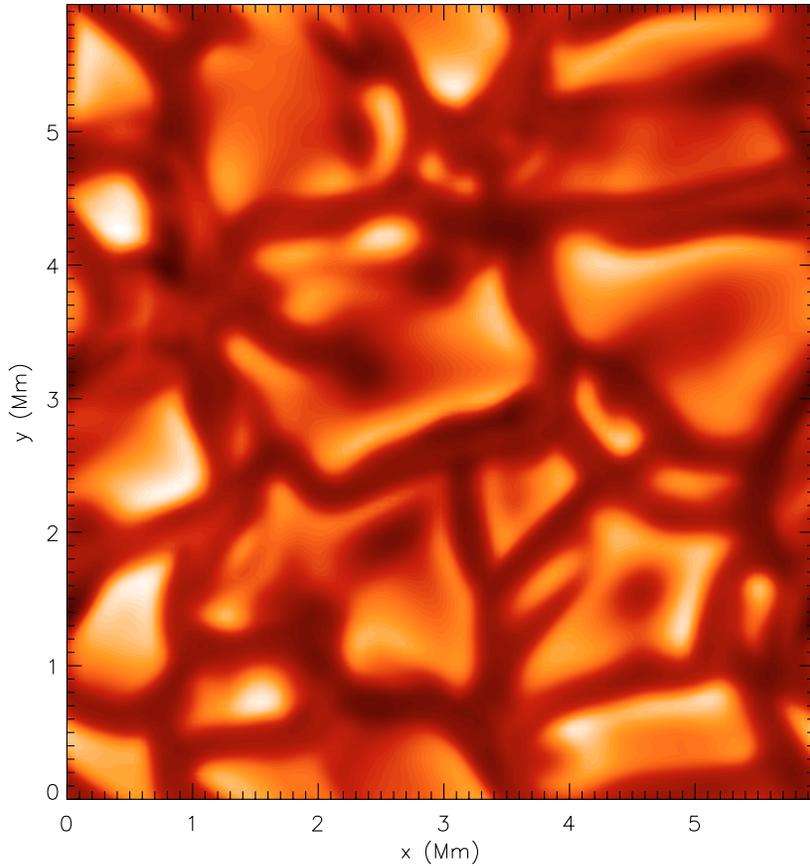
Model atmosphere	NPOI (526 nm to 852 nm)	VLTI/VINCI (2190 nm)
ATLAS 9, plane-parallel, $T_{\text{eff}} = 3750$ K, $\log g = 1.0$	$\Theta_{\text{LD}} = 6.18 \pm 0.06$ mas $\chi^2_{\nu} = 2.2$	$\Theta_{\text{LD}} = 6.05 \pm 0.02$ mas $\chi^2_{\nu} = 0.6$
PHOENIX, plane-parallel, $T_{\text{eff}} = 3750$ K, $\log g = 1.0$	$\Theta_{\text{LD}} = 6.11 \pm 0.06$ mas $\chi^2_{\nu} = 2.3$	$\Theta_{\text{LD}} = 6.05 \pm 0.02$ mas $\chi^2_{\nu} = 0.6$
PHOENIX, spherical, $T_{\text{eff}} = 3750$ K, $\log g = 1.0$, $M = 1.3 M_{\odot}$	$\Theta_{\text{LD}} = 6.30 \pm 0.06$ mas $\chi^2_{\nu} = 2.4$ $\Theta_{\text{Ross}} = 6.02 \pm 0.06$ mas	$\Theta_{\text{LD}} = 6.30 \pm 0.02$ mas $\chi^2_{\nu} = 0.6$ $\Theta_{\text{Ross}} = 6.02 \pm 0.02$ mas

**All atmosphere models have: $T_{\text{eff}} = 3750$ K, $\log(g) = 1.0$
but different geometries**

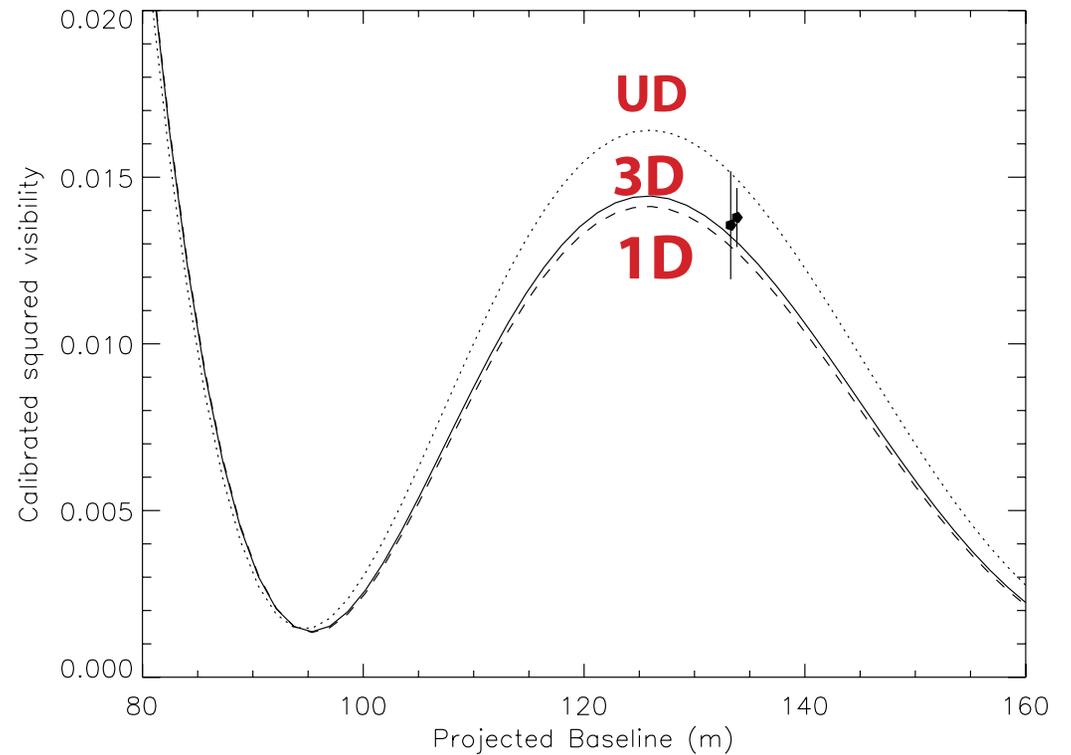
The limb darkening of α Centauri B

Matching 3D hydrodynamical models with interferometric measurements

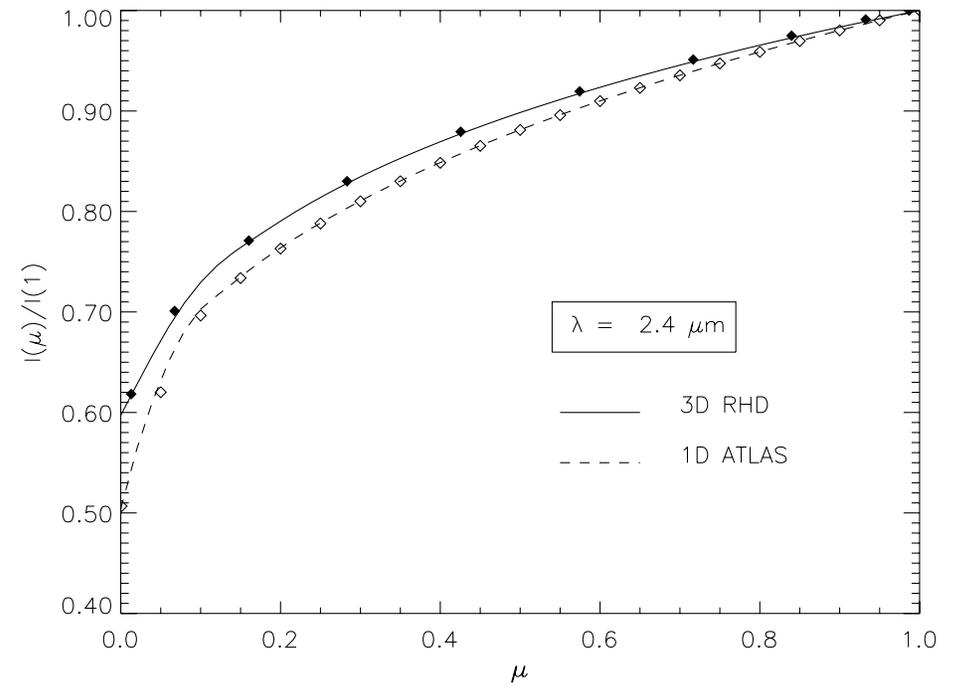
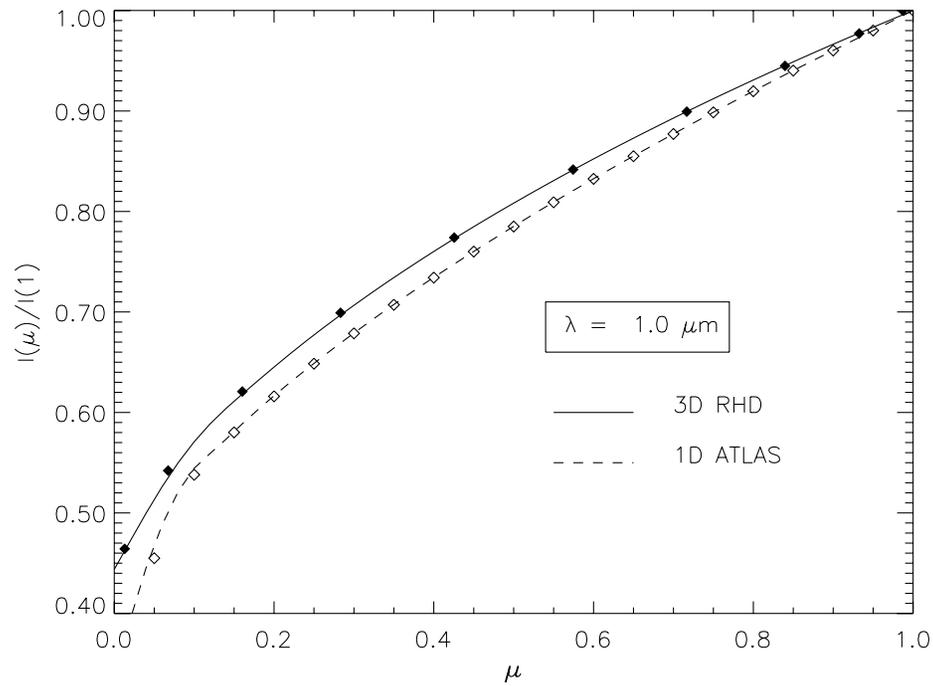
L. Bigot¹, P. Kervella², F. Thévenin¹, and D. Ségransan³



3D RHD Surface



3-D Radiative Hydrodynamic vs. 1-D Center-to-Limb Variations



- **Limb darkening weaker at longer wavelengths**
- **3D RHD models less limb darkened than (standard) 1-D models**

ON THE LIMB DARKENING, SPECTRAL ENERGY DISTRIBUTION, AND TEMPERATURE STRUCTURE OF PROCYON

J. P. AUFDENBERG¹

National Optical Astronomy Observatory, 950 North Cherry Avenue, Tucson, AZ 85719

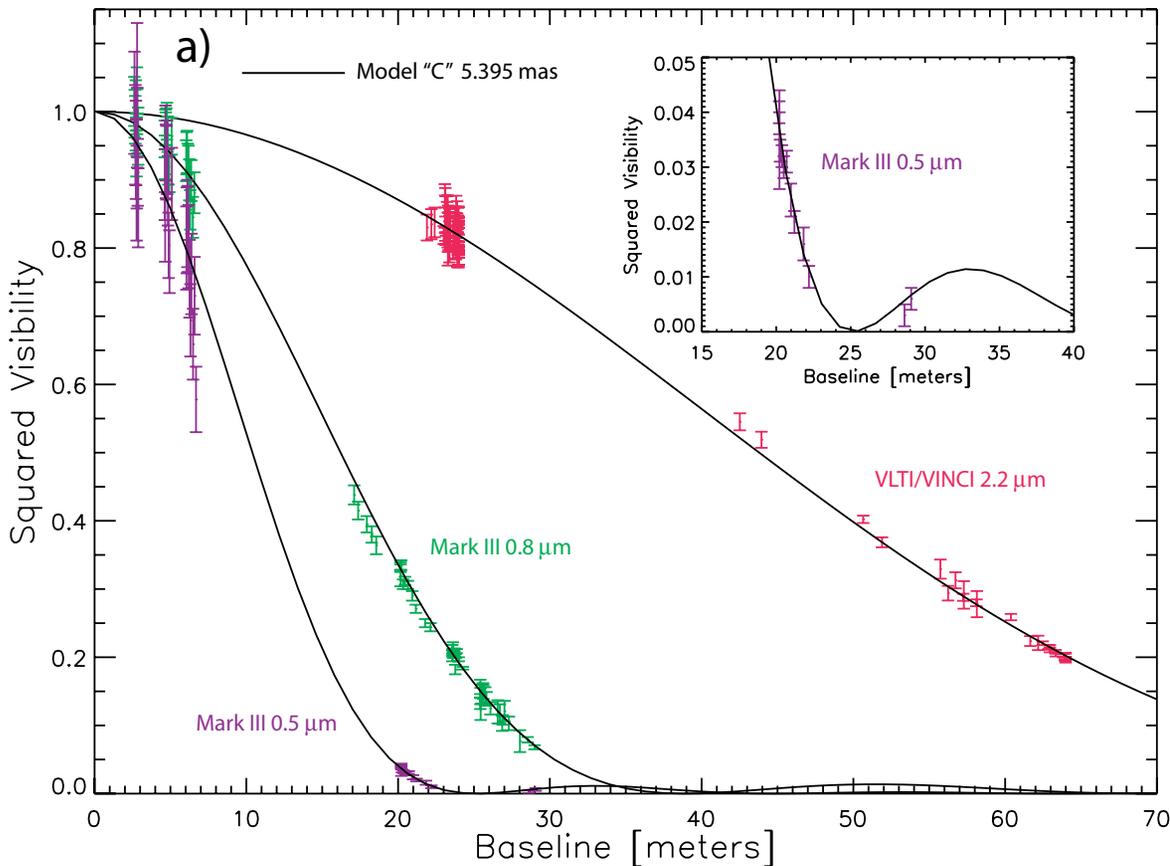
H.-G. LUDWIG

Lund Observatory, Lund University, Box 43, 22100 Lund, Sweden

AND

P. KERVELLA

LESIA, UMR 8109, Observatoire de Paris-Meudon, 5 place Jules Janssen, 92195 Meudon Cedex, France

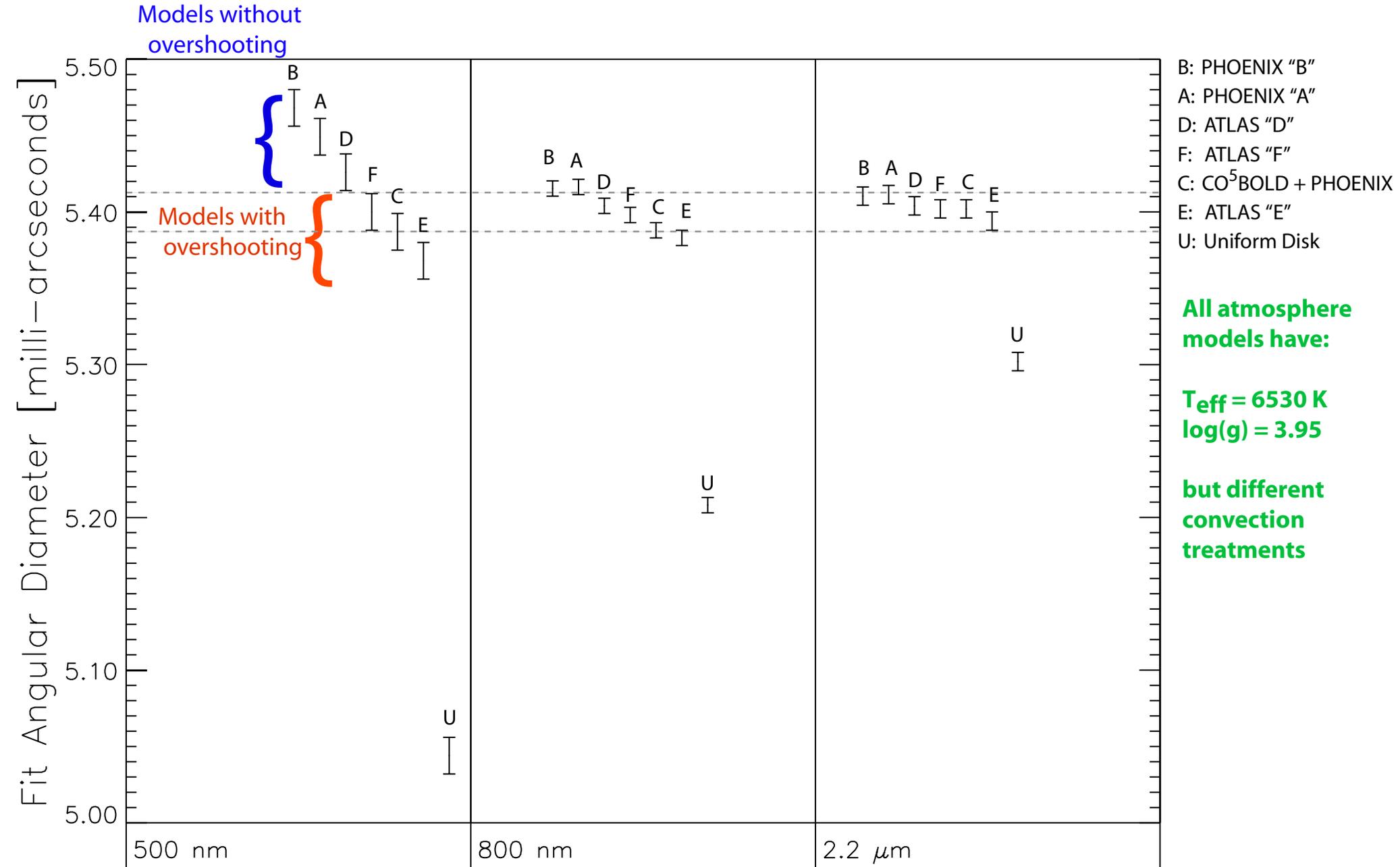


Procyon = α CMa (F5 IV-V)

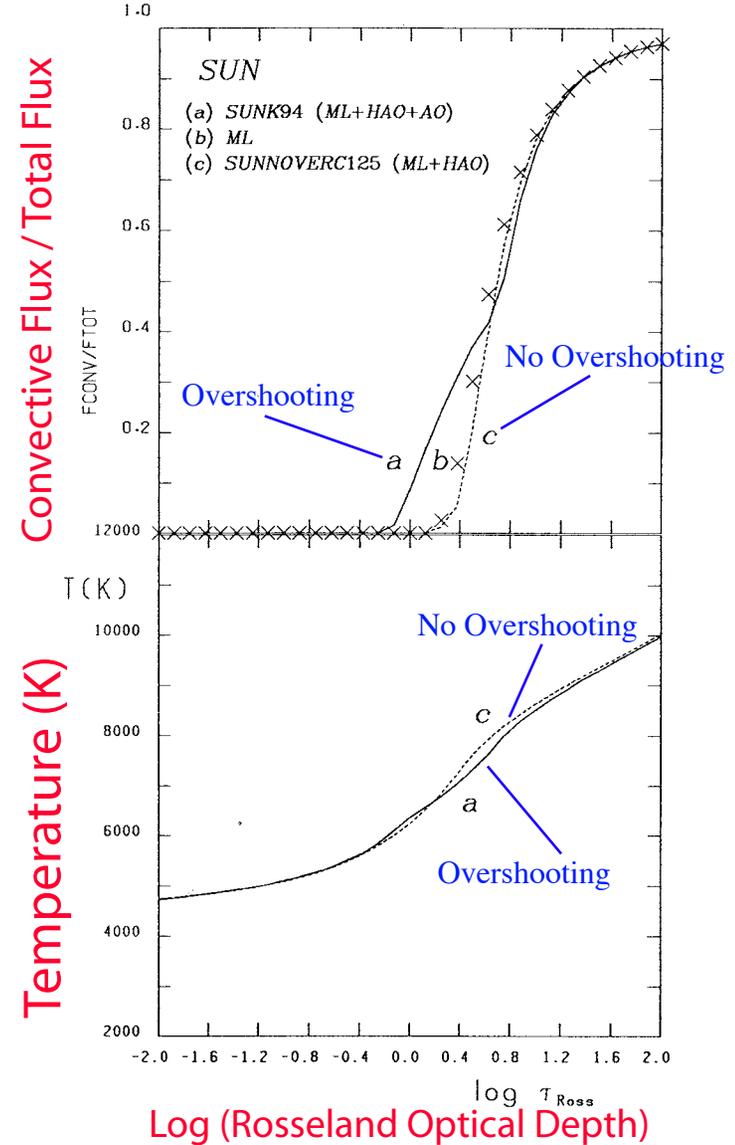
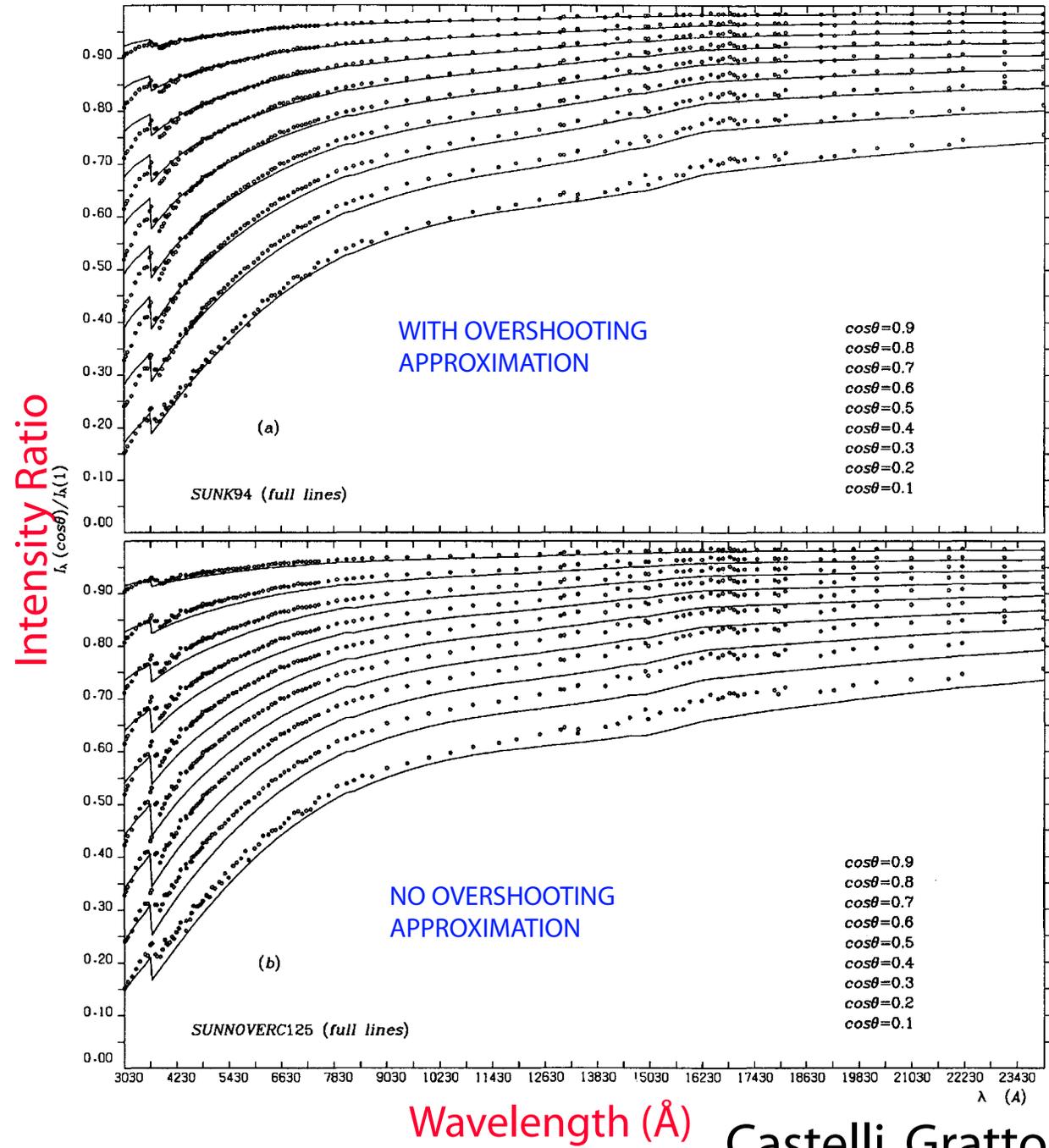
• Different UD angular diameters at 500 nm, 800nm, 2.2 μm reveal limb darkening

• Limb darkening most sensitive to temperature structure at shortest wavelength

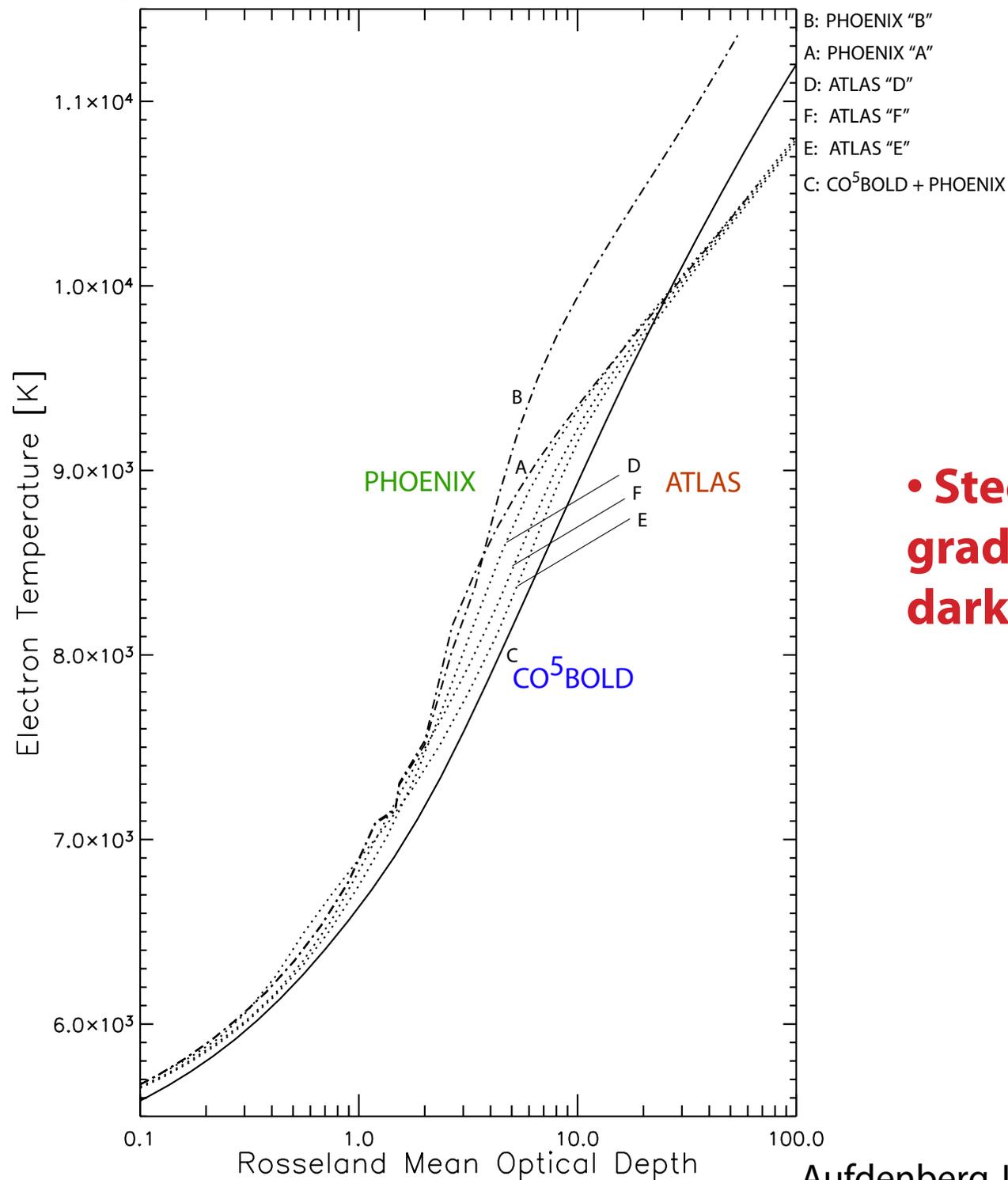
Procyon: Convection Effects on Limb Darkening



Limb Darkening and Convection in the Sun

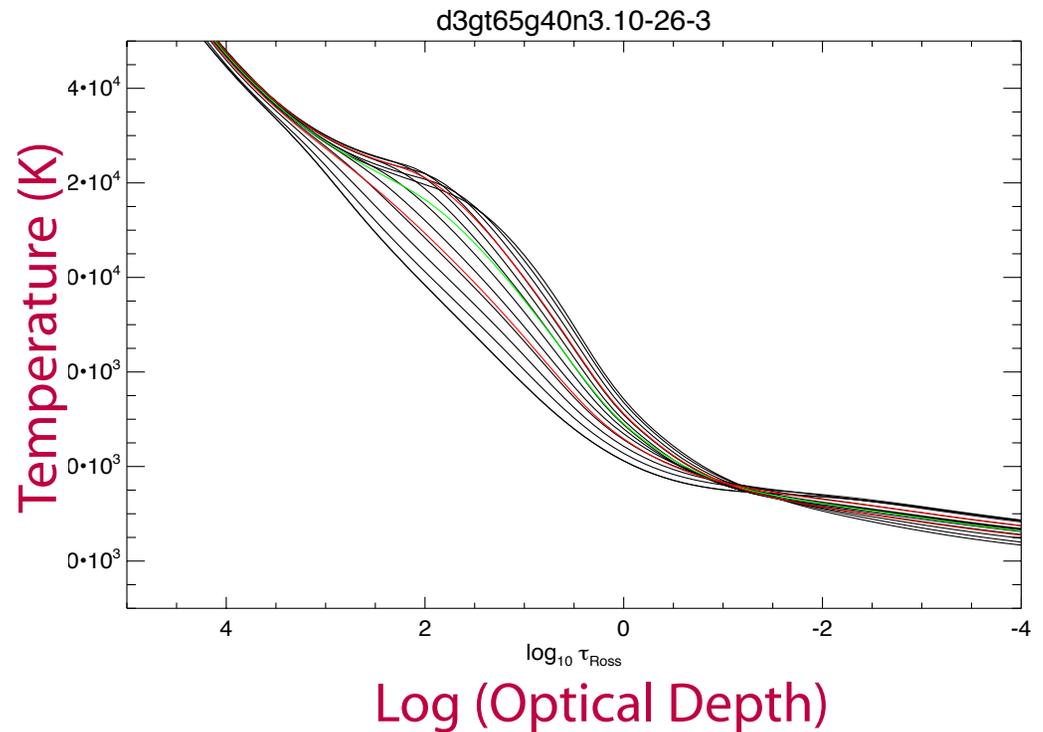
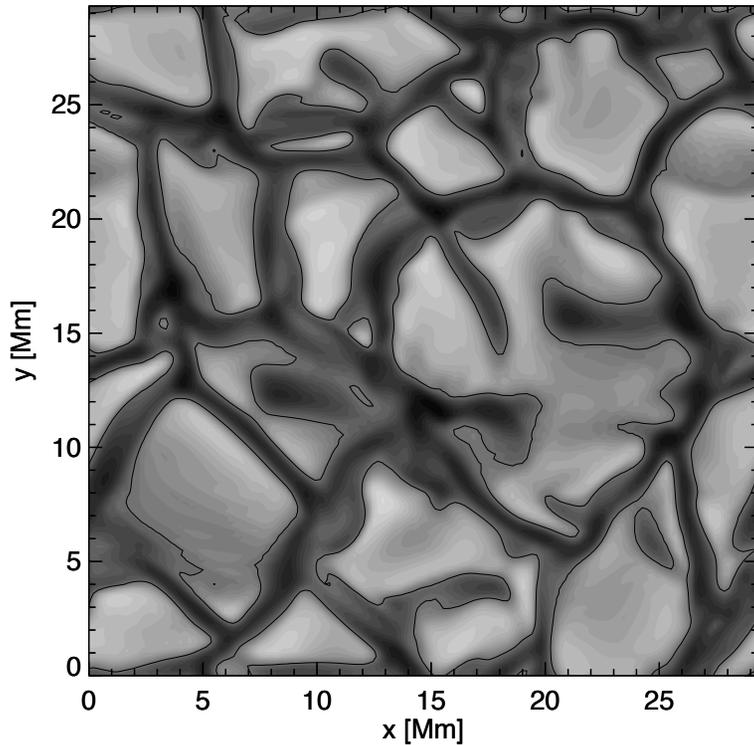


Temperature Structure Constrained by Interferometric Diameters



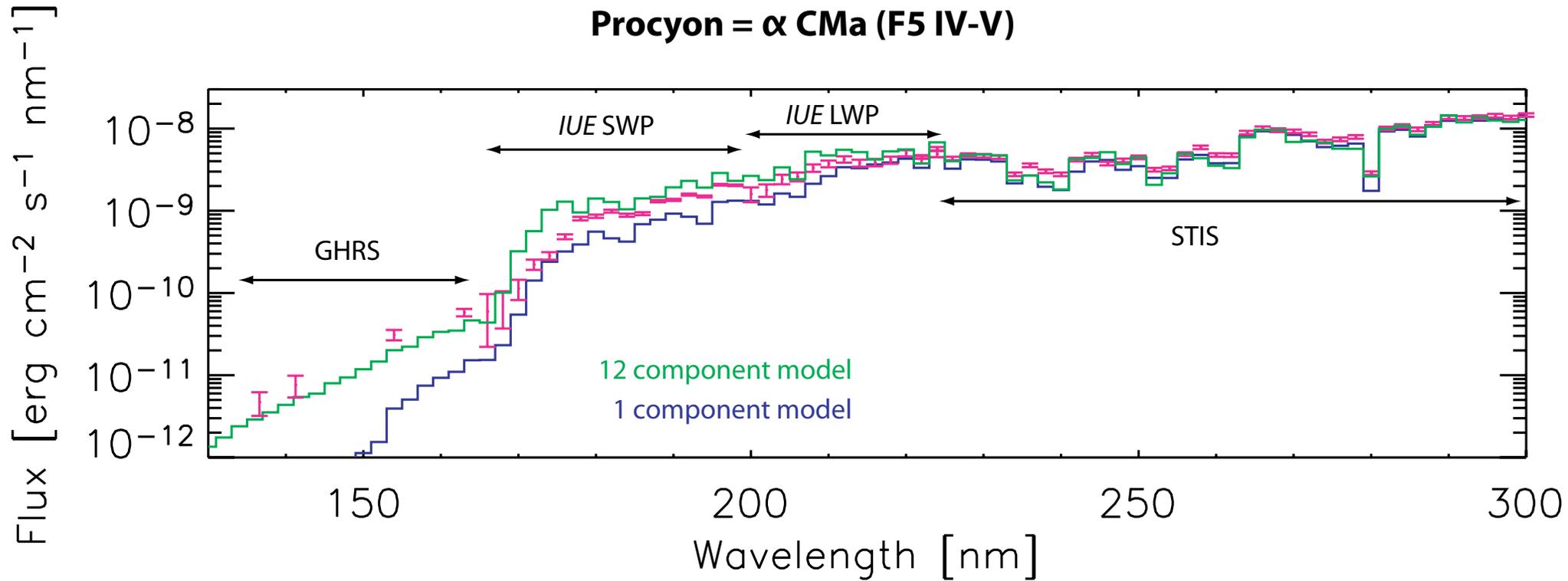
• **Steepness of temperature gradient determines limb darkening**

Stars up close, More Than One Temperature Structure



Hotter, rising granules have a warmer temperature structure than cooler, descending dark lanes.

Spectral Energy Distribution from 3-D Stellar Surfaces



- Multi-temperature component photosphere matches SED in the short ultraviolet, 1D model with overshooting does not

Solar spectral line strengths as a function of limb angle

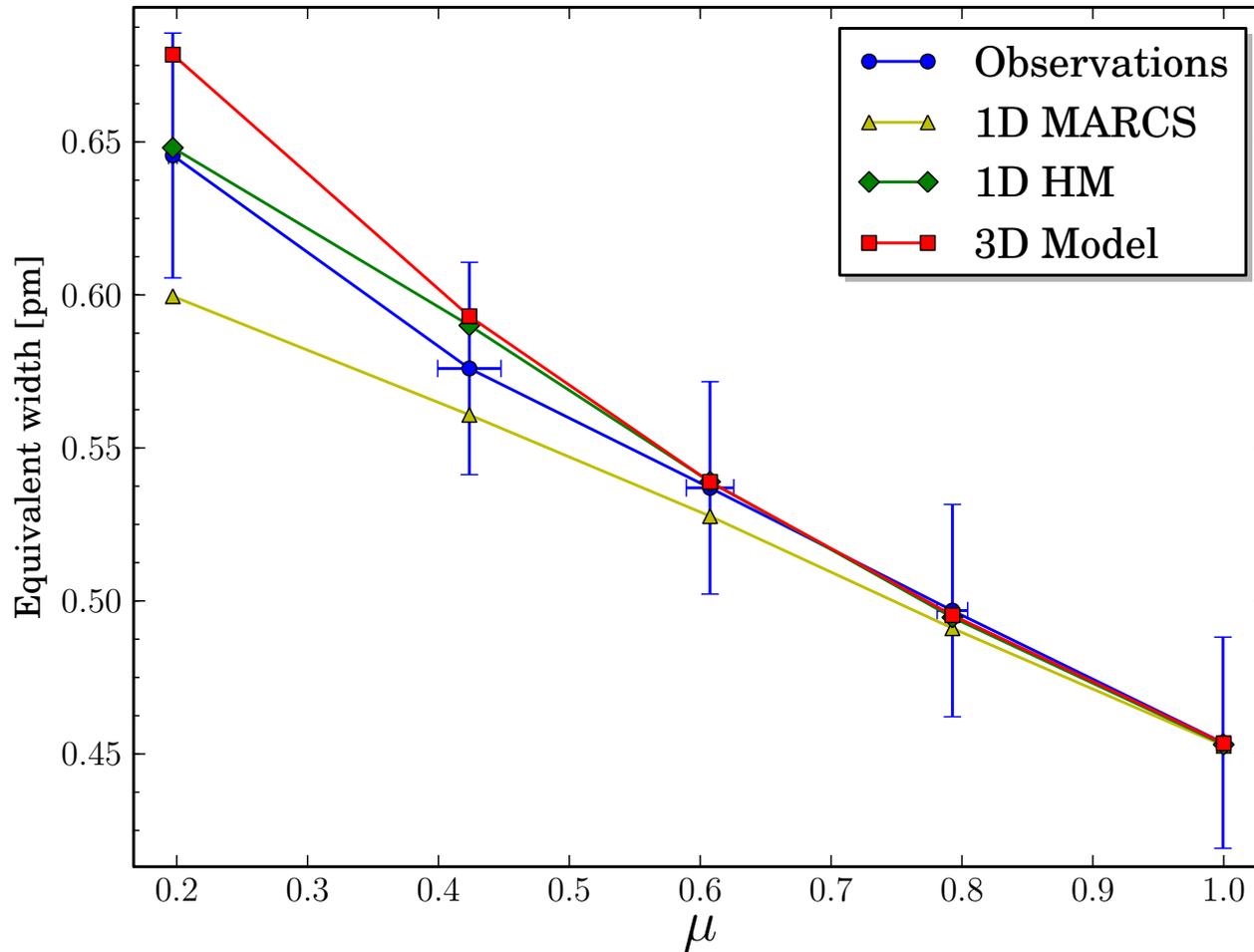
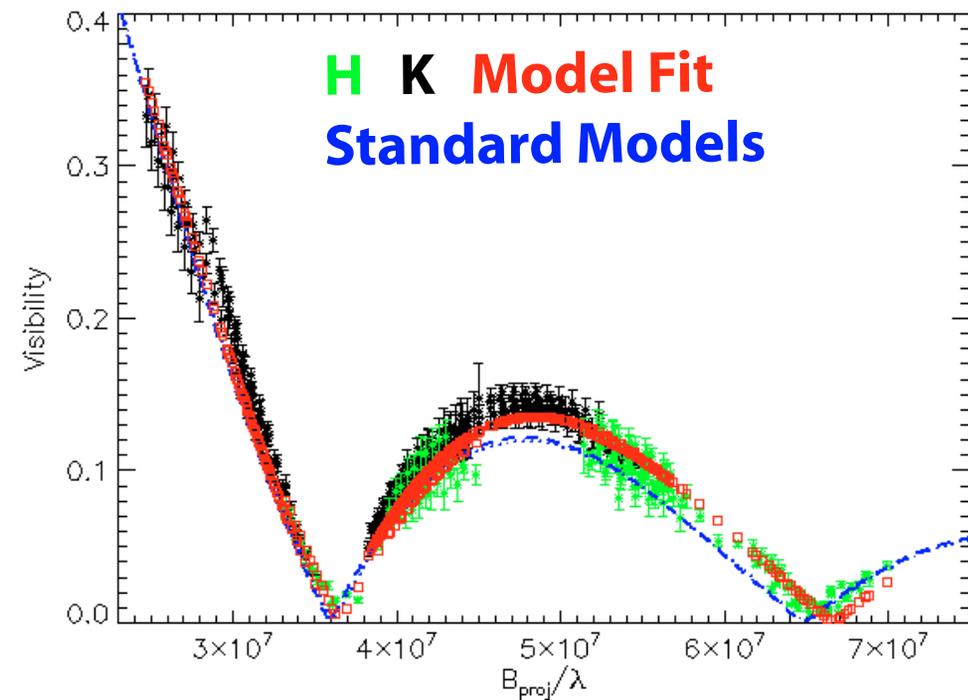


Fig. 9. Equivalent width vs. μ for the [O I]+Ni I 630.03 nm lines blend, for our observations and different models at different positions in the solar disk.

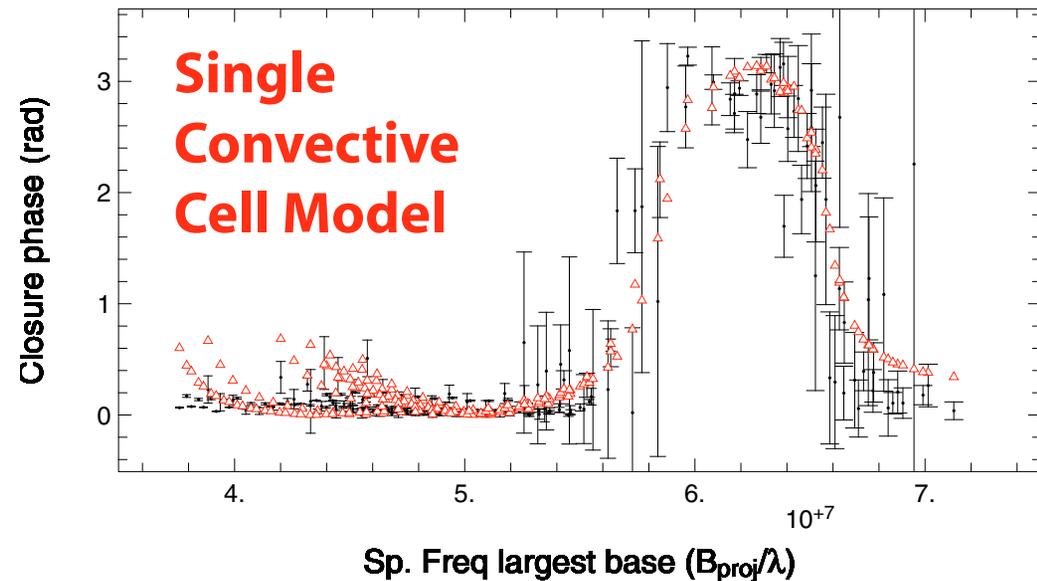
Diameter and photospheric structures of Canopus from AMBER/VLTI interferometry^{★,★★}

A. Domiciano de Souza¹, P. Bendjoya¹, F. Vakili¹, F. Millour², and R. G. Petrov¹

Canopus = α Car (F0Ib): H- and K -bands



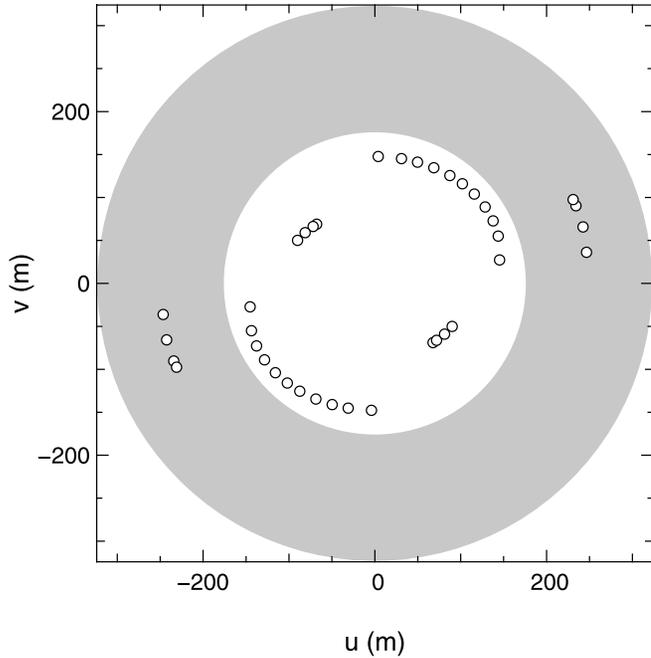
Non-Zero Closure Phase



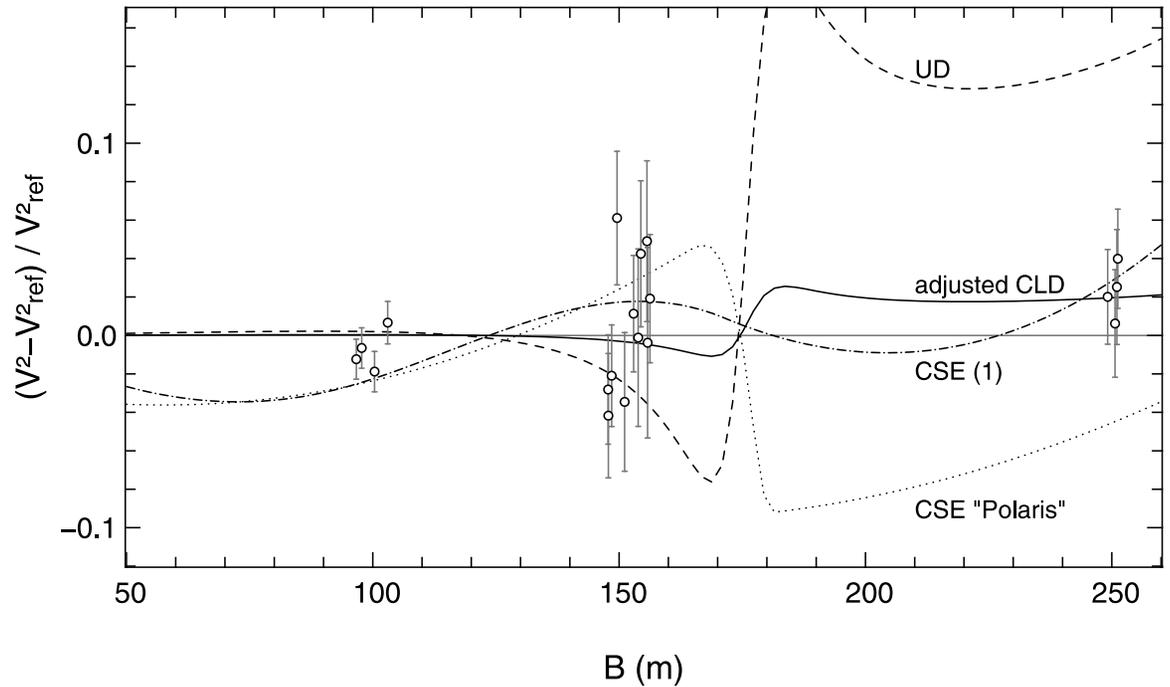
- Canopus less limb darkened than expected from standard models
- Evidence for presence for convective cell

EXTENDED ENVELOPES AROUND GALACTIC CEPHEIDS. III. γ OPHIUCHI AND α PERSEI
FROM NEAR-INFRARED INTERFEROMETRY WITH CHARA/FLUOR

α Per (F5Ib): K-band UV coverage



α Per (F5Ib): K-band Residuals to hydrostatic Model

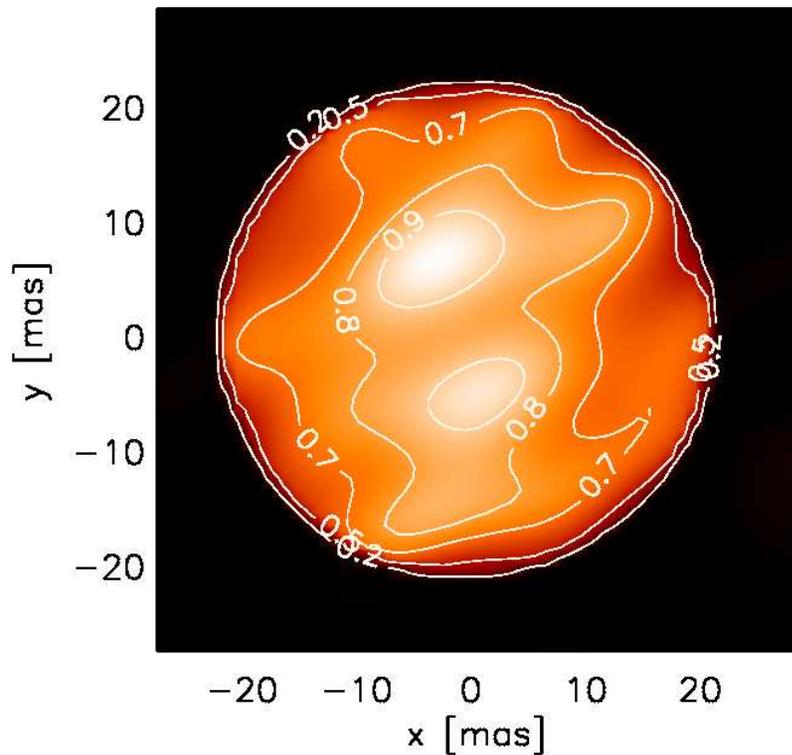


- α Per also less limb darkened than spherical hydrostatic models

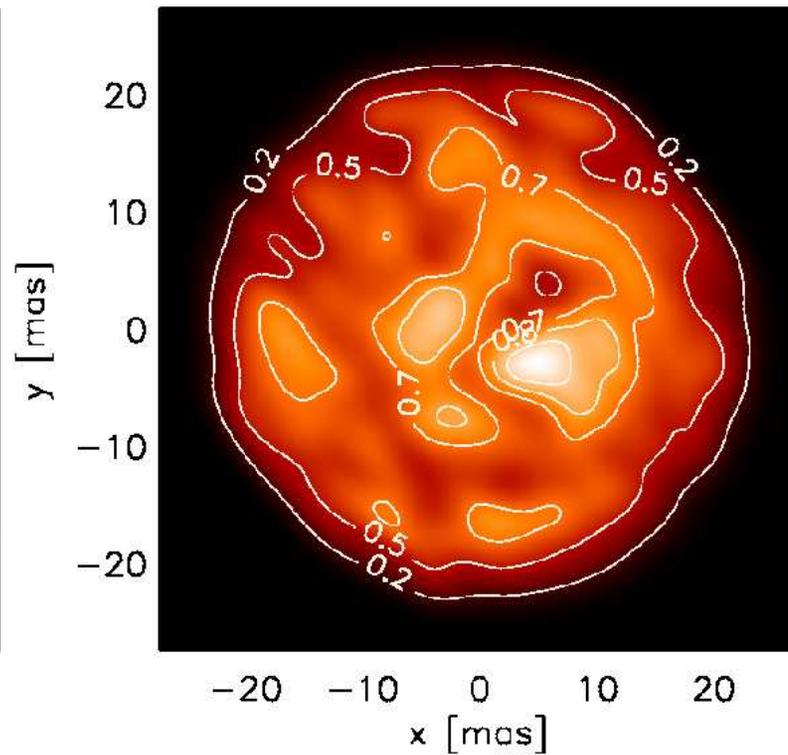
Radiative hydrodynamics simulations of red supergiant stars: II. simulations of convection on Betelgeuse match interferometric observations

A. Chiavassa^{1,2}, X. Haubois³, J. S. Young⁴, B. Plez², E. Josselin², G. Perrin³, and B. Freytag^{5,6}

IOTA data image reconstruction

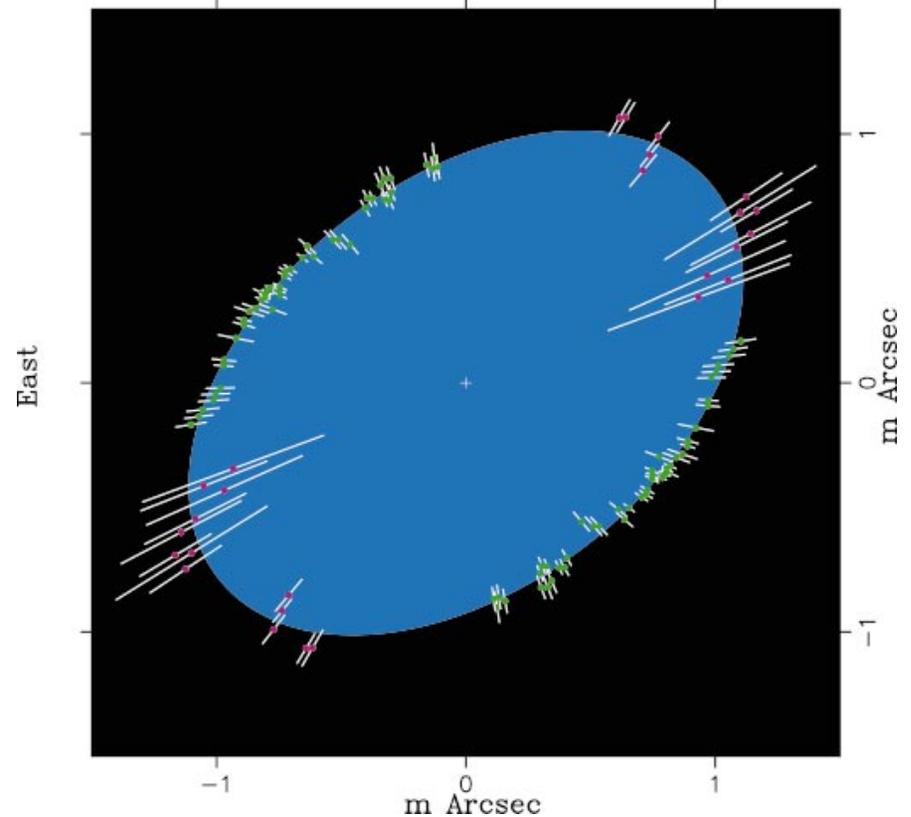
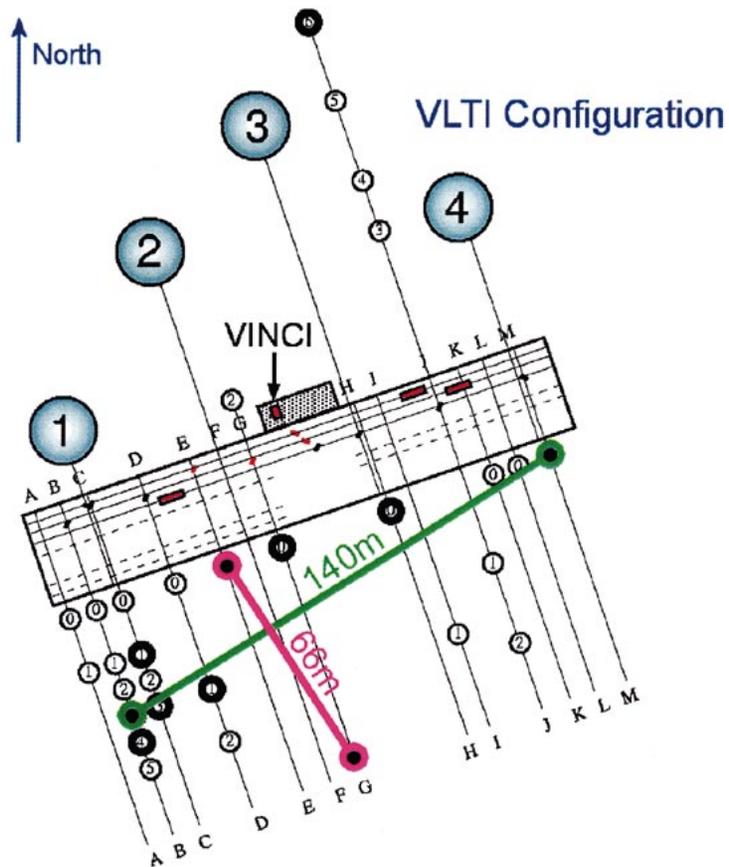


3D Simulation/Best match to V^2 and Closure phase data



The spinning-top Be star Achernar from VLTI-VINCI

A. Domiciano de Souza¹, P. Kervella², S. Jankov³, L. Abe¹, F. Vakili^{1,3}, E. di Folco⁴, and F. Paresce⁴

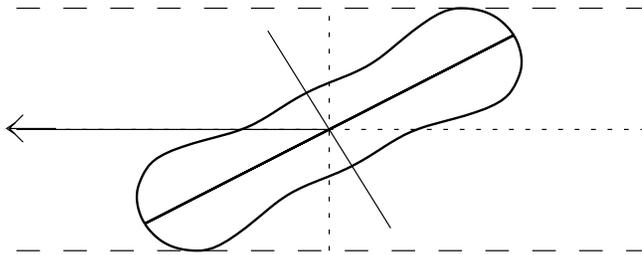


*Disk of **Achernar** (B3 Vpe) resolved as ellipsoid by VLTI (Axial ratio: 1.56 ± 0.05)

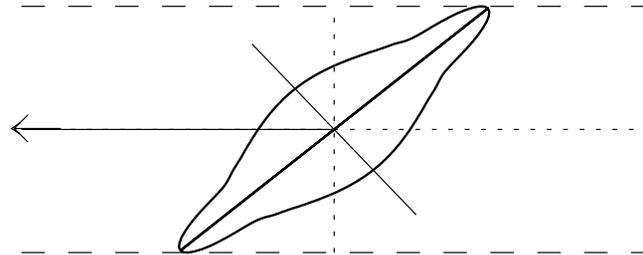
Theory of Rotating Stars Revitalized by Observations

Models for Achernar with Differential Rotation

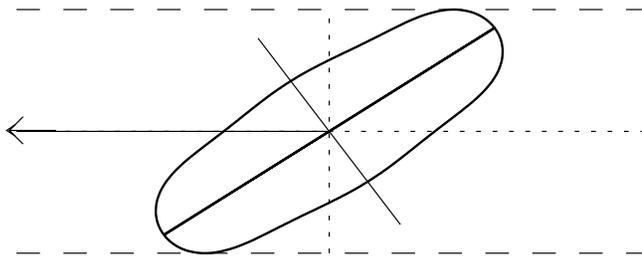
(A) $M=6 M_{\odot}$, $R_{eq}=12.19 R_{\odot}$
 $i=61^{\circ}$



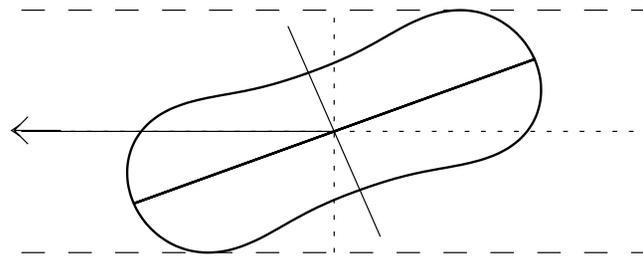
(B) $M=9 M_{\odot}$, $R_{eq}=11.73 R_{\odot}$
 $i=49^{\circ}$



(C) $M=12 M_{\odot}$, $R_{eq}=11.57 R_{\odot}$
 $i=55^{\circ}$



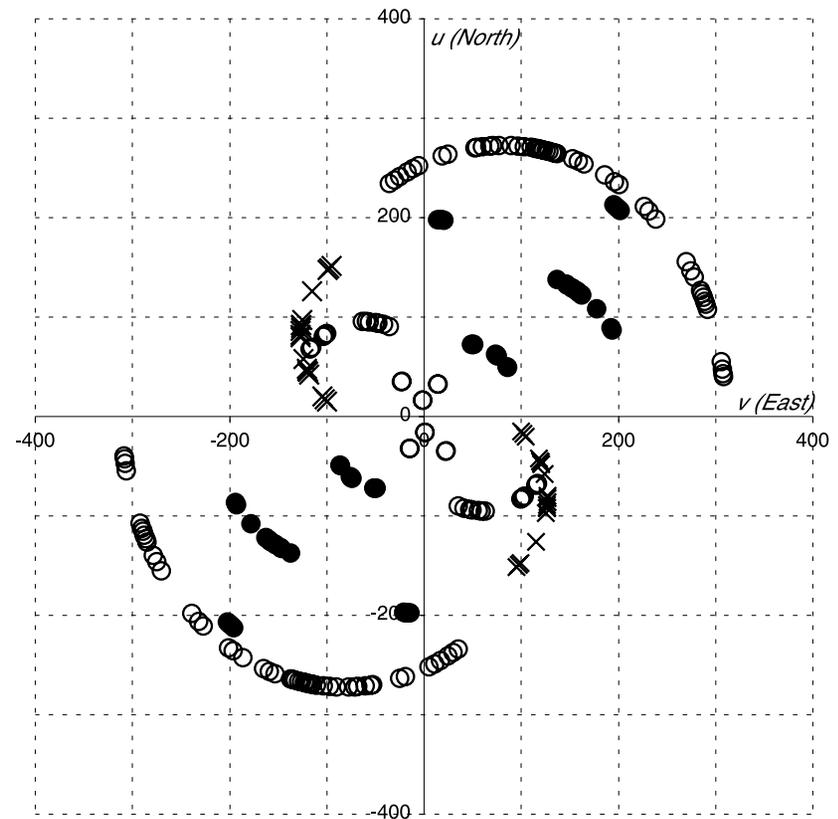
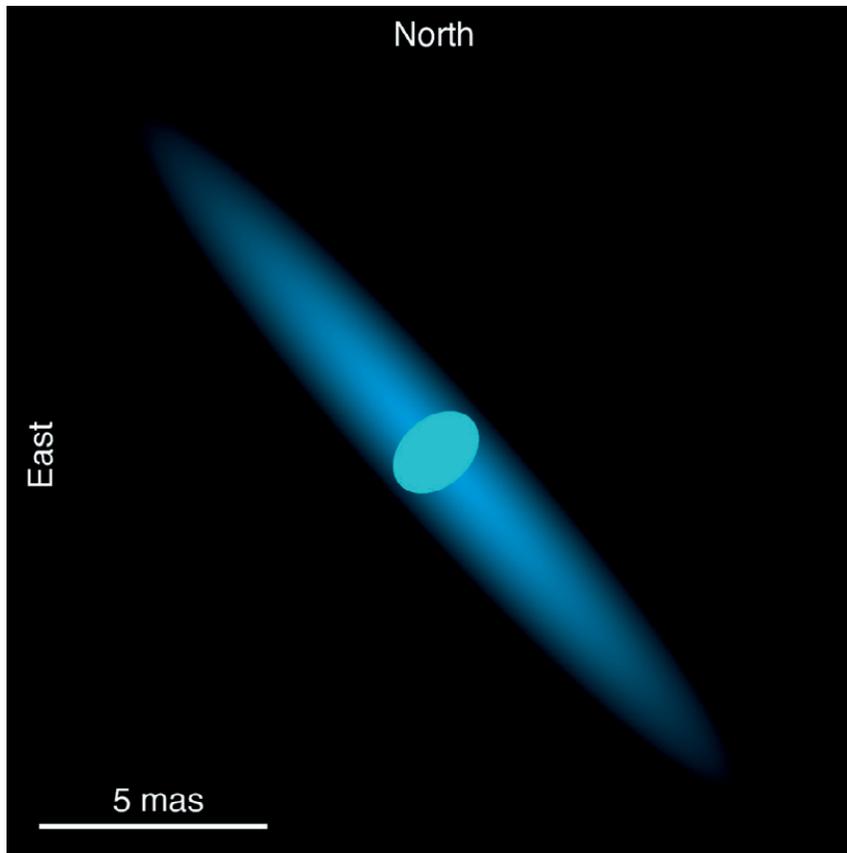
(D) $M=15 M_{\odot}$, $R_{eq}=12.41 R_{\odot}$
 $i=68^{\circ}$



The polar wind of the fast rotating Be star Achernar

VINCI/VLTI interferometric observations of an elongated polar envelope

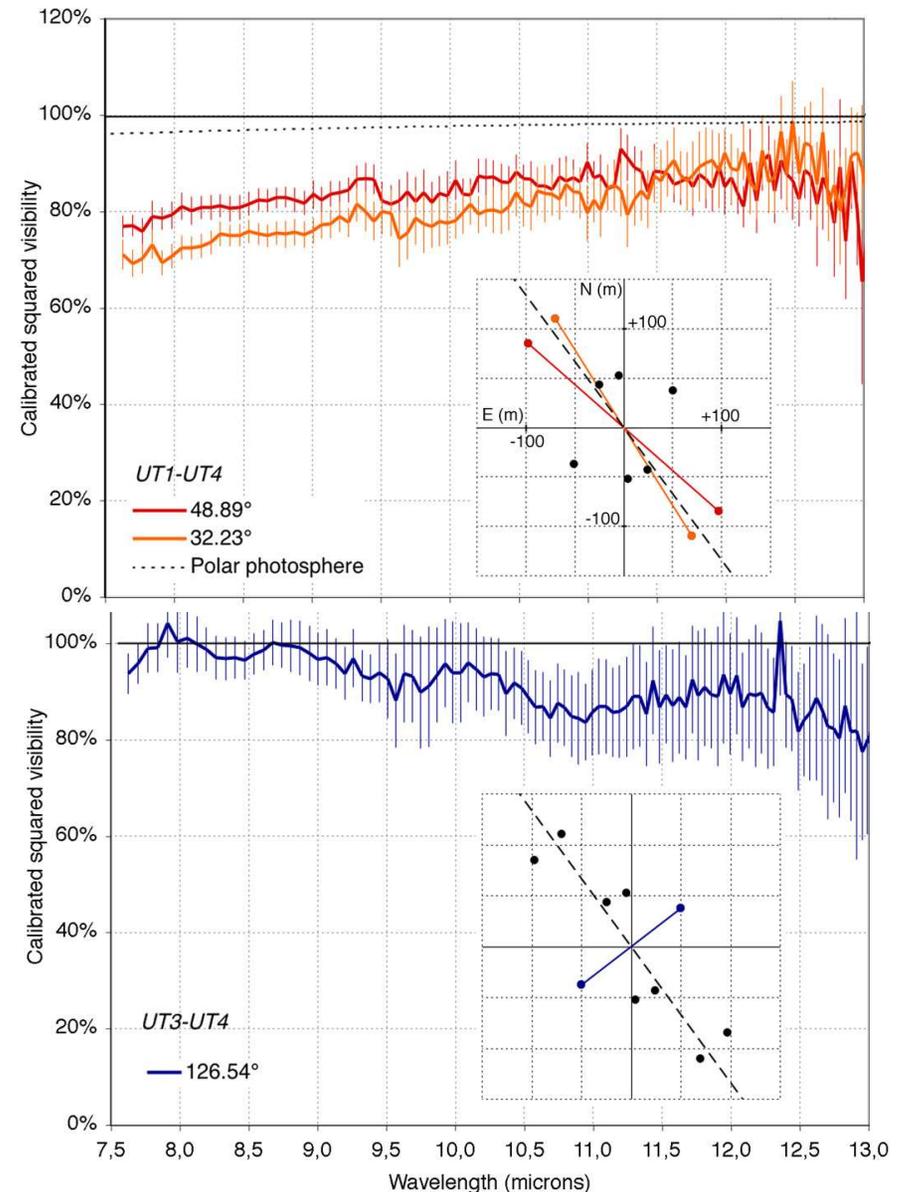
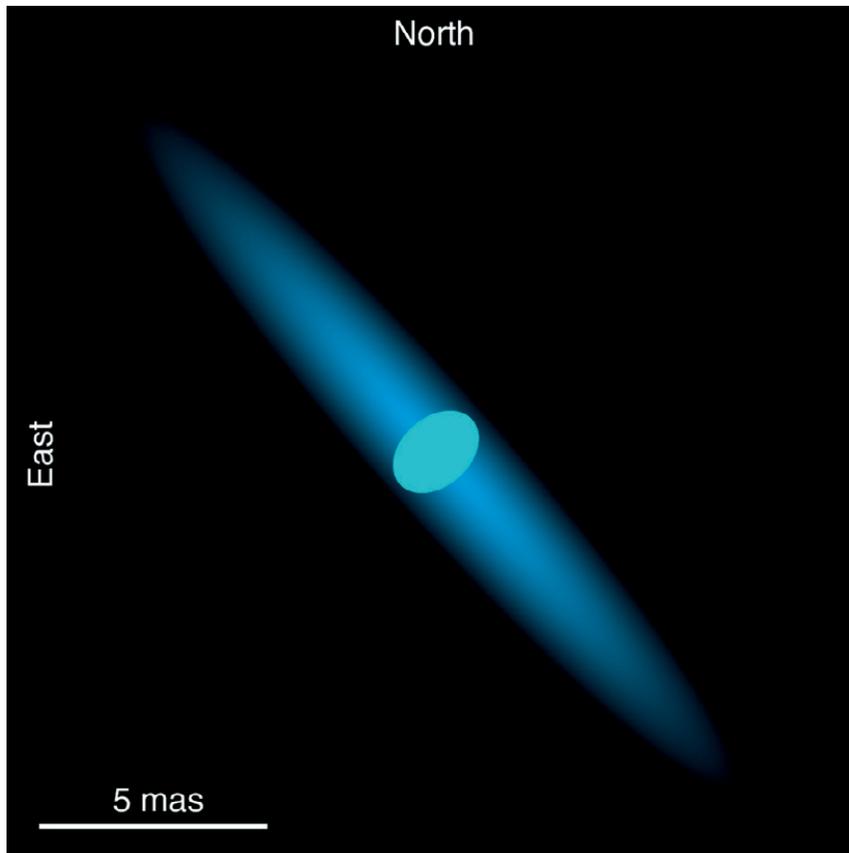
P. Kervella¹ and A. Domiciano de Souza^{2,3}



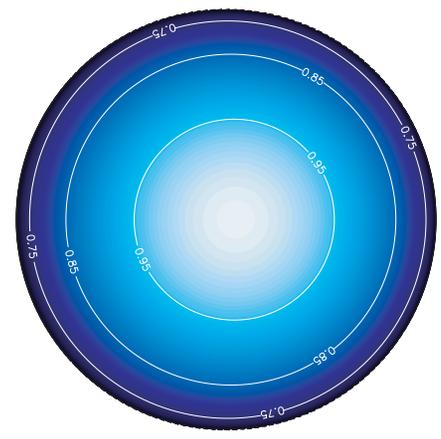
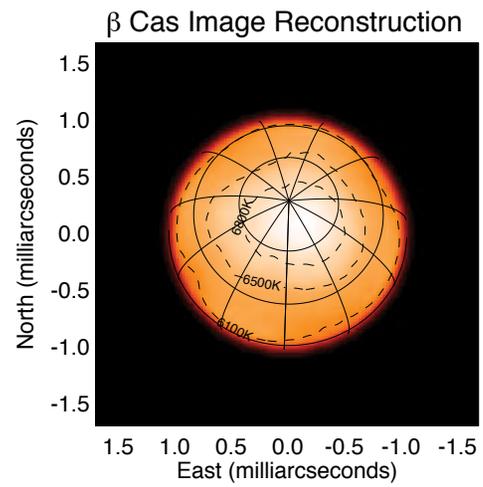
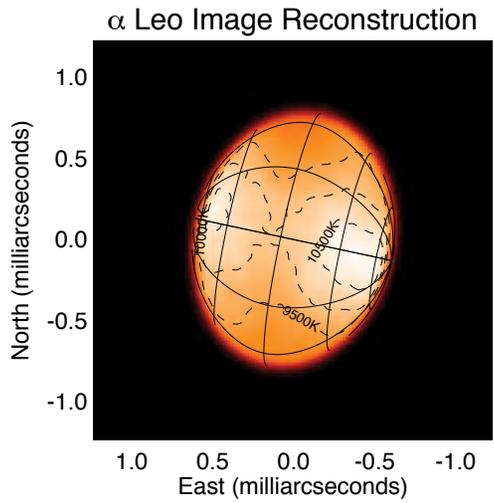
The environment of the fast rotating star Achernar★

II. Thermal infrared interferometry with VLT/MIDI

P. Kervella¹, A. Domiciano de Souza², S. Kanaan², A. Meilland³, A. Spang², and Ph. Stee²



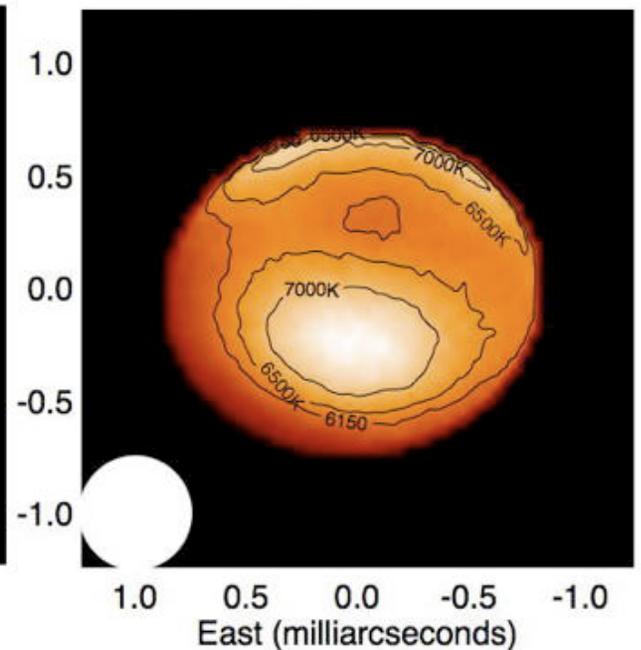
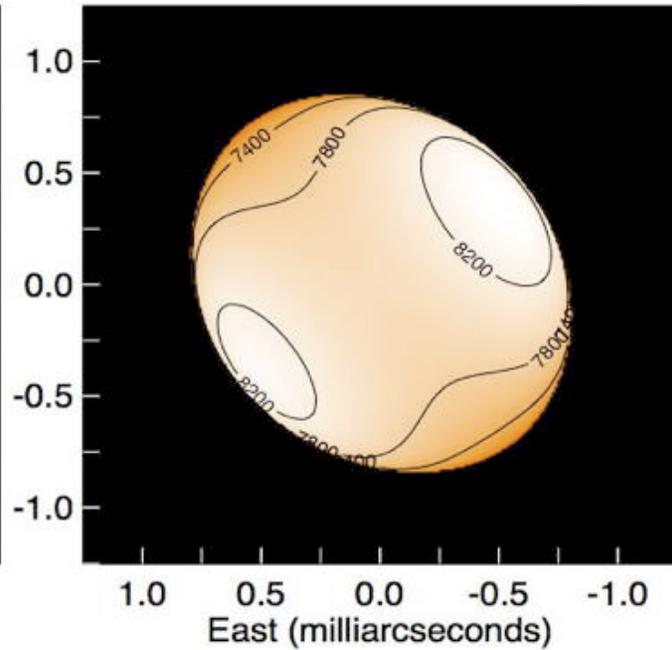
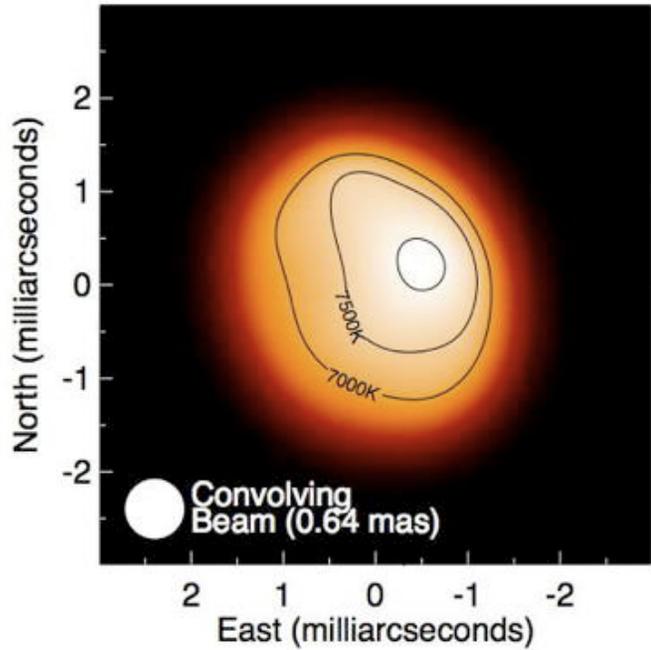
Additional Resolved Rapid Rotating Stars from Interferometry



*Disk of **Regulus** (B7 V) resolved as ellipsoid by CHARA (McAlister et al. 2005, Che et al. 2011).

*Disk of **Caph** (F2 IV) resolved as ellipsoid by CHARA/MIRC (Che et al. 2011).

*Pole of **Vega** (A0 V) resolved by CHARA (Aufdenberg et al. 2006).



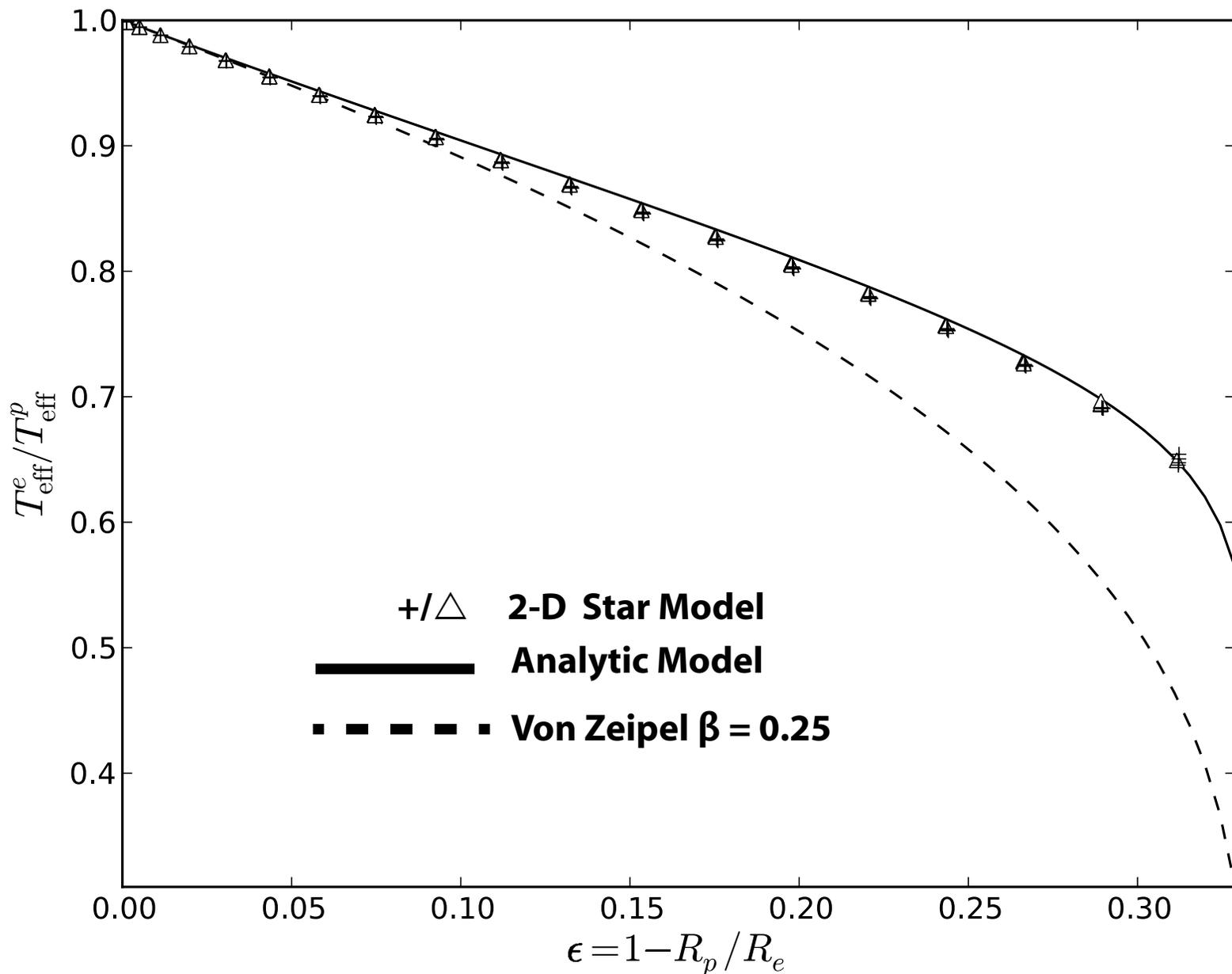
*Disk of **Altair** (A7 V) resolved by CHARA (J. Monnier et al. 2007).

*Disk of **Alderamin** (A7 V) resolved by CHARA (M. Zhao et al. 2009).

*Disk of **Rasalhague** (A5 III) resolved by CHARA (M. Zhao et al. 2009).

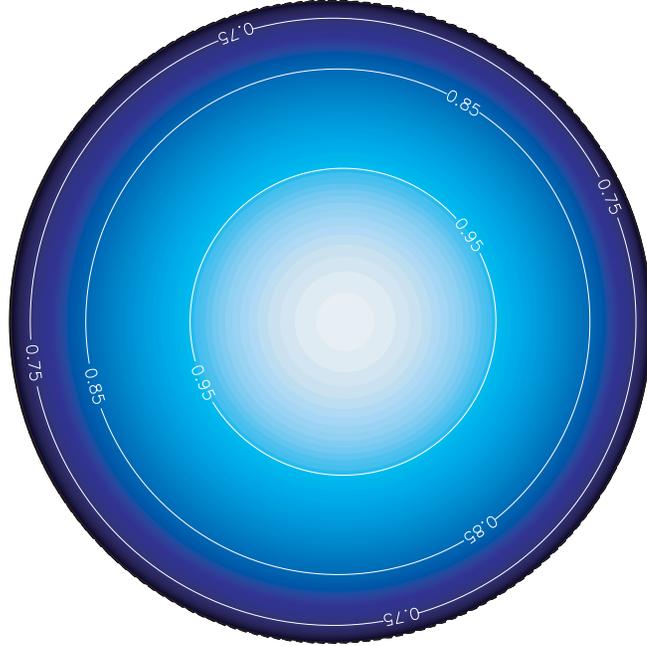
Gravity darkening in rotating stars

F. Espinosa Lara^{1,2} and M. Rieutord^{1,2}

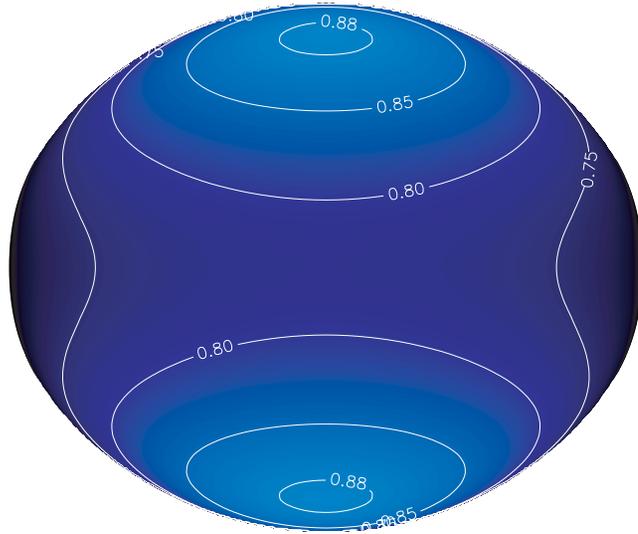


• **Observations by CHARA/MIRC show gravity darkening weaker than $\beta=0.25$**

Limb and Gravity Darkening for Rotating Stars



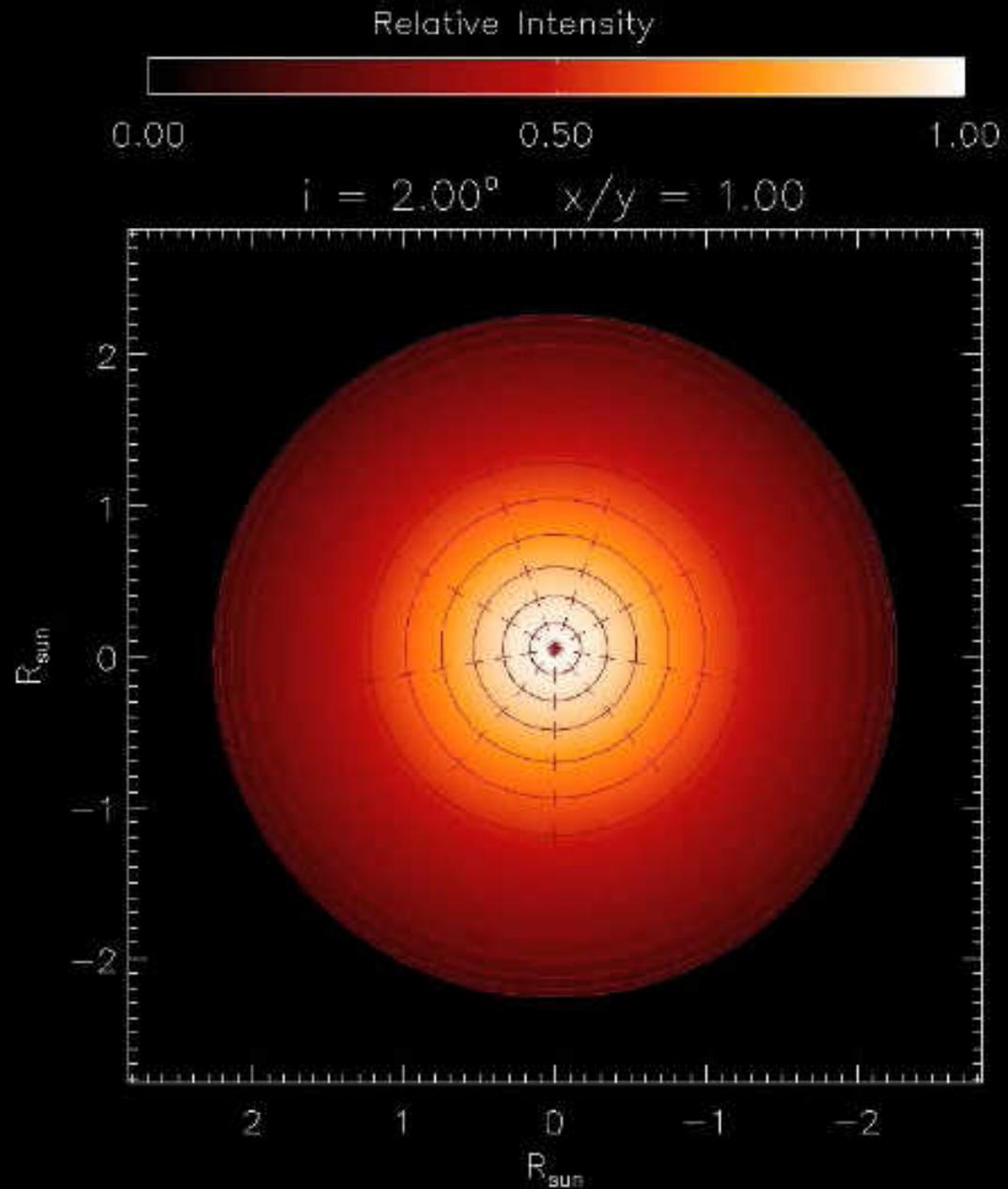
Pole-on view



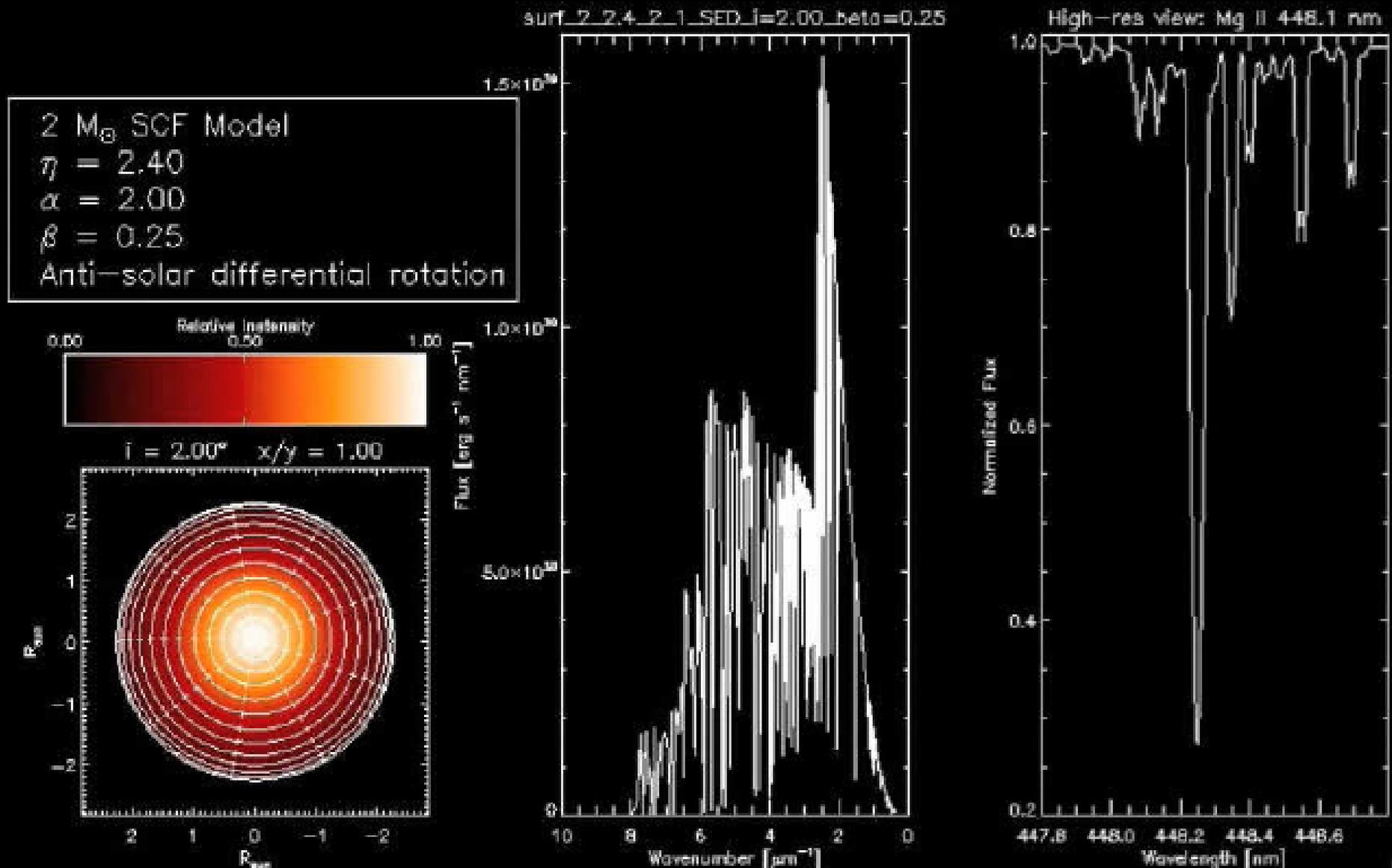
Equator-on view

Self-Consistent Field (SCF) Model Limb and Gravity Darkening Movie

Aufdenberg & MacGregor,
in preparation



SCF Models: SEDs and Line Spectra Movie



Aufdenberg & MacGregor, in preparation

Interferometry at visible wavelengths:

higher angular resolution --> O & B diameters & darkening

limb darkening more sensitive to temperature gradients

**Thank you for
your attention!**